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RAREBOOKCOLLECTION

The John J. and Hanna M. McManus and Morris N. and Chesley V. Young Collection
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## Onthe Frontilpice and Booke.

A LL Recreations do delig bt the minde, Buit shefe are beft being of a learned kinde: Here Art and Nature frive sogive content, In hewing wany a rare experiment; Which you may reade, and on their Schemes here looke Botbin the Exontifpice, and in the Booke. Vpin whofe table new conceats are fet, Like daziti diffes, ther cby for to mbet And minne your jsagement, with your appetite To tafte ibem, and therein 10 take delight. Thi Senfes objects are but dull as beft, But Art doth give the Intelle eit af caff. Come listher then, aud bere I will defcribe, What this fame table doth for you provide. Here Queltions of Arithineticke are wrought. And hidden fecrets unto light are brought, The like it in Geomerric doth anfold, And forse too in Cofmographic are told: It diver fepretby Dyalls doth deforie, Wiŝh frange experiments in Aftronomic, And Navigation with eaeh fever all Pisture, In Muficke, Opticke, and in Architecture: In Staticke, Machanicks,and Chimeftrie, In Waterworkes, and to afcend more bie, In Fireworkes, like to Ioves Arcillerie. All this 1 know thous in this Booke fhalt finde, And bere's enough for to content thy minde. For from good Authors, this our Author drew Thefe Recicurions, which are for ange, and truc. So chat ins Boolce's a Center, and tis fit, Thas in sbis Center, lines of praife fould meete.

## Jan caak: $\ldots 4^{\text {b }}$ Mathematicall Recreations.

## Or a Collection of fundrie Problemes,

 extracted out of the Ancient and Moderne PhiloSophers, as fecrets in nature, and experiments in Arithmeticke, Geoneetrie, Cof magraph bie, Horologographie, Afronomie, INavigation, Musicke, Opticks, Architectere, Staticke, Machanicks, Chimefrie, Waterworkes,Firemorks,sc. Not vulgarly made manifeft untill this time : Fit for Schollers, students, and Gentlemen, hat defirit to know the Pbilufopiticall curfe of many admirable Condufions.Vefull for others, to acuate and firre them up to the fearch of further knowledge ; and ferviceable to all for many excellent things, both for pleafure and Recreation.

Moft of which were written firft in Greeke and Latinf, lately compiled in French, by Henry Van Etters Gent. And now delivered in the Eng'thotongue, with the Examinations, Correfitions, and Augmentations.

Printed at London by T. Cotes, for Richard Hawkins, dwelling in Chancery Lame, neere the Romles, $16_{33}$.
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## т 0

## The thrice Noble and

 moftgenerous Lo.the Lo. Lambert Verreyken,Lo. of Hinden, woivershems, zer.CMy bonorable Eo.


Mongt the rare and curious Propofitions which I have learned out of the ftudies of the $\mathrm{Ma}_{-}$ thematicks in the famous Vniverfitic of Pont a Mouffon, I have taA $_{3}$ ken

## The Epifle Dedicatery.

ken fingular pleafure in certaine Problemes no leffe ingenious than recreative, which drew me unto the fearch of demonftrations more difficult and ferious;fome of which I have amaffed and caufed to paffe the Prefle, and herededicate them now unto your Honour; not that I account them worthy of your view, but in part to teftifie my affectionate defire to ferve you, and to fatisfie the curious, who delight themfelves in thefe pleafant ftudies, knowing well that the $\lambda_{0}$ billitie, and Gentrie rather ftudie the Mathematicall Arts, to content and fatisfie their affections, in the feculation of fuch admirable experiments as are extracted from them, than in hope of gaine to fill their Purjes. All which fludies, and others, with my

## The Epifle Dedicatory.

 whole indevours, I fhall alwayes dedicate unto your Honour, with an ardent defire to bee accouted ever,Your moft bumble and obedient Nephew,<br>and Servant

H. Van Etten。
$\wedge_{4}$


## Tothe Reader.


$T$ bath beene obleved by many, that fundry fine wits as well among $f$ the Ancient as Moderne, bave fported aud delighted themfelves upon Jeverall things of fmall conjequence, as upon the foote of a fly, upon a ftraw, upon a point, nay mpon nothing; friving as it were to fhew the greatne ffe of their glory in the jmals neffe of the jubject: And bave amongst moft olid and ar tificiall conclufions, compofed and produced fundry inventions both P hilofophicall and Mathema-

## The Epifle to the Reader.

 ticall, to folace the minde, and recreate the fpivits, which the Jucceeding ages bave imbraced; and from them gleaned and extracted many admirable, and rare conclufions, judging that borrowed mat. ter of tentimes yeelds praife to the indufrie of its author. Hence for thy u/e - (Courteous Reader) I bave with great fearch and labour collected al o, and heaped up together in a body of thefe pleafant and fine experiments to fisrre up and delight the affectionate, (out of the writings of Socrates, Plato, Ariftotle, Demofthenes, Pythagoras, Democrates, Plinie, Hiparchus, Euclides, Vitruvius, Diaphantus, Pergzus, Archined es, Papi Alexandrinus, Vitelius, Ptolomeus, Copernicus, Proclus, Mauralicus, Cardanus, Valalpandus, Kepleirus, Gilbertus, Tychonius, Dureirus,Iofepheus, $\mathrm{Cl} a-$ vius, Gallileus,Maginus,EuphanusTiberill,

## The Epifle to the Reader.

Tyberill, and otbers) knowing that Art imitating nature, glories alipayes in the variety of things, which ghe producetb to fat isfie the minde of curious inquifitors. And though pertaps thefe labours to fome bumorous per fons may jeeme vaine, and ridiculousifor fuch it was not undertaken. But for thefe which intentively bave defired and fought after the knowoledge of theefe things, it being an invination and motive to the fearch of greater matters, and to impley the minde in ufefull knomiedge, rather than to be bufied in raine Pamphlets, Play-bookes, fruitlefle Legends, and prodigious Hiftories that ale invented out of fan= cie, which abufe many Noble fpirits, dull their wits, ev alienate heir thoughts from laudable and bonourable Atudies. In this Tractate thou maift therefore make choife of Juch Mathematicall Problemes and Conclufions as may

## The Epitle to the Reader.

delight thee; which kind of learning doth excellently adorne a man, Seeing the wefulneffe thereof, and the manly accompli(hments it doth produce: profitable and delightfull for all forts of people, wobo may furnih and adorne themfelves woith abrudance of matter in that kind, - to belpe them by vbay of $u$ e, and dijcour $\int$ e. And to this we have alfo added our Pyrotechnie, knowing that Bealts bave for their object onely the furface of the earth; but boping that thy /pirit which followeth the motion of fire, will abandon the lower Elements, and caufe thee to lift up thine eyes to foare in a bigher Conteqnolation, baving foglittering a Canopie to behould; and thefe pleafant and recreative fires afcending may caufe. thy affections alfo to afcend. The Whole whereof we fend forth to thee, that defireft the Jcrutabillity of things; Na ture baving furnifhed us with matter,

The Exile to the Reader. thy Spirit may eafily digest them, and put them finely in order, though nov in diforder.

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3 Incident: Bewerth the deceit of pipes which conveies water, that a pipe of two inches diameter, doth caft out foure times as much pater as a pipe of one fuch diameter. 218 7 beaps of Corne of 10 -foote every may, is wot a wich as one heape of Corne of 20 . foot every may.

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$23^{2}$

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## FINIS:



# By vvay of advertifement. 

Five or fixe things 1 have thoughtworthy to declare before I paffe further.


Irft, that 1 place sot the fpeculative demonftratiows with all thefe Problemes, but content my Jelfo to fhew them as at the fingers cad: which was wy plot \& intention, becaufe thefe which under: Aland the matheraticks can conceive them eafly; others for the mof part will content themfelves onely rith the knowledge of them, urithout feeking the reafon.
Secondly, to give a greater grace to the pract ife of the fe things, they ought tobe concealed as much as they may, in the fubtiltic of the way for that which doch ravibuthe spirits is, an admirable effeet, whole caufe is unknowne : which if it were difcovered, balfe the pleafure is loft, therefore all the fineneffe, COR-

## By way of Advertifement:

 confifts in the dexterity of the $A C T$, concealing the meanes, and charging ofien the flreamse.Thirdly great care ougbt to be had that one deceive not bimfelfe, that wonla' declare by way of Art to deceive another: this woll make the matter conteriptibie to ignorant Perlons, widuch will ratber caft the fanlt upon the Science, than upon be that /hewes it: when the caufe is not in the Mathematicall princi. ples, but in bim ibat faybes in the acting of it.

Fourthly, in certaine Arithraeticall propofrions they bave onely their anforers as I foond them in fundry Authors, which any one being fudious of Marhemaricall learzing, masy finde their origimatl, and alfo the 2vay of their operation.
Fiftly, becaufe the number of there Problemes, and ibeir dependences are many, and intermixed, I thougbs it convenient logather ibeminto a Table: tbat fo cach one accarding to bir fancie, might make bef choife of that whish might befi pleaje bas palet the watter being not of onse nacure, nor of like fubtiltie: Bat whofoever will bave patience to resdeon, Jall finde the end better than the begixning.

# MATHEMATICALL KECREATION. 

Problemet.

To finde a number thought upos.


Id him that hee Quadruple the Nomber thoughe upon, that is, multiply it by 4 and unto it bid hion to adde, 6.8.10. or 2ny Nomber at pleafure : and let him take the halfe of the fumsae, then aske how auch it comes to : for then if yout take away halfe the Nwmber from it which you willed himat firft to adde to it, there Shall remaine the doable of the number. theughe upon.

## Examphor

The 2 vumber thoughe upoa.
The Quadruple of it.

$$
5
$$

Put 8. unto ie, makes
The halfe of it is added fro it, viz. 4 .the reft is $\}$ viz'

A Another way to finde what number was thought upon.

BId him which thinketh, double his $N u m$. ber, and unto that double adde 4.and bid him multiplie that fame product by 5 , and unto that product, bid him adde I2. and multiply that Jait number by 10 . (which is done eafily by fet: ting a Ciphar at the end of the number:) then aske him the laft number or produet, and from it fecretly fuberact 330 . the remainder in the huadreth place, is the number thought upon.

> Example.

The number thought upon 70
His double
To itadde 4 makes
Which muliplied by s-maks 90. To which ad 12 makes 102. This multiplied by 10 ) whichis onely by adding a Ciphar to it, [020. ding a From thisfubtract Reft

For which 700 account onely but the number of the hundreds viz. 7. fo har: you the numbr thoughr upolit

## Mathematicall Resreation.

To finde numbers corccived upon orbermife than the former.

BId the partie which thinkes the number, that he triple his thought, caule him to take the halfe of it : if it be odde take the leaft halfe Numand put one unto it,: then will him to Triple id hinthe halfe and take halte of it as before ; laftly, to thaske him how many nines there is in the laft $y$ thehalfe, and fos every 9. account 4 . in your meby fe morie, for that thall thew the number thoughe ) the upon, if both the Triples were even: but if an it be oddeat the firf Triple, and even as the aind fecond, for the one added unto the leaft halfe hough keepe one in memorie : if the firt Triple be even and the fecond odde, for the one added unto the leaft halfe keepe two in memorie:laftly if at both times in tiipling, the numbers be odde, for the two added unto the leaft halfes, keepe three in memorie, thefe cauriois obferved and adkd unto as many fowe $s$ as the partic fayes there is nines contained in the laft halfe, fhall never faile you to declare, or difcerne truly what number was thoughe upon. Example.
The namber thoughr upon, The Triple

4, or 7.
$12.0 r 2$ !.
The halfe there of 6 , or 10 . I put to it malies $1 .{ }^{(1)}$ The Triple of the halfe
The halfe $\sigma$.or 16.1 put to it maks

## Mathematicall Recreation.

The firft 1 , reprefenteth the 4 number though upon, and the laft 8 . with the caution makes 7 the other number thought upon.

## Note.

Order your method fo that you bee not dif covered: which to helpe you may with dexteritie, and induftrie make additions, fwh. tractions, multiplications, divifons, ซfc. and in ftead of asking how many nines there is: yon may aske how many eights, tens, acc there is, or fubtract 8.io. \&c. from the number which remaines, for to finde our the number thought upon.

Now touching the Demonftrations of the former directions, and others which follow, they depend upon the 2.7.8 and 9. Baoke of the Elements of Ewclid: upon which 2 . Book and 4 propofition this may bee extracted for there which are more learned for the finding of any number that any one thinketh on.

Bid the partie that thinkes, that bee breakt the number thought upon into any two parts and unto the fquares of the parts, let hion addel the double produrt of the parts : then askt what it mixounteth unto, fo the Root 2wadramet thall bethe number thought upon.

## The nwmber thought upon s.tbe parts Euppofe 3 .and 2 .

## Mashematicall Recreation.

1 10ugT The fquare of 3.makss. The fumme of the'e three numbers 2 s.the The product of 2 three numbers 2 s.the the parts viz.3, $b_{1}{ }_{12}$ is 5. the number 2. makes 6. which $\mathbf{6}$. doubled makes thought upon.

Ormore compendioufly, it may beddivered thus,

Breake the number into two parts, and to the product of the parts, adde the Square of ere halfe the difference of the parts, then the Root 15,8 2madrate of the azgregare is halfe the number mmonceived.

## EXAMINATION.

 He Problemes which comcern Arithmetick, we examixe not, for thefe are eafle to any one which hath read the gronnds and prim resiples of Arithmeticke : but we effecially tonch prixpon that, which tends to the pieculations of arphyficke, Geomerrie and Optickes,and fucho. 1 ai hers mbich are of more difficultie, and more uipriscipally to be examined and cosfidered.- 

B
Pros,

## 橉

## Masthematicall Recreation,

Probiemill.

How to reprefent to the se which are in a chamber that robich is with-
out, or all that which
paferthby.

THis is one of the fineft experimerts in the Opticques, and it is done thus, chufe a Chamber or place which is towardsthe ftreet, freguented with people, or which is againt fome faire flourifhing object, that fo it may be more delightfull and pleafant to the beholders, then make the Rodme darke by Chutting out the lighr, except a fmall bole of fixe pence broad, this done, all the Images and fpecies of the object which are without, will be feene within : and you fhall have pleafure to feeit not one ly upon the wall but elpecially upona theete of white paper or lome white cloth hung nere the bole: and if unto the bole you place a round Glafle, that is,a Glaffe which
 is thicker in the middie than at the edge: fuch as is the common burning Glafes, or fuch which old people ufe, for then the Images which before did feeme dead, and

## Matbematicall Recreation.

of a darkifh colour, will appeare and be feene upon the paper, or white cloth, according to their naturall colours, yea mote lively than their naturall; and the appearances will be fo much the more beautifull, and perfect, by how much the bole is leffer, the day cleare \& the fun Sinining. It is pleafure to fee the beautifull and goodly reprefentation of the Heavens, intermixed with clouds in the Horizon, upon a wooddy fituation, the motion of Birds in the Alire, of Men, and other Creatures upon the ground, with the trembling of Plants, tops of Trees, and fuch like, for every thing will be fectre within even to the life, but in ecred: notwithftanding this beautifull paint will fo naturally reprefent it felfe in fuch a lively perspective, that hardly the moft accurate Pain. ter can reprefent the like. Now the reafon why the Images and objects without are inverfed, is becaufe the $\beta$ pecies doe interfect one another in the bole: fo that the fpecies of the feeteafcend, and thefe of the head defcend.
But heere note, that they may be RepreCeated right two manner of wayes; firft with a concaze glaffe, fecondly, by helpe of another convex glaffe: difpofed or placed betweene the paperand the other Glaffe:asmay


## Mathematicall Recreation.

be feene here by the figure.
anw I will adde here onely by paffing by fo fuch which affect painting, and pertraiture that this experiment may exceliently helpo them, in the lively painting of things per. 1pective wife, as Topographicall cards, ©cr.and for philooophers, it is a fine fecret to explaine the organ of the fight, for the hollow of the sye is taken as the colofe Chamber, the balle of the Aple of the eye, for the bole of the Chame. ber, the Gryfalline bumor at the fmall of the Glaffe, and the bottome of the eye, for the mal, or leaft of $P$ aper.

## 

## EXAMINATION.

17 is falfethat the fpecies being prefled tofe ther or contraged doth performe it upos a wall, for the fpecies of any thing dotb reprefent is felfe xot oxely in one hole of a window, but is infnite bolesiereen unto the whole Spheare, or at Seaft unto a Hemifpheare (intelecterwall in afve medium) if the bearmes or refections be not inter. pofed, © by how much the hole is made lofotit give paffage to the feccies, by fo macb the more sively are the Images formed.
In convexe, or concave Glaffes the Images will be difiproportionable to the eye, by bow mush they are more concave, or convexs, and by hom

## Mathematicall Recreation.

 nuclo the parts of the Image comes neare to the Axis, for the fe that are seare are better proportionated, than thefe which are farther off.But to bave them more lively, and trae, according to the imaginaris conicall fellion, lee the bole be no greater than a pins head moade upen a peece of thinne Braffe, or fuch like, which hole reprefents the top of the Cone, and the Bafe thereof the serme of the fpecies: this pradice is bef whies the Sunne Bines apon the bole, for then the objeits which are oppofite to that plaine, will nake two like Cones, and will lively reprefent the things without, in a perfoa inverjed jerpe tive, whicich drawne by she Penfell -f fome artificiall painter, twrwe the paper upfide downe, and it will be direet, and to the life.
But the apparences may be direct, if you place another hole oppofite unto the former fo that the $\sqrt{P}$ - Elator be sunder it ; on let the /pecies reflect upos a Concave Glaffe, and let that Glafe reflect wpon 'apaper, or fonse white thing.

## Probinm. III.

Totell bow much waighs the blow of ones fff, of a Mallet, Hatchet or fuch like, or reffing without giving the blow.

SCaliger in his 33 I . exercife againt Cardan, relates that the CWathematitians of Maximillians the Ewperowr did propofe upon a day B. 5

## Nathematicall Recreatioss.

this Qneffiow, and promifed to give the refolution; notwithtanding Scaliger delivered it not, and I conceive it to be thus. Take a Balanea, and let the fift, the Mallet or Ha:chet reft upon sthe Scale or upon the beame of the Ballance; and put into the other foale, as much weight as may counterpoyfe it ; then charging or laying more waight into the Scale, and ftriking upon the other end: you may fee how much one blow is beavier than another, and fo confequently how much it may waygh;for as eArifotle faith; the motion rbat is made in friking ads great waight unto it; and fo muct the more, by bow much it is quicker : therefore in effect if there were placed a thoufand. mallets, or a thoufand pound waight upon a ftone, nay though
it were exceedingly preffed downe by way of a vice, by levers or other mechanick $\mathrm{nn}^{-}$ gine, it would be nothing to the rigor and violence of a blow.
Is it not evident that the edge of a knife laid upon butter, and a batchet upon a leafe of Pa per, without ftriking makes no impreffion, or at leaft enters not; but friking upon the rrood a little,you may prefently fee what effect it hath, which is from the quickneffe of the motion, whichbreakes and enters without refiltance,
f it be extreame quicke, as experience fhewes us, in the blowes of Arroms, of Cannons, $T$ bwo derboults, and fuch like.

## 

## EXAMINATION.

THis Probleme was extratied from Scaliger, who bad it from Ariftotle, but Somewhat refraftory compiled, and the ftrength of the effect be fayes depends oncly in the violence of the motion; then would it follow that a little light hammer upon a peece of wood being quickly canfed to mite, mould give a greater blow and doe more hurt than a great ledge friking foft; this is abfurd, and contrary to experience: therefore it confifts not totally in the motion, for if to Severall bammers, the ore being 20. times heavier than the other, hould move woithlike guickreffe, the effelt mould be much different; there is then fome thing elfe to be confidered befides the Motion which Scaliger underftood not, for if one foould have asked him, what is the reafon that a fone falling from a window to a place neare at hand is not $f$ o forceable, as if it fell farther downe; and when a bullet flying out of a peece and froking the marke neare at hand, mill not make fuch an effect as friking the marke furtber off: but weee suppose that Scaliger and Cardanus who banales this fubject, would not

## Mathematicallaccreation.

beeleffo troubled to refolvo this, than they have Geese is that.

## Problem. IIII.

How to breake faff which is laid upon two Glaljes full of water, without breaking the Glaffe, Billing the water, or aton two Reeds or Strawed without breaking -f them.

FInf place the Chafes which are full of water upon two joynt fiooles, or fuck like, the one as high as the other from the ground, and diftant one from another by 2. or 3 . foote, then place the ends of the ftaffe upon the edges of the two Gaffes fo that they bee sharpe; this done with all the force you can, with another $f$ affe trike the fife which is upon the two glafor in the middle, and it will break without breaking the Glafles or filing the water. In like manner may you doe upon two Reeds, held in the are without breaking
 them: thence Kitchenbayes often brake bones of mutton upon their hand, or with

## Mathematicall Recreation:

wapkin withour any hurt, in onely friking upon the middle of the bone, with a knife.

Now in this act the two ends of the flaffe in breaking flides away from the Glaffes, upon which they were placed; hence it commeth that the Glaffes are no wife indangered, no more than the knee upon which a fraffe is broken, for afmuch as in breaking it preffeth not: as Ariftotle in his Mechamicke quefiows oblerveth.

## 

## EXAMINATION.

ITwere meceffary here to noto, that this thing may be experimented, firft, withoas Glaffes, in plac ing a fmall Render Staffe upon two props, and then making tryall apon it, by which you may See bow the Staffe will either breake, bow, or depart frome his props : and that eyther directly, or obligwely: But woby by this violence, that one Staffe friking anotber, (which is supported by two Glaffes) will bee broken prithout offending the Glaffes, is as great a difficultio to be refol. yed as the former.

How to make a faire Geographicall Card in a Garden Plot, fit for a Prince, or great perfonage.

$\mathrm{I}^{T}$$T$ is ufuall amongt great men to have faire Geographicall mappes,large Cards, and great Globes, that by them they may as at once have a view of any place of the world, and fo furnith themfelves with a generallknowledge, not onely of their owne kingdomes forme, fituation, Longitsede, Latitude, coc. but of all other places in the whole Vnivet fe, with their Magnitudes, Pofitions, Climats, and diftances.

Now I efteeme that it is not unworthy for the meditations of a Prince, feing it carries with it many profitable and pleafant contentments : if fuch a Cord or CWrappe by the advice and direction of an able Marbematitian were Geographically defcribed in a Garden plot forme, or in fome other convenient place; and in ftead of which generall defcription might particularly, and Artificially be prefigured his whole kingdomes and dominions, the cMour. taines and Hils being raifed like fmall billocks with curfes of earth, the vallies fomew hat concave; which will be more agreeable \& pleafing to the Eye, than the defcription in plaine Mapps and Cards, within which may be prefenred, the townes, villages, Caffles, or other remarkeable edifices in fmall greene Miofje bankes, or fringmorke propartionall to the plat forme,

## Masthematicall Recreation.

the forreffs and woods reprefented according to their forme and capacitie, with hearbs and Itoubs, the grear rivers, lakes and ponds, to dilate themfelves according to their courfe from fome Artificiall fountaine made in the Garden to paffe through Cbanels; then may there bee compoted walles of plealure, eAfcents, places of repofe adorned with all varietie of delightfull bearbs $\&$ fowers, both to pleale the eye, or ocher fences. A Garden thus accommodated Thall farre exceede that of my Lo. of Verulams fpecified in his Effayes; that being onely for delight and plafure, this may have all the properties of that, and alfo for fingular ufe, by whicha Prince may in little time perfonally vifite his whole kingdome, and in flort time know them diftinctly, and fo in like manner may any particular man Geograpbically prefigure his owne poffeffion, or heritage.
PROBLEM. VI.

How three ftaves, knives, or likebodies may be conceaved to bang in the Aire, withont being fupported by any thing, but by themfolves.
Cotke the firt ftaffe $A . B$. raife up in the - Aire, the end $B$. and upon him crofwife place the faffe $C$. $B$. then laftly in T riangle wife place the third $f$ affe E. F, in fuch manner that it may be under $2 A_{0} B$. and yer upon C.D. I fay that thefe ftaves fo difpored cannot fall, and the
the fpace C.B.E, is made the fronger, by how much the more it is preffed downe, if the Faves breake not, or fever themfelves from the triaxgular formes fo that alwayes the Center of gravitie be in the Center of the Triangle: for A.B. is fupported by $E$. $F$. and $E, F$. is helde up by C.D. and C. D. is kept up from falling by A. B therefore one -t thefe ftaves carnot fall, and fo by confequence none.

> Probiem Vif.

How to dipose as many mex, or other things, in fuch fort thatrejelting, or cafting amay the 6.9.I0. Part, wento a certaine nnmber, there foall remaine thefe wich yon wosld bave.

oRdinarily the propofition is delivered inthis wife: I 5.Chriffinns and 15.1 wrkes being at Sea in one Shippe, an extreame tempeft being rifen, the Pilot of the Shippe fay it is neceffary to caft over board halfe of the number of Perfons to dilburthea the Shippe, and

## Mashemasicall Recrestion.

to fave the reft : now it was agreed to bee done by lot and theretore they content to pur themflives in ranke, couring by mue a a d mue the ninth Perfon fhould alwayes be caft into the Sea, untill there were halfe throwre ocer board; Now the Pilote being a chriftuan indeavoured to fave the Chriftians, how oughs hee therefore to difpofe the Chriftems, thas the lot might fall alwayes upon the Turkes, and that none of the Cbriftians be in the ninth place?

The refolution is ordinarily comprehended in this verfe,

> Populeanv virgam mater regina ferebat:

For having refpect unto the vowels, making $a$ one, $e$ two, $i$ three, o foure and $k$ five: o the firft vowell in the firft word fheweth that there mult bee placed 4. Cbriffians, the next vowell e, fignifieth that next unto the 4. Chriftiass muft be placed 5:Turkes, and fo to place both Cbriftians and Turkes according tothe quantitie and value of the vowels in the words of the verfe, untill they be all placed: for then counting from the firlt Chriftian that was placed, unto the ninth, the lot will fall upon a $T w k e$, and fo proceede. And here may be further noted that this 'Probleme is not to bee limited, feeing it extenis to any number and order whatfoever, and may many wayes bee ufefull for Captaines, Magifirats, or others is which have divers perforis to punim, and would n- chaftife chiefeiy the uarulieft of them, in taking the Io. 20.0r Io0, perfon; $2 \times c$, as we reade was
commonly pratifid amonget the ancient Ro. *ans: beretore to apply a generall rule in cuunting the third, 4.9. I0.ixc. amongt 30.40.50. perfons, and more or leffe; this is to bee otferved: take as many unites as there are per. fons, and difpofe them in order privately: as for example, let 24 . men bee propofed to have committed fome outrage, 6 . of them efpecially are found acceffry : and let it be agreed that counting by 8 and 8 . the tight man fhould be alwayes puninied: Take therefore firt 2 3. unites, or upon a peece of paper write downe twenty foure Ciphars, and account from the begianing to the eighth, which eighth marke, and fo continue counting aiwayes marking the eighth, untill you bave markt 6. by wlinch you may eafily perceive how to place thofe 6. men that are to betpu. nifhed, and fo of orhers. It is fuppofed that Io* Sephes the Author of the Iewißh Hifory, efcaped the danger of death by helpe of this Proo bleme; for a worthy Author of belic fe repors in his eighth Chapter of the third Booke of she deftruction of Yerufalem, that the Towne of lotapata being taken by maine force by $V_{b_{n}}$ Jatian; Io fephous being governour of that rowhe accompainet with a troope of 40 . Souldjess, hid themfelves in a Cave in which they refolved rather to famith than to fall into the hands of Vejpatian: and with a bloody refolution in that great diftreffe would have butchered one another for fuftenance: had not lofephus perCwaded them to die by

## Mathemaicicall Recreation.

Lor, andorder, upen which it Mould fall : Now feeing that Iofeplous did fave himfelfe by this Art: It is thought that his indufrie uas exercifed by the helpe of this Problcine: fo that of the 40 perfons which hee had, the third was al wayes killed. Now by putting himfelfe in the 36 or 3 r . place he was faved, and one with him which hee might kill, or cafily perfwade to yeeld unto the Remans.

LEt the three things bee a Ring, a peece of Gold, and a peece of Siluer, orany other fuch like, and let chom bee knowne privatly to your felfe, by theferhree vowels, $a \in \dot{i}$ or let there bee three perfons that have different names, as Ambrofe, Edrsond and Iobn; which privately you may note or account to your filfe once knowne by the aforefaid vowels; which fignifie for the firft vowell I. for the fecond vowell 3. for the third vowell 3 .

Now if the fayd three perfons fhould by the mutuall confent of each other privatly change their names, it is mof facill by the courle and excellencie of numbers; diftinctly ta declare each ones name, fo iuterchanged: or of shree per fons in private, the one hould take a Riny, the

## Mathematicall Recreation.

othar a peece of Gold, and the third fhould take a peece of Silver; it is cafie to finde which hath the Gold, the Silver, or the King, and it is thus done.

Take 30 or 40. Counters (of which there is but 24. neceffary) that fo you may conceale the way the better, andlay them downe before tl e parties, and as they fit or fland give to the firlt 1. Connter, which fignifieth a the fint vow.ll, to the focond 2. Counters which reprefents e the fecond vowell, and to the third 3 . Counters which fands for $i$, the third vowell: then leaving the oiher Counters upen the $T_{a}$ ble, retire apart, ard bid bim which hath the Ring, take as many Counters as you gave him, and hee that hath the Gold, for every one that you gave bim, let himstake 2 . and he that hath the Silver for every one thit you gave him let him take 4. this being done, confides to whon you gave one C cunter, to whom two, and to whom three; and marke what number of Counters you had at the firit, for there are necelfarily but 24. as was fayd before, the furplule you may privately reject. And then there will be left cither 1.2.3.5.6.or 7 . \& no other number can remaine, w ${ }^{\text {ch }}$ if there be, then they have failed in taking according to the directions delivered : but if either of thele numbers doe remaine, the refolution will bee difcovered by one of thefe 6. words following, whichoughe to be had in memory, viz. Sulve, certa, axima, femita, vita, quies. 1. 2. 3. 5. 6. 7 .

## Mathematical Recreation.

ind fin As fuppofe 5. did remaine,the word belongen ing unto it is femita, the vowels in the fort the it wo lillables are e and $i$, which fheweth actording to the former directions that to whom ichthe you gave 2. Counters he hath the Ring (ieeing ty con it is the fecond powell reprefented by two weber as before) and to whom you gave the 3 given Counters he hath the Gould, for that $i$ reproa the fens the third vowel, or 3 . in the former which direction, and to whom you gave one Connhethir ter, he hath the Silver, and to of the reft: the vardvor retie of changes in which exercife, is layd it he open in the Table following.

This feat may be done alto without the for men words by helve of the Circle A. for having divided the Circle into 6. parts, write I. within and 1 . without, 2. within and 5 . without, \& 2 c. the firf $1.2 \cdot 2$. which are within with the numbers over them, belongs to the upper femicircle; the other numbers both within and without, to the under Semicircle;

$$
C_{3}
$$

now if in the Action there remaineth fuch a number which may bee found in the upper/e. mecircle without, then that which is oppofice within fheuses the firlt, the next is thelecond, ecc. as if $s$. remaines, it thewes to whom hee gave 2. hee hath the Ring, to whom you gave 3. hee haxh the Gould Gc. but if the remainder bee in the under femicircle, that which is oppofite to it, is the fuft; the next backwards towards the right band is the fecons, as if 3 . remaines, to whom you gave 1 . he haththe Ring ; he that had 3 ,he had the Gould, orc.

## Problem. JX.

How to part a veffeltwibich is full of wine con. taining 8. Pints, into troo cquall parts, by two otber veffels mbich cortained as much as the greater ve $\int$ ell; as the one being s. Pints, and the otber 3 . Pints.

TAEt the 3. veffels be reprefented by A.B.C, fir $A$.being full, the uther two being emptie; firft powre out $A$. into $B$. uncillit bee full: fo there will be in $B .5$. Pints and in $A$.but 3. Pints; then powre out of $B$. into $C$. untill it bee full: fo in $C$. Thall be 3. Pints, in $B 2$ Pints, and in A3. Pints; then powre the wine which is in $C$. into $A$. fo in $A$. will be 6 . Pints, in $B 2$. Pints, and in $C$ nothing : then powre out the wine which is in $B$. into the pot $C$. fo in $C$. there
h fuch there is now 2 . Pints, in $B$. nothing, and in eA. upperf 6.Pints. Laftly, powre out of $A$, into $B$. untith oppofis it be full, fo there will
is the bee now in $A$. oncly? o who工. Pint, in B. 5, Pints, and in C. 2. Pints: But it is now evident that if from $R$. you powre in unto the pot C. untill it bee full, there will remaine in B.4. Pints, and if that which is in $C$.
viz. 3 Pints bee powred into the veffell $A$. which before had 1. Pint, there fhall bee in the veffell $A$. but halfe of its liquor that was in it at the firft, viz 40 Pints as was required. Otherwite powre out of $A$. into $C$. untill it be full, which powre ine to $B$ then powre out of $A$ into $C$, againe untill it bee full, fo there is now in $A$. omely z. Pints, in $B$. 3, and in $C_{3}$. then powre fron $C$ into $B$. untill it bee full; fo in $C$. there is now but 1 . Pint,5. in $B$. and 2 . in $A$. powre all that is in $B$. into eA. then powre the wine which is in $C$ into $\mathcal{B}$.fo there is in $C$. nothing, in $\mathcal{B}$, onely I Pint, and in A.7. Pints : Laftly out of A. fill the pot $C$.fo there will remaine in CA. $4 . F$ ints, or be but halfe full: then if the liguor in $C$.bee powred into $B$. it will bee the other halfe. In like manner might bee taken the halfe of a veffell which containes 12. Pints, by having bat the meafures 5 . and 7 . or 5 and 8 . Now.

## Mathematicall Recreation.

fuch others might be propoled, but wee omit many, in ore and the fame nature.

> PROBLEM. X.

## To make a ficke frand upon the tipp of ones finger, withiut falling.

FAften the ed, es of two knives or fuch like of equail poile, at the end of the fricke, leaning out fomewhat from the ficke, fo that they may connterpoife one another; the ficke being foarpe at the end and held upon the top of the finger, will there reft without fupporsing : if it fall it muit fall together, and that perpendicular or plambe wife, or it mult fall fide-wife or before one another; in the firft manner it cannot: for the Center of gravitie is fupported by the rop of the finger:and feeing that each part by the knives is counterpoyfed it cannot fall
ii tewife, therefore it cannot fall no wife.
Inlike manner may great peeces of Timber. as hoiffs\&c.be fuppoited, if unto one of the ends be applyed cunvenient proportionall counterpoifes, yea a Lance or Pike, may fland finger : or placed in the midft of a Court by helpe of his Center of gravitic.

## 

## EXAMINATION.

THis Propofition Sermes doubtfull for to imagine abfolutely, that a Pike, or fuch like, armed with two knives, or other things foll fand upright in the Ayre, and foremaine without any ot ber fupport, Jeeing that all the parts hath an infinite differ ence of propenfitie to fall; and it is mithort queffion sbat a tlaffe So accömpodated upon bis Center of gravitie, but that it may incline to fome one part without fomse remedie be applyed, and fuch as is bere ppecified in the Probleme will not warrant the thing, nor keepe it from falling; and if more knives frould be placed about it, it homld canfe it to fall more swiftly, for afmuch as the fuperiour parts (by reafon of the Centricall motion) is made more ponderous and therefore leffe in reft.

Toplace therefore this prop really, let the two knives,sr that which is for counterpoife, be longer alwaies than the ftaffe and fo it will hang to. gether as one body: and it will appeare admirable if you place tbe Center of gravitie, neare the fide of the top of the finger or point; for it will then bang Horizontall, and feeme to hang onely by a tonch, yet piore ftrange if you turize the point or top of the finger apfide domne.

Prob.

Problem. XI.

How a milftoneor other Ponder oftie, may be fupo ported by a fmall needle, without breaking or any wife bowing the fame.

LEt a needle be fet perpendicular to the Horizoo, and the center of gravitic of the ftome, be placed on the top of the 7 Tedle : it is evident that the ftone cannot fall, for afmuch as it hangs in aquilibra, or is counterpoyfed in all parts alike; and moreover it cannot bow the 2 ceedle more on the one fide, than on the other, the Reeedle will not therefore be eythes broken or bowed; if otherwife, then the parts of the Tedede mult penitrate and finke one with anothet : that which is abfurd and impoffible to natare : therefore it fhall be fupported. The experiments which are made upon trencher plates, or fuch like leffier thing doth make it moftcredible in greater bodies.

But here efpecially is to bee noted that
 the ACedic ought to be unitorme in matfer and figure, and that it be erected perpendicular to the Horizom, and laftly that the Censer of gravitie be cxactly found.

Prob.

## Mathomaticall Recreation.

PROBIEM. XII.
To make three knives bang and nove upon
the point of N Needle.

FIt the three knives in forme of a ballance, and houlding a Needle in your hand, and place the backe of that knife which lies croffewife to the 0 ther two, upon the point of the Needle: as the figure here Theweth you, for then in blowing foftly up-
 on them, they will eafily turne \& move upon the point of the meedle without falling.

## Problem. XIIf.

To finde the weight of fmoake, which is exbaled of any combuftible body what oever.

IEt it be fuppofed that a great heape of $F a$ gots, or a load of ftraw waying soo 1 fhould be fired, it is evident that this groffe fubftance will bee all inverted into fmoake and Ages: now it fecmes that the fmoake waighes nothing; feeing iti is of a thinne fubftance now delated in the efire, notwithftanding if it were gathered and reduced into the thickelt
kelt that it was at firft，it would bee fenfibly waighty：waigh therefore the afhes which admit so pound，now feeing that the reft of the matter is not loft，but is exhaled into fmoke， it muft neceffarily bee，that the reft of the waight（to wit） 450 pound，muft bee the waight of the fmoke required．

## 上2， <br> EXAMINATION．

NOw although it bee thus dolivered，yet here may be noted，that a ponderofitic in his owne medium is sot waightio：for things arefayd to be waighty，when they are out of their place，or meainm：and the difference of fuch gravitie，is according to the motion：the \｛moke therefore certainely is light being in its true medium（the ayre）if it fould change bis medi－ um，thers mould we cbange our difcourle．
Problem. XIIII.

Many things beingldifoo fed circular，（or other－ wise）to find which of them，any one thinkes кpon．

Suppofe that having ranked 10 things，as N．ABCPEFGHIK，Circular（as the figure fheweth）and that one had touched or thought upon $G$ ．which is the $\eta$ ：aske the partic at what letter he would begin to account（for
up
$\qquad$

## Mashematicall Recreation.

count he muft, otherwife it cannot bee done) which fuppole, at $E$ which is the .s place, then ad fecretly to this 5. 10. (which is the number of the Circle) andit makesis, bid him account is. backward from $E$, begimning his account with that number hee thought upon,fo at $\varepsilon$ hee fhall account to himfelfe, 7, at $D$ account 8 , at $C$ account 9 \&ic. So the account of is will exactly fall upon $G$, the thing or number
 thought upon: and foof others: but to conceale it the more, you may will the party from $E$ teaccount 25 . 35 \& c . and it will be the fame.
There are fome that ufe this play at cards, turned up fide downe, as the ten fimple Cards, with the King and Queene, the King flanding for 12 , and the 2 ueene for 11 , and foknowing the fcituation of the Cards: \& thinking a certaine houre of the day: caufe the partic to account from what Card hee pleafeth: with this Provifo, that when you fee where hee intends to account fet 12 . to that number, fo in counting as before, the end of the account thall fall upon the Card:which fhall denore or fhew the houre thought upon, which being turned up will give grace to the action, and wonder to thofe thatare ignoranr inthe caule:

## Mathematicall Recreation.

> Problem, XV.

## How to make adore, or a Gate, which Ball opens on both fides.

ALL the skill and fabtiltie of this, refts in the artificiall difpofer of 4 plates of lron; $^{\prime}$ two at the higher end, and two at the lower end of the Gare: fo that one fide maymove upon the hookes or hindges of the Pafts, and by the other end may be made faft to the Gate, and fo moving upon there hindzes, the Gate will open upop one fide with the aforelayd plates, or hookes of Iron: and by helpe of the other two plates, will open upon the other fide.

## ar) Problem. XVI.

To Sow how a Porderofitie, or beavie thing. may be fupported tipon the end of a ftaffe (or fuch like) upon a Table, and nothing bolding or toncling it.

TAke a paile which hath a handle, and fill it full of water (or at pleafure:) then takea ftaffe or fticke which may not rowle upon the Table as E C, and place the handle of the Paile upon the faffe; then place another Faffe, or Aticke

## Mathematicall Recreation.

Aicke, under the flaffe $C$, which may reach from the bottome of the Paile unto the former ftaffe $C \mathcal{E}$, perpendicular wife: which fuppore F.G, then fhall the Paile of water hang without falling, for if it fall it
 muft fall perpendicularly, or plumbe wife: and that cannot bee recing the ftaffe CE, fupports it, it being parallel to the Horizon and fuftained by the Table, and it is a thing admirable that if the faffe C E, were alone from the table, and that end of the flaffe which is upon the Table were greater and heavier than the other : it would be conftrained to hang in that nature.

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## EXAMINATION.

NOw without fome experience of this Problemo, a man would acknowledge cither a poffibulity or impoffibilitie; therefore it is that very touchftone of knowledge in any thing, to difcourfe firft if a thing bee poffible in nature, and then if it can bee brought toexperience and under fence without feeing it done At the frft, this propontion feemes to be abfurd
abfurd, and impoffi'sle at the firt. Notwithftanding, being fupported with two Iticices as the figure declareth, it is made facill: for the Hortzontall line to the edge of the $T$ able, is the Center of mosion; and palfeth by the Center of gravitie, which neceffarily fupporteth it.

1 Problem. XVII.

## Of a deceitfull Bowle to play withall.

MAke a hole in one fide of the Bowle, and calt moulten Lead therein, and then make up the hole clofe, that the knavery or deceit be not perceived:you will have pleafure to fee, that notwithftanding the Bowle is caft directly to the play, how it will turne away fide-wife: for that on that part of the Bowle which is heavier upon the one fide than on the orher, it never will goe truly right, if artificially it bee not corrected; which will hazard the game to thofe which know it not: but if it bee knowne that the leady fide in rowling, be alwayes under or above, it may goc indifferently right; if otherwife, the weight will carry it alwayes fider wife.

Prob-

## Mathematical Recreation.

Problem, XVIII.
To part an e Apple into 2.4 or 8 like parts, without breaking the Rind.

Paffe an needle and three under the Rind of the espples and then round it with diver fe turnings, until you come to the place where you began : then draw oat the three gently, and part the Apple into as many parts as you think convenient: and fo the parts may bee taken Le, and out between the parting of the Rind, and the make rind remaining always whole. sit be e, that ty to wife: beattn c not ole that

## Problem. XIX.

To finde a number thought upon without asking of any queftions, certain operatrons being done.

BTd him adds to the number thought (as ad* mit 15) halle of it, if it may bee, if not the greateft halfe that exceede the other but by an unite, which is 8; and it makes 23: Secondly, unto this 23. adde the halle of ir if it may bee, if not the greateft halle wit. $\mathbf{1 2}$. makes 39 . it the meanie time; note that if the number thought upon cannot be halfed at the first time as here it cannot: then for it keeps 3. in the memory, if at the fecond time it will not be both times it could not be equally halved, them may you together referve five in memory: thind done, caule him from the laft fumme, viz, 35 . fubtrat the double of the number thought, yiz, 30. reft 5 . will him to take the halfe of that if he can, if nor, reject 1. and then take the halfo of the reft: which keepe in your memory then will him to take the halfe againe if he can if not take one from it, which relerve in your memory, and fo perpetually halveing untill 1 , remaine: for then marke how many halfesthere were taken, for the firft halfe account 2 , for the fecond 4 , for the third 8, \&c. and adde uno thofe numbers the ones which you refervedin memory, fo there being 5 remaining in this propofition, there were 2 halfengs: for whith Lait I account 4 , but becanfe it could not exatly be halved without rejecting of I: 1 adde the 1 therefore to this 4, makes 5, which halfe or fumme alwayes multiplyed by 4 , makes $20:$ from which fubtract the firft 3 and 2 , becaule the balfe could not bee formerly added, leates 15 , the number thought upon.

Matbematicall Recreation.

## Other examples.

The halfe of it
For which account and 1 putto it becaufe the could not bee halfed, makes this multiplied by 4 makes 12

The number thought 79 The greateithalfe $40 \quad 3$ The fumme II 9

The greateft halfe of which is

| The fumme of it is | 179 |
| :--- | :--- | The double of 79 is ${ }^{2} 58$

Which taken from it, refts 25 The lefter half 10. wech halve: The halfe of this is 5 which makes
The half of this is $2 \mathrm{w}^{c h}$ is 10 The half of this is I , with 10 and 11 is $2 I^{\circ}$
this 21 which is the double of the lart halfe with the remainder being multiplied by 4 makes 84 , from which take the aforefaid 3 and 2 ,reft 79; the number thought upon.

## PROBZEM. XX.

How to make an uniforme ${ }_{3}$ on an irflexible bodys to paffe through two fmall holes of divers formes, as one being circular, ef the other fquare, Quadrangular, and Triangularwife, yet fo that the boles Ball be exactly filled.
$T$ His Probleme is extraated from Geomiteris call obfervations, and feemes at the fitt tracted in this nature, will appeare more diffi. calt aind admirable. Now in all Geometricat praftices, the leffer or eafier Problemes doe alwayes make way to facilitate the greater: and the aforefaid Probleme is thus refolved. Take a Cone or round Pyramedie, and make a Cerchlar bole in fome boord, or orher hard materiall, which may becequall to the bates of the Cone, and alfo a Triangular bole, one of whafe fides may be equall ro the Diamizer of the circte, and the other two fides equall to the length of the Cone: Now it is moft evident that this Conicall or Tyramidath body, will fill up the Circular bole, and being placed fide-wife
 will fill up the Triangular bole: moreover if you caufe a body to be turned, which may be like to two Pyramides conjoyned, then if a Circular bole bee made, whole Diamiter is eguall to the diamint of the Cones conjoyned, and a Guadrangular hole, whofe nlopeing fides bee equall to the length of each fide of the Pyramidie, and the bredth of the hole equall to the dianssiter of the Circle, this conjoyned Pyramidie fhall exailly fill both the circular bole, and allo 2 uadrande bole.

## Mashematicall Recreation.

Probleme, XXI.

How with one uniforme body or fuch like to fill sbree feverall boles: of which the one is round, the other a juft fquare; and the third an ovall forme.

THis propofition feemes more fubtill than the former, yet it may bee practifed two wayes: for the firth, take a Cilindricall body as great or little as you pleafe: Now it is evident that it will fill a (irceular bole, which is made equall to the bafis of it: if it bee placed downe right, and will alfo filla long fquarc: whofe fides are equall unto the DiAmiter and lengeth of the Cylinder, and according to Pergem, A Archimedes, \&\&c. in their Cylindricall demonfrations, a true Ovall is made when a Cylinder is cut llopewife, therefore if the Oval have bredel equall unto the Diami ter of the $\mathcal{B}$ afis of the Cylinder, \& any length
 wharfoever : the Cylinder being put into his owne ovall bole fhall alfo exactly fill it.
The fecond way is thus, make a Circular hole in fome board, and alio a fquare hole, the fide of which Square may bee equall to the Diamiter

$$
D_{3}
$$

of the Circle: and lafly make a hole Ovall wife whofe bredth may be equall unto the diagonall of the Square; then let a Cylindricall body bee made, whofe Bafis may be equall unto the ${ }^{\text {ith }}$ cle, and the length equall alfo to the fame: Now being placed downe right fhall fall in ths Circle, and flat-wile will fit the Square hole, and being placed floping-wife will fill the 0 . vall.

## K2uccuricidurine

## EXAMINATION.

YOn way note upon the laft two Problenes fartiser, that if a Cone bee cut Eclipticke wife, it may paffe through an Iffocele Triangle through many Scalen 'Triangles, and through an Ellipfis;and if there be a Cone cnt fcalen wife, it will paffe through all the former, onely for the Ellipfisplace a Circlesand further if a follid Co lume be cut Eclipticke-wife it may fill a Circle, *Square, divers Parallelogrames, and divers Ellipris, which bave different Diamiters.

# Mathematicall Recreation. 

## Probiem XXII.

o the Io finde a number thought upon after another the fi manner, than that which is formeriy delivered. fall in:

BId him that he multiply the number thought upon, by what number he pleafeth, then bid him divide that product by any other number, and then multiply that 2 uotient by fome other number; and that product againc divide by fome other, and fo as often as he will: and here nore that he declare or tell you by what number he did multiply and devide. Now in the fame time take a number at pleafure, and fecietly maultiply and divide as often as he did: then bid him devidecthe laft number by that which hee thought upon. In like manner doe yours privately, then will the Quotiegt of your devifor. be the fame with his, a thing which feemes admirable to thafe which are ignorant of the caufe. Now to have the number thought upon withour feemeing to know the laft Quosient, bid him adde the number thought upon to it, and aske him how much it makes: chen fubtra:t your 2 uotient from it, there will remaine the number thought upon. For example, fuppofe the number thoughrupon were 5, multiply it by 4 makes 20 : this divided by 2 , the 2 uotient makes 10 , which rumtipiped by 6 makes 60 , and divided by 4 makes 15 : in the fame time admit you thinke upon 4 , which multiplyed by 4 makes 16 , this divided by 2 makes 8 , which

## Mathomasicall Recreation:

 multiplyed by 6 makes 48 , and divided by 4 makes 12 ; then divide 15 by the number thought which was 5 , the 2 notient is 3 ; din vide alfo 12 by the number you tooke, viz. 4 , the 2 uotient is alfo 3 as was declared, therefort if the 2 notient 3 bee added unto the number thought $v i z 5$, it makes 8,4 hich being known the number thoiight upon is alfo knowne.
## Problem. XXIII.

To finde out many numbers that fundry per. fons, ar one nsan bath thought upon.

1F the multitude of numbers thought upon be cdde, as three numbers, five numbers, ifaven 3 c as for examplelet 5 numbers thought upon be thefe, $2,3,4,5,6$. Bid him declare the fum of the firft and fecond, which will be 5 ; the fecond and third which makes 7, the third and fourth which makes 9 , the fourth and fifth which makes II, and fo alwayes adding the two next together; aske him how much the firf and laft makes together, which is $8:$ then take thefe fummes and place them in order, and adde all thefe together which were in the odde places: that is the firf, third, and fifth, viz, 5 : 9, 8 , makes 22. In like manner adde all thefe numbers together which are in the even places, that is in the fecond and fourth places, viz. 7 and 11 makes 18 , fubtras this frow the former 22 , then there will remaine the double of the firlt

## Mathematicall Recrention:

firf number thought upon, wiz. 4, which knowne the reft is eafily knowne: feeing you know the fumme of the firtt and fecond; but if the multitude of numbers bee even as thefe fixe numbers, viz. $2,3,4,5,6,7$, caufe the partic to declare the fumme of each two, by antecedent and confequent, and alfo the fumme of the fecond and latt which will bee $5,7,9,11,13$, 10, then adde the odde places tugether, except the firf that is 9 , and 13 , makes 22 ; adde alfo the ewen places together, that is $7,11,10$, which makes 28 ; fubtract the one from the other, there fhall remaine the double of the fecond $n$ wabher thought upon, which knowne all thereft are knowae.

## Prosemm. XXIIII.

> How is it that a man in one and the fame timee, may have bis head spward, , and bis fert upward, being in one and the fame place.

THe anfwere is very facill, for to bee fo he mult be fuppofed to be in the center of the earth: for as the heavens is above on every fide, Calum undique fur/um, all that which lookes to the heavens being diftant from the center is upward; and it is in this fenfe that Maurolyeus in his Cofmograpbie, and firt dialogue, reported of one that thought hee was led by one of the ©Muses to hell, where hee faw Lwcifer fitting

## Mathematicall Recreation.

in the middle of the worid, and in the center of the earth as in a Throne; having his kead and feete upward.

## Problem. XXV.

Of a Ladder by which two men afeerding at one time; the more they afcend the more they foall be afunder, notwithfranding one being as high as a-
notber.

THis is moft evident, that if there were a Ladder halfe on this Gide of the Center of the earth, and the other halfe on the other fide: and that two at the Cexter of the world at one inftant, being to afcend the one towards us, and the other towards our Antipodes, they fhould in afcending goe farther and farther, one from - another; notwithflanding both of them being of like height.

## probiem. XXVI.

How it is shat a man having but a Rode or Pole of land, dethbragge that be nzay in a right line paffe from place to place above 3000 miles.

IHe opening of this is eafie, forafmuch as he that pofleffeth a Rode of ground pofferfeth

## Mathematicall Recreation:

Ceth not onlythe exterior furface of the earth, but is matter alfo of that which extends even to the senter of the earth, and in this wife all beritages and pofeflions are as fo many Pyramides; whofe fummets or points mecte in the center of the earth, and the bafss of them are nothing elfe but sach mans pofoffion, field, or vifible quantitie; and therefore if there were made or imagined fo to be made, a defcent to goe to the battome of the heritage, which would reach to the center of the earth; it would bee above 3000 miles in a right line as before.

## Problem. XXVII.

! How it is that a mas flasding upright, and looking which way be wit, be looketh true North or Sosth.

$T$His happeneth that if the partic be under either of the Poles, for if he be under the North pole, then looking any way hee looketh South, becaufe all the Meridians concurre in the $\mathcal{P}$ oles of the werld, ayd if he be under the Soutb pole, hee lookes difectly North by the fame reafon.

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## Matbematicallizecreation.

probiem. XXVIIt.

To tell any one what number remaines after cortaine operations being ended, withowt asking any grefion.

BId him to thinke upon a number, and will him to multiply it by what number you thinke converient : and to the product bid him adde what number you pleafe, provided that fecretly you confider, that it may be divided by that which multiplied, and then let him divide the fum by the number which he firft multiplied by, and fubrract from this 2uot iens the number thought upon: In the fame time divide apart the number which was added by that which multiplied, fo then your 2notient fhall bee equall to his remainder, wherefore without asking him any thing, you fhall tell him what did remaine, which will feeme ftrange to him that knoweth not the caufe: for example, fuppofe he thought 7 , which multiplied by 5 makes 35 , to which adde 10 , makes 45 , which divided by 5 yeeldes 9 ; from which if you take away one the number thought, (becaufe the Maltiplier divided by the divifor gives the 2 notient 1 ,) the ref will be 2 , which will be alfo proved, if 10 the number which was added, were divided by $5, v i z, 2$.

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## Mathematicall Recreation.

$$
\begin{aligned}
& \text { PROB LEM. XXIX. } \\
& \text { Of the play with two feverall thing. }
\end{aligned}
$$

I$T$ is a pleafure to fee and confider how the fcience of sumbers doth furnifh us, not onely with fports, to recreate the firits, but alfo bring us to the knowledge of admirable things, as thall in fome meafure bee fhewen in this enfuing progreffion. In the meane timeto produce alwaies fome of them : fuppole that a man hold divers things in his hand, as Gould and Silver, and in one band he heid the Gould, and in the other hand hee held the Silver: to know fubtilly, and by way of divination, or artificially in which hand the Gold or Silver si; attribute to the gould, or fuppofe it have a certaine prife, \& folikewife attribute to the Silver another price, conditionally that the one be od and the other even: as for example, bid him that the Gould be valued at 4. Crownes, or Billingr, and the Silver at 3.Crownes or 3. Shilings or any other number fo that one be odde, and the other evenas before: then bid him triple that which is in the right hand, and double that which is in the left hand, and bid him adde thefe two products together, and aske him if it be even or odde, if it be even then the Gould is in the right hand, if oddethe Gould is in the lefc hands

Pros:

## Matkamaticall Rccreationo

## Problem. XXX.

Two unmbers being propofod unto two foitco rall parties, to tell which of thefe num. bers is taken by each of them.

AS for example : admit you had propofed untotwo men whofe names were Peter, and Iohn, two numbers, or peeces of moneys the one even, and the other odde, as 10 and or and let the one of them take one of the numbers, and the other partie take the other number, which they place privatly to themfelves: how artificially yaccording to the congruitie, and excelleacy of numbers, to finde which of them did take re.and which 9 . without asking any queition: and this feemes molt fubtill, yer delivered howfoever differing little from the former, and is thus performed: Take privately to your felfe alfo two numbers, the one even and the other odde, as 4 .and 3 . then bid Peter that the double the number which he tooke, and doe you privately double alfo your greateft number; thea bid Iobn to triple the nuwber which hehath, and doe you the like upon your laft number: adde your two products together, and marke if it be even or odde, then bid thetwo parties put their nambers together, and bid them take the halfe of it, which if they cano not doe, then inamediatly tell Peter hee tooke Io.and Iobs 9 . becaufe the aggregate of the double of 4 . and the triple of 3 . makes odde,

## Naincmaticall Recreatien.

 the double of Peters number and Tobirs nsmber. if Peter had taken ro. if otherwife, then they might have taken halfe, and fo Iobn fhould have taken ro, snd Peter 9 . as fuppofe Peter had taken ro.the double is 30 , and the triple of 9. the other number is 27 . which put together makes 47.0 dde : is like manner the double of your number conceived in minde, viz. 4 . makes 8.and the triple of the 3 . the other number, makes 9 . which fet together makes 17 iodde : Now you cannot take the balfe of 17 . nor 47 . which argueth that Peter had the greater number, for otherwife the double of 9 is 18 .and the triple of 10. is 30 . which fet together makes 48.the halfe of it may be taken : therefore in fuch cafe Peter tooke the leffe number: and Ioba the greater, and this being done cleanly carries much grace with it.> Problem. XXXI.

How to defcribe a Circle that Ball towch $3^{\circ}$ Points placed howfoever upon a plaine, if they be not in a right line.

LEt the three points bee eA. B.C. put one foot of the Compaffe uport A. and defcribe an Arch of a Circle at pleafure: and placed at $B$.croffe that $A r k e$ in the two points $E$.and F. and placed in C.croffe the e Arke in G. and $H$. then lay a ruler upon $O, H$ and draw a line, and

## Mathematicall Recreation.

place a Ruler upon $E$. and $F$. cut the otker lipe in $K, f o K$. is the Center of the Cireumference of a Circle, which will paffe by the faid three points A. B.C. or it may bee inverted having a Cirsle drawne, to finde the Center of that Circle. Make 3.points in the circumforence, and thenule the fame way: fo fhall you have the Center a thing moft facill, to every practitioner in the pinciples of Geometrie.

## P\&OBIEM. XXXII.

How to change a Circle into a fguar forme.

N Ake a Circle upon paltboard or other. ters and difpole them $f 0$, that $A$. at the center of the Circle may alwaies be at the Angle of the $/ q$ ware and fo the foure quarters of the circle

## Mathematicall Recreation:

Circle being placed fo, it will make a perfect fquare, whofe fide $A . A$. is equall to the diamiter $B . D$. Now here is to bee noted that the 厅quare is greater than the Circle by the vacuty in the middle, viz, $M$.

## PROBLEM. XXXIIL.

thith one aind the fame compaffes, and at one and the fame extent, or opersing, bo wo to de firibe. many Circles concentricall, that us, $_{3}$ greater or leffer ane tham another.

T T isnot without caufe that many admire how this propofition is to bee refolved; yea in the judgement of fome it is thought inpoffible : who confider net the induftrie of an ingenious Geometritian, who makes it polfible, and that moft facill, fundry wayes; for in the firft the place if you make a Circle upon a fine plaine, and upon the Center of that Circle, a fmall pegge of wood be placed, to bee raifed up and put downe at pleafure by helpe of a fmall hole made in the Center, then with the fame opening ofthe Compaffes, you may defcribe Cir-
cles
eles Concentricall : that is, one greater or leffer thin another: for the higher the Center is lifted up, the leffer the cirele will be. Secondly, the compaffe being at that ex . tent upon a Gibus body, a Circle may bee defcribed, which will beleffe than the former, upon a plaine, and more artificially upos a Globe, or round bomole: and this againe is moth obvious upon a round Pyramide, placing the Compaffes upon the rop of it which will be fart lefe than any of the former ; and this is demor ftrated by the 20:Pro. of the firt of Ewclids, for the Diamiter $\mathcal{E} . D$ is leffe than the line iA D.eAE. taken rogether, and the lines $A D$, AE. being equall to the $\mathcal{D}_{\text {inmiter }} \mathcal{B}$ C.becaule of the fame diftance or extent of opening the Compafes, it followes that the Diamiter ED. and all his Circles together is much leffe than the Diamiter, and the Circle B C. which wasto be performed.

# Matbematicall Recreations 

рroblem. XXXIIII。

> Any nambers under 10.6 eing thought upos; ro finde what numbers they were.

LEt the firft thember be doubled, and unto is adde 5 . and moultiplyed that fumme by 5 -and unto it adde 10 . and the next nimber thonghic upon; multiplye this fame againe by 10 . and adde unto it the next number, and fo proceede : now if he declare the latt fumme; marke if he theught but upon one figure, for then fubtract onely 35 -fromit, and the firft figure in the place of tens is the number thought upon: if he thought upon two figures, then fubtract 35 allo, and the 2 allo the faid 35 . from his laft fumme, and the two figures which remaines are the number thought upon : if he thought upor three figures, then fubtract 350 . and then the firt 3. figures are the nismbers thought upon, $\& c$.fo if one thought upon thefe numbers 5.7 . 9, $\sigma$ double the firlt, makes 10 to which adde 5 . makes 15 . this multiplyed by 5 . makes 75.50 which adde 10 , makes 85 . to this adde the next number, viz. 7 -makes 92 . this miltiplyed by 10. makes 920. to which adde the next number, viz. 9.makes 929 . which multiplyed by 10: makes 9290. to which adde 6. makes 9296 . from which fubtract 3500 . refteth 5796 . the foare numbers thought upon. Now becaufe the twd laft figures are like the two nombers thoughe

## Mathematicall Recreation.

upon sto conceale this bid him take the halfe of if, or put firft iz.or any other number to it, and then it will not be fo open.

## Problem. XXXV. <br> Of the Play mith the Ring.

AMonght a company of 9 . or 10 perfons, one of them having a Ring, or fuch like: to finde out in which hand: upon which finger, joynt it is; this will caufe great aftonifhment toignorant fpirits, which, will make them beleeve that he that doth it workes by magicke, or mitchoraft: But in effect it is nothing elfe butan nimble act o: Arithmeticke, founded upon the precedent Probleme: for firt it is fup. pofed that the perfons fand or fit in order that one is firft, the next fecond, \&ec. likewife there muft be imagined that of thefe two hands the one is firf and the other fecond : and alfo of the five fingers the one is firt, the next isfecond, and laftly of the joynts, the one is as 1. the other as 1 . the other is as 2, the other as 3 . \&c.from whence it appeares that in perfor ming this Play there is nothing elfe to be done than to thinke 4.nambers: for example if the forth perfon had the Ring in his left hand: and upon the fift finger and third joynt, and I would divine and finde it out thus: I would proceede as in the 35 . Probleras: in caufing him to double the firft number : that is, the number of per-
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## 'Mashematicall Recreation:

fons, which was 4.and it makes 8. to which ad 5 .makes I 3. chis noultiplyed by 5 .makes 65 .put 10.co it,makes 75 . unto this put 2 . for the numbber belonging to the left band, and fo it makes 77. which multiplyed by 10 makes 770 . to this adde the number of the fingers upon which the Ring is, viz.5. makes $775^{\circ}$. this multiplyed by 10 make6 7750. to which adde the number for the joynt upon which the Ring is viz the third joynt, makes 7753 . to which caufe him to adde 14. or fome other number, to conceale it the better: and it makes 7767 . which being declaredunto you, fubtract 3514 and there will remaine $4 \cdot 2 \cdot 5 \cdot 3$. which tigures in order declares the whole myflery of that which is to bee knowne, 4, fignifieth forth perfon,2. the left band, 5 . the fifth finger, and 3 , the thir joynt of that finger.

## problem. XXXVI.

## The Play of 3 4. or more Dice.

THat which is faid of the two precedent Problemes may be applyed to this of Dice (and many other particular things) to finde what aumber appeare upon each Dice being caft bo fome one, for the points that are uponany fide of a Dice are alwayes leffe than ro.and the points of each fide of a Dice may be taken for a namber thought upon : theretore the Rule will be as the former : As for example, E 3 one

## Mathematicall Recreation:

one having throwne three Dice \& you would declare the sumbers of each one, or how much they make together, bid him donble the points of one of the Dice, to which bid hum adde 9 . then multiply that by 5 . and to it adde 10 . and to the fumme bid him adde the number of the fecond Dice : and multiplie that by 10 .laftiy, to this bid him adde the number of the lalt Dict, and then let him declare the whole number:then if from it you fubtrat- 350 . there will remaine the number of the three Dice throwne.

## problem. XXXVII.

> How to make water in a Glaffe feeme to boyle and parkle.

TAke a glaffe neare full of mater or other liquer; and fetting one hand upon the foote of it, to hould it faft : turne flightly one of the fingers of your other hand upon the brimme, or edge of the Glaffe; having before privatly wet your finger: and fo palfing Coftly on with your finger in preffing alittle: for then firt the Glaffe will begin oo make a noyfe : fecondly the parts of the glaffe willencibly appeare to tremble, with notable rario fication and cosdenfation : thirdly the water will hake,feeme to boyle : fourthly it will caft it felfe out of the Glaffe, and leape our by fmall drops, withgreat aftonifhment to the ftanders by; if they be ignorant of the caure of it, which

## Matbematicall Recreation.

you wa is onely in the Rarifation of the parts of the how hay glafe : occafioned by the motion and preffure ethepoin of the finger.

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## EXAMINATION:

THecaufe of this, is not in the rarifation of the parts of the Claffe, but it is rarber in the guicke locall wotion of the finger, for reafor Bewesh usthat by bow such a Body draweth nearer to a qualitie, the lefle is it fubject or capable of another which is contrary monto it: nom condenfation, and rarifaction are contrary gwalities and in this Probleme there is threcbodies confidered, the glaffe, the water, and the ayre; now it is evident that the Glaffe being the moft folid, and impenitrable Body, is loffe fubjeff, and capable of rarifaction thas the water, the water is le fefubje 昗 than the ayre, and if therebeany: rarifaction, it is rather confidexable in the ayre than in the water, which is infcribed by the Glaffe, and above the water, and ratber in the water than in the Glaffe: the agitation, or the trembling of the parts of the Glalfe to the fence appeares not: for it is a continued body; if in part why then not in the mole ; and that the water turnes in the Glaffe this appeares not; but onely the upper contigrous parts of the water: that at the bottome being lefferubject to this agitatiow, and it is moff certaine that by bow wixch

## Sashematicall Recreation?

quicker the circular motion of the finger upoz the edge of the Glaffe is, by fo much the more foallthe Ayrebeagitated, and fo the water foall receive fome apparant affection more or left from it, according to that motion: weefou from the quickne ffe of winde uppon the Sea, or calme tbereef, that there is a great or leffer agio tation in the water; and for furtber examination, we leave it to the fearch of thefe which are curious.

## PROBLEMA XXXVIII.

of a fine veffell which bolds wine or water, being caft into it at a certaise beight, but being filled bigher, it will rumne out of its owne accord.

IEt there be a reffell A.B.C.D. in the middle of which place a Pipe; whofe ends both above at $E$, and below at the bottome of the vefell as at $F$. are open; let the end $E$. be fomewhat lower than the brimme of the Glaffe: about this Pipe place another Pipe as $H, L$, which mounts a little above $\boldsymbol{E}$, and let it mot diligently be clofed at $H$ 。 that no Aire enter in thereby, and this Pipe at the bottome may have 2 fmall hole to give paflage unto the water: then powse in water or wine, and as long as it mounts not above $E_{2}$ it is fafe; but if you powre in the water fo that it mount above it, farewell all: for it will not ceafe untill it beall gone

Out: the fame may be done indifpofing any crooked Pipe in a vef. fell in the manner of a fancet or funzell, as in the figure $H$ : for fill it under $H$, as pleafure, and all will goe well; but if you fill it unto H. you will fee fine foort, for then all the
 raffell will bee empty incontiuent, and the fubtiltie of this will feeme more admirable, if you conceale the Pipe by a Bird, Serpent, or fuch like, in the middle of the Glaffe. Naw the reafon of this is not difficult to thefe which know the nature of a Cocke or Farcet; for it is a bowed Fipe one end of which is put into the water or liquor, and fucking at the other end untill the Pipe be full, then will it sunne of it felfe; and it is a fine fecret in nature to fee, that if the end of the Pipe which is out of the water be lower than the wrater, it will runne out without ceafing: but if the mouth of the Pipe bee higher than the water or levell with it, it will not rume, although the Pipe which is without be many times bigger than that which is in the poater: for it is the property of water to keepe alwayes exactly levell.

EXAMINA.

## Nashematicall Recreation: <br> 上5x

## EXAMINATION.

HEre is to be noted that if the face of the water without be in one and the fame plain, with that which is withix, though the onttermoff. Pipe bee ten times greater than that which is within: the water naturally will nat runne, bist if the plaise of the water without be any part lower than that which is within, it will freely runse: and bere may be noted further that if the mouth of the Pipe which is full of water, doth but onely touch the fuperficies of the water within, although the ot ther end of the Pipe withont be nuch lower than that within, the water it will not rex at all: which contradicts the firf grownd; bexce we gather that the prsficre or ponderoftite of the water within, is the canfe of ranning iq fome respett.

> Probiem. XXXIX. Of Glaffe very pleafant.

$\$$Ometimes there are Glaffes which are made of a double farhion, as if one Glaffe were within another, fo that they feeme but one, but there is a little face betweene them. Now powre wine or other liquor betweene the two edges

## Mathematicall Recreation:

edges by helpe of a Tünnell, into a little hole left to thisend: fo will there appeare two fine delufions or fallacies; for though there be not a droppe of wise within the hollow of the Glaffe, it will feeme to thefe which behold it that it is an ordinary Glaffe full of wine, and that efpecially to thele whach are fidewife of it; and if any one moove it, it will much confirme ir, becaufa of the motion of the wine: but that which will give moft delight, is that it any one fhall take the Glaffe, and putting it to his mouth thall thinke to drinke the wine; inftead of which hee fhall fuppe the aire: and fo will caufe laughter to thefe that fland by: who being deceived, will hold the Glaffe to the light; and thereby conlidering that the rayes or beames of the light are not reflected to the eye, as they would bee if there were a liquid fubftance in the Glaffe: hence they have an affured proofe to conclude, that the hollow of the Glaffe is totally empty.

> Problem. XL.

> If any one Bould bold in each band, as many peeces of money as in the other, how to. finde bow much there is.

BId him that holdes the meney that hee pot out of one hand into the other what number you thinke convenient: (provided that it may be done, this done, bid him that out of the band that he put the other number into, that he take

## Matbematicalldecreavion:

take out of it as many as remaine in the other hand, and put it into that hand: for then be affured that in the hand which was put the firt taking away: there will be found juf the double of the number taken away at the firf. $E x$. ample, admit there were in each band 12 Shillings or Counters, and that out of the right band you bid him take 7 and put it into the left: and then put into the right hand from the left as many as dothremaine in the right, which is 5 : fo there will bee in the left band 14, which is the double of the number taken out of the right hand, to wit 7 : then by fome of the rules before delivered, itis cafie to finde how much is th the right band, viz. 10 .
Problem, XLI.

CMany Dice being caft, bow artificially to dif cover the number of the points that may arife.

SVppofe any one had caft three Dice fecroxly, bid him that he adde the points that were upmoft together: then putting one of the Dice apart, unto the former fumme adde the points which are under the other twe, then bid him throw thefe two Dice, and marke how many points a paire are upwards, which adde unto the former fumme: then put one of thefe Dice away not changiag the fide, marke the points which

## Matbematicall Recreation.

which are under the other Dice, and adde it to the former fumme: laftly throw that one Dice, and whatfoever appeares upward adde it unto the former fumme; and let the $\mathcal{D i c e}$ remaine thus : this done, comming to the Table, note what points doth appeare upward upon the three $\mathcal{D}$ ice which adde privately together, and untoit adde 21 or 3 times 7: fothis efdditions or fumme fhall be equall to the fumme which the party privately made of all the operations which hee formerly made. As if hee fhould throw three Dice, \& there fhould appeare upward $5,3,2$ othe fum of them is $10: 3$ fetting one of them apate as 5 . unto 10 , adde the points which are under 3 and 2 , which is 4 and 5 ; and it makes 19 : then cafting thefe two Dice fuppofe there fhould appeare 4 and 1 , this added unto 9 makes 24: and fetting one of thefe two Dice aparte as the 4 -unto the former 24 , I adde the number of points which is under the other Dice, viz, under I, that is 6 , which makes 30 . Laft of all I throw that one Dice, and fuppore there did appeare 2 , which I adde to the former $3^{\circ}$, and it makes $3^{2}$ : then leaving the 3 Dice thus, the points which are upward will be thefe, $5,4,2$, unto which adde fecrecty 21 , (as before was faid) fo have you 32 the fame number which he had: and in the fame manser you may praEtice with 4,5,6, or many Dice or other 6odies, obferving onely that you muft adde the points oppofite of the $\mathcal{D}$ ice: for upon which depends the whole demonitration or fecret of the play; for alwayes that which is above and under-

Mathematicall Recreation. neath makes 7 : but if it make another number, then mult you adde as often thas number.

> Problem. XLII。

I'mo mettals as Gold and Silver, or of other kind moighing alike, being privately placed into tro like Boxes, to finde which of them the Gold or Silver is in.

IT is faid that an Emperor was requefted by one of his fervants after he had long timeres mained with him, to affigne him fomereward: to whichafter few dayes the Emperour condefcended, and caufed him to come into his Treafury, where he had prepared two Boxes, one full of Gold, and the other full of Lead, both weighing, and of forme and magnitude alike: and bid him chufe which he would have. Now many thinke that in this Trobleme one nnult be guided onely by fortune in this choife, and it is that which moft makes a man happy in fuch a choife: bat the want of knowledge caufeth them fo to judge which knoweth not otherwife. A Matheniatician accounts it an cafie propofition and will infallibly chufe the cheft of gold, and leave the cheft of Lead, without either breaking, or opening any of the chefts, and not goe by chance and fortune: for if he may bee permitted to weigh thofe chefts firft it the aire, then is the water: it is a thing cleare

## Masbematicall Recreation.

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## Mathematicall Recreation.

it is fuppored that the wooden globes or chefis are of equall weight, forme, and magnitude: and to dilcover in which the gold or lexid is in, take a broade paire of Compaffes and slip one of the coffers or globes fome what from the middie as at $D$; then fixe in the cheft or globe a fmall peece of iron between the feet of the compafes,as $E K$, at the end of which hang a weight $G$ to that the other end may be counterpoyled, and hang in equilibro:se doe the like to the other cheff or globe. Now it that the other cheft or globe being clipfed in like diftant from the end, and hang: ing at the orher end the fame weight $G$. there be found no difference: then clipfe them nearer cowards the middle, that fo the points of the Compaffe may bee againft fome of the mettell which is inclofed: or juft againt the extremitie of the gold as in $D$, and fuppofe it hang thus in equilibriojit is certaine that in the other coffer is the lead; for the points of the Compafles being advanced as much as before, as at $F$. which takes up a part of the lead, (becaufe it occupies a greater place than the gold) therefore that thall helpe the weight $g$ to weigh, and to will not hang in equilibrio except $G$ be placed neare to $F$ : hence we may conclude that there is the lead; and in the other chef or globe there is the sold.

## Mathematicall Recreation.

nagnitue -lead iss ad clipo a the a Cobeafici mpaffer tG 1otir


## EXAMINATION.

 Ih zeeisht they fall rece forily a be ap like place and he weights, they foall mece flarily take ap like place ins archefi the water, ow therefore weigb alfo one as wish as lobebe another: bence there is no poffibilitie to finde the nd ham inequallitie of the mettells rahich are inclofed in G. then thefe Boxes in the water: the intertion of Archimedes was not upon contrary mettells sinclofed in equall Boxes, but confifted of comparing metrels, mettr fimple in the water one with another: therefore the inference is falfe and abfurd.
## Problem: XLIIT,

Tw, Globes of diverfe mettles, (as one gold and the other copper) yet of equall weight being put into a boxe as B. G. to finde is which end the gold or copper is.

THis is difcovered by the changing of the places of the two Boirles or Globes haying the fame counterpoyfe $H$. to bee houng at the other fide as in $\lambda$ and if the Gould which is the leffer Globe were before the neareft to the handle $D$. E. having now changed his place will bee fartheft from the handles $D$. E. as in K. Globes taken together, hhall bee farther feparte from the mide of the handle (under which is the Center of $\mathrm{gra}^{-}+$ vitic of the Box): han it was before, and feeing that the hande is alwayes in the midle of the box, the waight $\mathcal{N}_{\mathrm{c}}$ muft bee augmented, to keepe it in requilibria: and by this way one may know, that if at the fecond time, the counter poife bee too light, it is figne that the Gould is fartheft off the hardle, as at the firft triall it was neare?


## Mathematicall Recreation.?

may fee dies of fundry forts, the violet, the 6 lew. the orion, the faplsir, the jacist, and the emer and colours, as a lively plant placed in a greene foyle: and as a moftrich treafure of nature, it is a high worke of the Sunre who cafteth his rayes or beames as a curious Painter drawes frokes with his penfell, and placeth his colours in an exquifite fituation; and Salomon faith, Eccief. 43 . it is a chicfe and principall worke of God. Notwithftanding there is lefe to induftrie how to reprefent it from above, here below, though not in perfection yet in part, with the fame intermixtare of colours that is above.

Have you not feene how by Cares of a Boate it doth exceeding quickly glide upon the water with a plealant grace? Ariftotle fayes that ic coloureth the water and makes a thoufand atomes, upon which the beames of the Sunne reflecting makes a kinde of coloured Rainebow: or may we not fee in bouses or gardens of pleafure artificiall fountaines, which powre forth their droppie ftreames of water, that being be* tweene the Sunne and the fountaine, there will be prefented as a continuall Rainebow? But not to goe farther, I will hhew you how you may doc it at your doore, by a fine and facill experiment.

Take water in your month, and turne your backe to the Sunne, and your face againft fome obfcure place, then blow out the water which is in your mouth, that it may bee fprinkled in fmall drops and vapours: you Chall lee there F2 atomes

## Mathematicall Recreazon.

 atomes vapours in the beames of the Sumeto turne into a faire $R$ abinebom, but all the griefe is that it lafteth not bur foone is vanifhed.But to have one more ftable and permanent in his colours, take a glafe full of water andex. pofc it to the Swme, fo that the rayes that pafte through Atrike पןpoli a thadowed place, you will have pleafure to fík the fine forme of a Raimebow by this reffexion. Of take Trigomall glafe or Criffall glaffe of diverfe Angles, and looke through it, or let the beames of the Sunne pafic through it, or vith a candle lect the appearances be received upon a fhadowed place:you will have the fame contentment.
Problem. XL.V. - Problem. XL.V.

How that if all the Poroder in the world were ina clofed witbins a bowle of paper or glaffe, and boing fired on all parts, it could not breake ibat bowle.

T
F the bowle and the pow der be uniforme in all
Lhis parts, ehe by that means the powder would preffe and move equally on each fide, in which there is no polfibilitie whereby it ought to begin by one fide more than another. Now it is impolfivle that the bowle fhould bee broken in all his parts: for they are infinite.

Of like finenes or fubtiltie may it be that a bowle of iron falling from a high place upona plaine pavement of thin glafle, it were impol.
$\qquad$

## Mathematicall Recreation.

fible any wife to breake it; if the bowle were perfectly roma, and the Glaffe flat and unforme in all his parts: for the bowle would touch the Glaffe but in one point, which is in the middle of infinite of parts which is about it: neither is there any caufe why it ought mo:c on one fide than on another, feeing that is may nct be done with all his fides togethers it may bee concluded as fpeaking naturally, that fuch a bowle falling upon fuch a glaffe will not break it. But this matter is meere Mstaphyfoall, and all the workemen in the world cannot ever with alltheir induftrie make abomle perfectly round, or a Glaffe uniforme.

## Problem. XLVI.

To finde a number wiblh being divided by 2 there will remaine 1, being divided by 3 , there will remaine I; and fo likewife. being divided 6y 4,5, or 6.there would fill remaine 1: but bcing divided by 7 , there
will remaine
nothing.
N many Authors of Arithmeticke this ProLbleme is thas propofed: A woman carrying eggest to market in abasket, mett aia unruly fellow who broake them; who was by order made to pay for them: and fhe being demanded what number fhe had, thee could not tell: but fhe re-

## Mathematicall Recreation.

membred that counting them by $2, \& 2$; there remained 1: likewire by 3 and 3 , by 4 and 4 , by 5 and 5, by 6 and 6; there fill remained 1; but when the counted them by 7 and 7 , chere remained nothing: Now how may the number of egges be difcovered?

Finde a number which may exactly be mea Sured by 7 , and being meafured by $2,3,4,5$, and 6 ; there will till remaine a unity: multiply thefe numbers together, makes $7 \circ^{2}$, to which adde 1 ; fo have you the number, vix. 7ar: in like manner 301 will be meafured by $2,3,4$, in 6 ; fo that 1 rernaines: but being meafured by nothing will remaine; to which continually adde 220 , and you have other numbers which will doe the lame: hence it is deubtfull what number fhee had, therefore not to faile it mat be knowne whether they did exceed 400, 800, \& 2 . in which it may bee conjectured that it conld not exceed 4 or 5 hundred, feeing a math or monean could not carry 7 or 8 hundredegere; therefore the number was the former 3010 which fhee had in her basket : which being counted by 2 and 2 , there will remaine 1 , by 3 and 3, sc. but counted by 7 and 7 , there will nam

One bada certaine number of crownes, and counting them by 2 and 2 , there reffed 1: counting them by 3 and 3 , thererefted 2:carnting them by 4 and 4, there reffed 3: counting them by 5 and 5 , there refted 4:counting them by 6 and 6 , there reffed 5: but counting them by 7 and 7 , there romained nothing: bow many crownes might bee bave.

$T$His 2uefion bath fome aiffinitie to the precedent, and the refolution is almof in the fame manner: for here there muft be found a number, which multiplied by 7 , and then divided by $2,3,4,5,6$; there may alwayes remaine a number leffe by 1 than the divifor: Now the firft number which arives in this nature is 119 , unto which if 420 be added, makes 539 , which alfo will doe the fame: and fo by adding 420 , you may have other numbers to refolve this propofition.

## probiem, XLVIII.

How many forts of weights in the leaft manner muft there be to weigh all forts of thingsketreene 1 pound and 10 pound, and $f_{0}$ unto 121 , and 364 pound.

T
O weigh things betweene I and 40: take numbers in triple propurtion, fo that their
fumme be equall, or fomewhat greater than 40, as are the numbers I. 3.9.27. I fay that with 4 fuch weights, the firft being of I pound, the fecond being 3 pound, the third being 9 pound, and the fourth being ${ }^{27}$ : any weight betweene I and 40 pound may bee weighed. As admitto weigh 21 pound, put unto the thing that is to be weighed the 9 pound weight, then intheo. ther ballance pat 27 pound and 3 pound which doth counterpoife 21 pound and 9 pound: and if 20 pound were to be meigbed, pur to it in the ballance 9 and r , and in the other ballance put 27 and 3 , and fo of others.

Ia the fame manner take thofes weights, $\mathrm{I}_{2}$ $3,9,27,81$, you may weigh with them betweene I pound, and 121 pound: and taking thofe 6 meigbts, as $5,3,9,27,81,243$, youl may weighe even from I pound unto 364 pound this depeads upon the property of continued proportionalls, the latter of which containing twice all the former.

> PROBLEM. XLIX.

Of a deceitfull ballance which being empty feemes to be juft, becaule it hangs in aquilibrio: notwithfanding puting 12 pousnd in one ballance, and I in the other, it will remaine in aquilibrio.

## Mathematicall Recreation.

the Merchants of purpofe in his time ufed them to deceive the world the futivie or craft of which is thus, that onearme of the ballance is longer than anther, the fame proportion, that one weight is hewvier than another: As if the beame were 23 inches long, and the handle placed fo that 12 inches thould be on one fide of it , and II inches on the other fide: conditionally that the forter end fould be as heavy as the longer, a thing cafie to bee done : then after-
 wards put into the ballance two unequall weights in fuch proportion as the parts of the beame have one unto another, which is I 2 to II; but fo that the greater be placed in the ballance which hangs upon the fhorter part of the beame, and the leffer weight in the other ballance: it is molt certaine that the ballances will hang in aquilibrio, which will feeme moft fincere and juft; though it bee moft deceiffull, abominable, and falle.

The reafon of this is drawne from the experiments of eArchinsedes, who fhewes that two unequall weights will counterpoyfe one another, when there is like proportion betwene the parts of the beame (that the handle feparates) and the fame counterpoife, by how muchit is farther from the Center of the handle, by fo much it feemes heavier; therefore if there bea diverfitic of diflance that the ballances hang from the handle, there muft neceffarily bee an inequallity of weight in thele ballances to make them hang in aquilibrio, and to difcover if there be deceite, change the weight into the other ballance, for as foone as the greater weight is placed in the ballance that hangs on the longer parts of the beame: it will weigh downe the other inftantly.

Problem. L.
To beave or lift up a bettle with a fraw.

$T$Ake a fraw that is not bruifed, bow it that it make an Angle, and put it into the botles: fo that the greatelt end bee in the necke; then the Reede being put in the bowed part will caft fidewife, and make an Angle as in the figure may bee feene; then -may you take the end which is out of the bottle in your hand, and heave up the bottle: and it is

## Mathematicall Recreation.

fo much furer, by how much the Angle is acuter or Charper ; and the end which is bowed approacheth to the other perpendicular parts which comes out of the bottle.

Problem.LI.

How in the middle of a mood or defert, without the fight of the Sunne, Starres, Shaddow or Compaffe, to finde out the North or South, or the foure Cardinall points of the world, Enf, weft, ơc.

T is the opinion of fome, that the mindes are ${ }_{\text {to }}$ be obferved in this: if it be hot, the South is found by the windes that blow that way, but this obfervation is uncertaine and fubject to much error: nature will helpe you in fonie meafure to make it more manifeft than any of the former from a tree, thus: cut a fmall tree off even to the ground, and marke the many circles that is about the fap or pith of the tree, which feeme nearer together in fome part than in 0 ther, which is by reafon of the funnes cmorion about the tres: for that the humiditie of the parts of the tree towards the South by the heas of the Sunne is rarified and caufed to extend: and the Sume not giving fuch heat tnwards the North part of the tree, the fap is leffer rarified but condenfed; by which the circles are nearer together on the North part, than on the South part: therefore if a line bee drawne from the wideft

## Mathematicall Recreatiom.

wideft to the narroweft part of the circles, it fhall fhew the North and South of the world: Another experiment may bee thus, take a fmall needle fuch as women worke with: place it gently downe flatwife upon fill water and it will not finke, (which is againft the generall tenet that iron will not fwimme) which needle will by little and little turne to the North and South points. But ifthe needle bee great and will not fwimme, thrult it through a fmall peece of corke or fome fuch like thing, and then it will doe the fame : for fuch is the propertic of iron when it is placed in aqulibrio, it frives to finde out the Poles of the word, or poines of North and South: in a manner as the magnes doth.

##  EXAMINATION.

HEre is obfervable that the moyfure which aydeth to the grometh of the tree, is dilated and rarified by tho Meridionall heat, and con. trakied by the Septentrionall cold:this rarifaction workes upon the part of the bumour or moyfture that

## Mathcrinaticall Recreation.

that is wore thinne, which doth eafbly diffipate andevaporate: which evaporation carries a part of the falt with it, and becaufe that folidation or condenfation, fo that there is left but a part of the nouribment which the heat bakes up and confumes: fo contrarily on the orbor fide the condenfation and refirictive quality of the moyftre caufetb leffe evaporation and perdition: and fo confequently there remaines more nowrifbment. which makes a greater increase on that fide than on the other fide: for as trees bave their gromth in winter, Gecanfe their powers, and thefe of the earth are 乃ut up: $f 0$ in the foring when their powers are open, and mben tbe fappe and moy fiure is drawne by it, there is not fuclscold on the North fide that it may bee condenfed at once: Bitit cona trarily to the fide which is South, the heate may be fuch, that in little time by continuance, this mo yfture is diffipated greatly:and cold is nothing but that which hardneth and contracteth the moyfure of the tree, and fo converteth it into mood.

## PROBLEM.LII.

Three perfonsbaving taken Connters, Cards, or other things, to finde bow mucheach one hath taken.,

Aufe the third party to take a number
which may be divided by 4 , \& a often as he
takes 1 , let the iecond party take 7 , and the

## Mathematicall Recreation.

firft take 13, then caufe them to put them all rogether and declare the fumme of it: which recretly divide by 3 , and the 2 noticnt isthe double of the sumber which the third perion did take. Or caufe the third to give unto the fecond and firft, as many as each of them hath; then let the fecond give unto the firtt and third, as many as cach of them hath: laftly let the third give unto the fecond and firtt, as many as each of them hath; and then aske how much one of them hath: (for they will have then all alike,) fo halfe of shat number is the number that the third perfon had at the firft: which knowne all is knowne.

- Prorleme Lili.

> How to make a confort of muficke of many parts rith one voyce, or one inftrument onsly.

THis Probleme is refolved, fo that a finger or player upon an inftrument, be neare an Echo which anfwereth his voice or inftrument; and if the $\varepsilon$ cho anfwereth but once at a time, he may make a double; if twice, then a triple; if three times, then an barmonis of foure parts; for it muft be fuch a one that is able to exercife both tune and note as occafion requires. As when he begins ut, before the Echo anfwere, he may begin fol , and pronounce it in the fame tune that the Echo anfwereth, by which meanes you have a fifi, agreeable confort of muficke : then

## Mathematicall Recreation:

in the fame time that the Echo followeth, to found the fecond note fol, hee may found forth another fol higher or lower to make an eight; the moft perfect confort of musicke, and fo of -athers; if he will continue his voyce with che Echo: and fing alone with two parts. Now experience fheweth this to be true, which often comes to paffe in many Cburches; making one to beleeve that there is many noore parts in the muficke of a 2 uier, than in effect truly there is, becaufe of the refounding and multiplying of the voyce, and redoubling of the 2 wire.

## Praelem. LIIII.

To make or deforibe ax O all forme, or that which neare refombles unto it, at one
trorning with a paire of common Compafles.

THere is many fine wayes in Geometricall praflices, to make an Ovall figure or one neare unto it, by feverall centers: any of which I will not touch upon; but fhew how it may be done promptly upon one center only. In which I will fay nothing of the Ovall forme which appeares, when one defcribeth circles with the points of a common compaffes, Comewhat deepe upon a skinne ftretched forth bard: which contracting it felfe in fome parts of the skinne makethan Ovall forme. Bot ic will more evidently appeare upon a colwmme or cylinder: if paper paper afterwards being extended, will not bee circular but ovall-mi $e$ e: and a paire of Compaffes may be foaccommodared that it may be done alfo upon a plain thus. As let the lengeth of the 0 . vall be $H . K$, faften 2 pinnes or nayles neare the end of that line as $F$. $G$, and take a threed - which is double to the length of $G$. $H$, or $F$. $K$ : then if you take a Compafle which may have one foot lower thas another, with a
 fpring betweene his
1 legges: \& placing one foot of this Compaffe in the Center of the Ovall, and guiding the threed by the other foot of :he Compaffes, and fo carrying it about: the foring will helpe to defcribe and draw the Ovall forme. But in ftead of the Compaffes it may be done with ones hand onely $y^{2}$ as in the figure may appeare.

## Problem, LV.

## Of a purfe difficult to be opened.

IT is made to fhut and open with rings: firt at each fide there is a ftrap or Atring, as $A B$

## Nashematicall Recreation.

 and the ftring $C D$ paffeth through the ring $B$, fo that it may not come out againe; or be parted one from another: and fo that the ring $B$; may flide up and downe upon the ftring $C \mathcal{D}$, then over the purfo there is a peece of leather $\varepsilon . F$. G. H. which covers the opening of the puir $C_{5}$ and there is another pesce of leather e1. E. which paffeth through many ringes: which hath a flitte towards the end $I$. fo great that the Atring B. C. may nide inte it: Now all the cunning or craft is how
 to make faft or to open the parre, which confifts in making the fring B.C. Alide through the fide at $I_{\text {; }}$, therefore bring downe $\boldsymbol{B}$. to $I_{3}$ then make the end $I$. paffe through the ring $B$ : and alfo $D$. with his ftring to paffe through the lit $I$, fo thall the purfe be fatt; and then may the frings be put as before: and it will feeme dificult to difcover how it was dose. Now to open the pur $\int e$, put through the end 1 . through the ring $B$, and then through the flit $I_{;}$by which you put through the fring $D C$ : by this way the purge will be opeaed.

## Mathematicall Recreation.

## PROBLEM. LVI.

Whether it is more hard and admirable without Compaffes to makea perfeal circle, or being made to finde out the Center of it,

I$T$ is faid that upon a time paft, two Mathe maticians meete, and they would make tryall of their induftry: the one made inflantly a petfea circle without Compaffes, and the other immediately pointed out the center thereof with the point of a needle? now which is the chiefeft action: it feemes the firf: for to draw the mot noblelt figure upon a plaine Table without other helpe than the hand, and the minde, is full of admiration: to finde the conter is bur to finde out only on point, tut to drawa round, there murt be almoft infinite points, $e$ quidiftant from the center or middle: that in conclufion it is both the circle and the center together. But contrarily it may feeme that to finde the center is more difificult, for what attention, vivacitie, and fubtiltie muft there be inthe fpirit, in the eye, in the hand, which will chufe the true point amongft a thoufand other points? He that makes a circle keepes alwayes the fame diftance, and is guided by a halte diftance to finifh the reft; but he that moft finde the center, mult in the fame time take heed to the parts a. bout it, and choofe one onely point which is equall diftant from an infinite of other points which are in the circumference: which is very

## Mathematicall Recreation.

difficult. Arifotle confirmes this among? his moralls, and leemes to explaine the dificultie which is to be found in the middle of vertue; for it may want a thoufand wayes and be farre feparated from the true center of the end of a right mediocritie of a vertuous aftion: forto doe well it mult touch the middle point which is but one, and there mutt be a true point which refpects the end, and thats but one onely. Now to jadge which is the mof dificults as before is fatd, either to draw the round or to finde the center: the round feemes to be harder than to finde the center, becaufe that in finding of it; it is done at once, and hath anequall diftant from the whole: But as before to draw a round there is a vifible point imagined, about which the circle is to bee drawne. I efteeme that it is as difficult therefore if hot more, to make the circle without a center, as to finde the iniddle or center of that circle.

Problem. LVI.
Ary ore baving tahen 3 Cards, to finde how many points they containe.

$T$His is to bec exercifed upon a full packe of Cards of 52 , then let one choofe any three at pleafure fecretly from your fight : and bid him fecretly account the points in each Card: and will him to take as many Gards as will makeup 15 to each of the points of his Cards; the number of poiats that his three Cards which lie tooke at the firft did containe. As if the 3 Cards were 7,10 , and $4 ;$ now 7 wants of 15,8:take 8 Cards therefore for your firth Card: the 10 wants of 15.5 , take 5 Cards for your fecond Card: lafly 4 wants of 15,11, take is Cards for your third Card, and giving him the reft of the Cards, there will be 25 ; from which take 4, there remaines 31 : the number of the three Cards taken, viz. 7, 10, and 4.

Whofoever would practife this play with 4 , 5,6, or more Cards, and that the whole number of Cards be more or leffe than 52 ; and that the terme be $15,14,12, \& c$. this generall rule enfuing may ferve: multiply the terme by the number of Cards taken as firtt : to the product adde the number of Cards taken, then fubtrat this fumme from the whole number of Cards; the remainder is the namber which mult bee fubtracted from the Cards, which remaines to make up the game: if there remaine nothing after the $\int$ ubffraction, then the number of cards remaining doth juftly fhew the number of points which were in the Cards chofen. If the Jubfraction cannot be made, then fubtrailt the number of Cards from that number, and the remainder added unto the Cards that did remaine, the fumme will be the number of points in the Cards taleen, as if the Cards were $7,10,5,8$, and the terme given were 12 ; fo the firft wants 5 the fecond wants 2 , the third wants 7 , and

## Mashematicall Recreationo.

the fourth wants 4 Cards, which taken, the party gives you the reft of the Cards: then fecretly multiply 12 by 4 , makes 48 ; to which adde 4 the number of Cards taken, makes 52 , from which 52 fhould bee taken, reft nothing: therefore according to the direction of the remainder of the Cards which are 30, is equall to the points of the foure Cards taken, viz. 7,10 , 5,8. Againe let thefe five Cards bee fuppofed to be taken, $8,6,10,3,7$; their differences to If, the termes are $7,9,5,12,8$, which number of Cards taken, there will remaine but 6 Cards: then privatly multiply 15 by 5 , makes 75 , to which adde 5 makes 80 , from this take 52 the number of Cards, reft 28 , to which adde the remainder of Cards, make 34: the fumme with 8 , $6,10,3,7$.

## Probiem. LVII.

Many Cards placed in diverfe rankes, to finde which of thefe Cards any one bath thought.

TAke $I_{5}$ Cards and place them in 3 heapes in rankewife,s in a heape: now fuppofe any one had thought one of there Cards in any one of the heapes, it is eafie to finde which of the Cards it is, and it is done thus: aske him. in which of the beapes it is, which place in the middle of the other two: then throw downe the Cards by I and I into three feverall heapes in ranke-wile, untill all be caft downe; then aske

## Mathemaricell Recreation.

him in which of the rankes his Card is: which heape place in she middle of the other two heapes alwayes; and this doe foure tinees at leaft, fo in putcing the Cards al:ogether, look: upon the Cards, or let their backebee towards you, and throw out the cight Card: for that was the Card thought upon without faile.

## PROBLEM. LVIII.

Many Cards being offered to fundry perfons, $t o$ finde wich of thofe Cardsany one thinketh upon.

ADmit there were 4 perfons, then take 4 Cards and fhew them to the firft: bid him think one of them, \& put thefe 4 away; thentake 4 other Cards and fhew them in like mannerto the fecond perfon, and bid him thinke any one of thefe Cards: and fo doe to the third perion, and fo the fourth, \&cc. Then take the 4 Cards of the firft perfor, and difpofe them in 4 rankes: and upon them the 4 Cards of the fecond per. fon, upon them alfo thefe of the third perfon, ${ }^{2}$ lattly upon them thefe of the fourth perfon: then fhew unto each of thefe parties each of thefe rankes, and aske him if his Card be in it which be thought: for infallibly that which the Inft partie thought upon will bee in the frit ranke, and at the botrome; the Card of thefecond perfon will bee in the fecond ranke: the Card of the thirdehought upon will be inthe

## Mathemaiticall Recreation.

third ranke, and the fourth mans Card will be in the fourth ranke; and fo of others: if there bee more perfons ufe the fame methode. This may be practifed by other things, ranking them by certaine numbers: allotted to peeces of money, or fuch like chings.

## PRostem, LIX

How to make ax informent to belpe hearing, as Gallilens made to belpe the fight.

THinkenot that the Mathematickes(which hath furnifhed us with fuch admirable helpes for feeing) is wanting for that of hearing: its well knowne that long trunkes or pipes makes one heare well farre off, and experience fhewes us that in certaine places of the Arcades in a hollow vault, that a man fpeaking but foftly at one corner thereof, may be audibly underfood at the other end: notwithftanding thefe which are betweene the parties cannot heare him fpeake at all: And it is a generall principle, that pipes doe greatly Kelpe to Atrengthen the activitie of naturall caufes: we lee that fire contracted in a pipe, burnes 4 , or 5 o foot high, which would fcarce heat, being in the open aire: the rupture or violence of water iffiing out of fauntaine, the wes th that water being contracted into a pipe, caufert a viglence in its paflage. The glaffes of Gallivers makes प's

## Matbématicall Recreation.

fee how ufefull pipes or trunkes are to make the light and fpecies more vifible, and proporo tionable to our eye. It is faid that a Prince of Italy hath a faire ball, in which he can with fa. cility heare diftinctly the difcourfes of thefe which walke in the adjacent gardens, whichis by eertaine veffels and pipes that antwere from the garden to the ball.Fitruvius makes mention alfo of fach veffels and pipes, to ftrengthen the voyce and action of Consedians: and in thele times amongit many noble perfonages, the new kinde of trunkes are uled to helpe the hearing, being made of flver, copper, or other refounding materiall; in funnell-wife putting the wideftend to him which fpeaketh, to the end to contrat the voyce, that fo by the pipe applyed to the eare it may be more uniforme and leffe in der. ger to diffipate the voyce, and fo confeguent: ly more fortified.

## Probiem. LX.

:Of a fine lampe which goes not our, though one carry it in ones pocket: or being rouled upon the ground will
fill burne.

1I mutt be obferved that the veffell in which the oyle is put into, have two pinnes on the fides of it one againft another, being indlue ded within a circle: this circle ought to have two other pinnes, to enter into another circlo of

## Mathematicall Recreation.

braffe, or other follid marter: laftly this fecond circle hathtwo pinnes which may hang within fome box to containe the whole lampe, in fuch manner, that there be 6 pinnes in different pofition: Now by the aide of thefe pegges or pinnes, the lampe that is in the middle will bee alwayes well fcituated according to his Center of gravity, though it bee tarned any way: though if you endeavour to turne it upfide downe, it will lie levell: which is pleafant and admirable to behold to thefe which know not the caufe: And it is facill from this to make a place to reft quiet in, though there bee great agitation in the outward parts.
Problem. LXI.

> Axy one having thought a Card amongft noany Cards, bow artificially to difcover it out.
$T^{\text {Akc any number of Cards as } 10,12, \text { \&c.and }}$ open fome 4 or 5 to the parties fight, and bid him thinke one of them, but let him note whether it be the firft, fecond, third, \&ic. then with promptneffe learne whatnumber of $C$ ards
you had in your hands, and take the other pari of the Cards, \&x place the on the sop of thefe you hold in your hand; and having done fo, aske him whether his (ard were the firft, fecond, scc. then before knowing the number of Cards that were at the bottome, account backwards untill you come to it : fo thall you cafily take out the Card that he thought upon.

## Probiem. LXII.

Three mozsen A. B. C. carryed apples so a market to fell, A. had 20, B. 30 , and C. 40 ; they fold as many for a penny, the one as the other: and brought homse one as much money as another, bow could this be.

THe anfwere to the Probleme is cafie, as fuppofe at the beginning of the market: $A$. fold her apples at à penny an apple: and fold but 2.which was
 2 pence, and fo Thee B 3o had 18 left:but $B$ :fold 17. which was $1 \%$ pence, and fo had $\mathrm{I}_{3}$. left: $C$. fold 32 which Was 32 pence, and fo had 8 apples left: then A. faid fles would not: fell her apples fo

## Mathematicall Recreation.

cheape, but would fell them for 3 pence the peecs, which thee did: and fo her apples came to 54 pence, and B.having left but 13 apples fold them at the fame sate which came to 39 pence: and lafly $C$. had but 8 apples, which at the fame rate came to 24 pence: thefe fummes of money which each others before received come to 56 pence, and fo much each one received; and fo confequently brought home one as much as another.

FIrft, any two numbers is juft the fumme of an number that have equall diftance from tbe halfe of that number: the one augmenting, and the other diminifhing, as 7 and 7 , of 8 and 6 , of 9 and 5 , of 10 and 4 , of $I I$ and 3 , of 13 and 2 , of 13 and 1 : as the one is more than the halfe the o her is leffe,

Secondly, it is difficult to finde two numbers whofe fumme and product isalike, (that is) if the numbers be multiplyed one by another, and added together, will be equall: which two numbers are 2 and 2 , for to multiply 2 by 2 makes 4 , and adding 2 unto 2 makes the fame: this property is in no other two whole nambers, but in broken numbers there are infinite, whofe fumme and product will bee equall one to another. As Clavius Chewes upon the 36 Pro , of the $\mathrm{g}^{\text {th }}$ booke of Euclide.

> Thirdlys

## Mathematicallineereation.

Thirdly, the numbers 5 and 6 are called circular numbers, becaufe the circle turnes to the point from whence it begins: fo thefe numbers multiplyed by themfelves, doe end alwayes in 5 and 6 , as 5 times 5 makes 25 , that againe by 5 makes 125; fo 6 times 6 makes 36 , and that by 6 makes $216,8 \mathrm{c}$.

Fourthly, the number 6, is the firft which A. rithmeticians call a perfect number, that is, whofe parts are equall unto it, fo the $\sigma$ part of it is 1 , the third part is 2 , the halfe is 3 , which are all his parts: now 1,2 , and 3 , is equall to 6 . It is wonderfull to conceive that there is fo few of them, and how rare thefe numbers are, fo of perfect men: for betwixt $1 \& 1000000000000$ numbers there is but ten, that is; $6,28,486$. 8128. 120816. 2096128. 33550336. $536854528.8589869056, \& 137438691328:$ with this admirable property, that alternately they end all in 6 and 8,84 the twentieth perfeet number is 151115727451553768931328 .

Fiftly, the number 9 amongt other privio ledges carries with it an excellent property, for take what nuraber you will, eitber in grofle or in part: the nines of the whole or in its parts rejected, and taken fimply will be the fame, as 27 it makes 3 times 9 , fo whether the nines bee rejefted of 27 , or of the fumme of 2 and 7 , it is all one: fo if the nines were taken a way of 240. it is all one, if the nines were taken away of 2,4 , and 0 ; for there would remaine 6 in either: and $f 0$ of others.

Sixtly, II being multiplyed by $2,4,5,6,7$,

## Mashematicall Recreation.

8 , or 9 , will end and begin with like numberrs; fo if multiplyed by 5 makes 5s: if multiplyed by 8 , it makes 88 , $\begin{gathered} \\ \text { c. }\end{gathered}$
Seventhly, the numbers 220 and 284 being unequall, notwithtanding the parts of the one number doth alwayes equallife the other number: fo the alliquot parts of 220 are $110,54,44$, $22,20,11,10,5,4,2,1$, which together makes 284: the alliguot parts of 284 are $14^{2}, 71,4$, $2, \mathrm{r}$, which together makes 220 , a thing rare and admirable, and dififcult to finde in other numbers.
Eightly, the numbers $3,4,5$, (found our by Pythagoras) have an excellent property in making of rectangle Triangles: upon which the 47 Pro: of the firlt booke of Exclide, was grounded, fhat the /quare of the Hypotenufa in any fuch Triangle, is equall to the Jquare of the other two, lides : that is 5 , the Hypotenufe maltiplyed in 5 makes 25 , and 4 multiplyed in makes 16, and
 multiplied in $3_{3}$,makes 9 : but 9 and 16 is equall to 25: or if thele numbers $3,4,5$, bee doubled, viz. 6,8 ,
10: the fquare of 10 is equall to the fquate of 8 and 6, viz. Io times io makes 100, and 8 times 8 makes 64 , and 6 times 6 is 36 ; which

## Mathematicall Recreation.

$3^{6}$ and 64 , put together makes 100 as befores and fo may they be Tripled, 2 madrupled, err.

The ufe of thefe numbers 3,4,5, are manifold, but it may bee applied thus, for the helpe of fuch which plot ont gardens, boufes, encampe horfe or foote, \&sc. Example, take 3 cords: one of 5 yards, another of 4 yards, and another: of 3 yards; or the dosble, triple, decuple, ofe.or all in one line: and make knots at the tearmes of thefe meafures; fo thefe three parts will make a right angled Triangle, as $A$. B. C. and it is calie with this Triangular cord to plot out a gardemplot: a fquare building plot, or other long fquare. As iuppofe there is a figure $E . D . G$. F. to bee plotted: $E$. D. of 60 yardes broad, and D.G. 100 yardes long. Fifft meafure out $E, D, 60$ yardes, and at $E$. and $D$. place two pinnes or pegges; then at E. place the angle of your Triangular cord B, and let the line of the Triangle $A . B$. be in the line $E$. D: which fuppofe at e F: make the cord A.B. faft in $E$. and $A$, then put the other two cords of the Triangle untill they meete, which will be in $C$, and place a pegge at $C$ : take afterwards a long sord, and by the points $E$. and $C$, augment it unto $F .100$ yards from $E$, and at $F$, place a pegge: then at $F_{\text {p }}$ apply your Trianoular

## Mathermaticall Recreation:

cord as you did at $\varepsilon$, and fo may you draw the line $F . G$.as long as E. D, viz. Go yards. Laftly it is cafie to draw the line $G . D$, and fo the rcctanguled figure or long fquare fhall be plotted, whofe bredth is 60 yards, and length 100 yards as was required: and to examine this, mealure $E, G$, then if $F$. D. be as long, the figure is true: otherwife it is defective and may eafily bee amended.

If one bee taken from any Square number which is odde, the /quare of haife of it being added to the firft Square, will make a Sguare number.

The fquare of halfe any even number r. I being added to that even number makes af guare number, and the even number taken from it leaves afquare number.

If odde numbers bee continually added froma the unitie fucceffively, there will bee made all Tguare numbers, and if cubicke numbers bee addid fucceffively from the unitie, there will bee likewife made fquare sumbers.

## Problem. LXV.

Of an excellent lampe which jerves or furwibheth it felfe zuith oyle, and burnes a long times.

ISpeake not here of a common lampe which Cardanns writes upon in his book de fubtilitate, for thats a little veffell in collumne-wife, which

## Mathematicall Recreation:

which is full of oyle, and becaufe there is vurt one litcle hole at the bottome neare the weeke or match; the oyle rumnes not, for feare that there be emptineffe above: when the match is kindled it begins to heat the lampeyand rarifyo ing the oyle it iflueth by this occafion: and $f_{0}$ fends his more airie parts abovetoavoide vao cuitie.

But that which I here deliver is more ingenious, the principall peece of which is a velfell as C.D:which hath neare the bottome a hole, and a fannell or pipe $E$ : \& then a bigger funnell which paffeth through the middle of the vefSell, having an opening at $\mathcal{D}$.neare the $\varepsilon$ top, and another at the bottome as at $E$, neare the veffell under it, fothat the pipe touch it not: the veffell being thus made, fill it with ogle, and opening the hole $C$. the oyle runniag out will ftop the hole at $E$ : or throwing in oyle into the veffell underneath, untill $E$. bee ftopped; then the oyle at $C$. will not runne : becaufe no aire can come into the pipe D. E. Now as the oyle burneth and confumeth inthe veffell $A . B$. the hole at $\varepsilon$, will begin to be open, then immediatly will $C$.begin to runne to fill up $A B$ : and $E$ being ftopped with the oyle, the ofle at $C$. ceafeth to run.

## Sathematicall Recrestion.

It is certaine that fuch a lampe the $A$ thenians nied, which latted a whole yeare without being touched: which was placed before the flatue of Minerva, for they might put a certaine quantitic of oyle in the lampe $C$. $D$, and a match to burne without being confumed: fuch as the naturallifts write of, by which the lampe will furnilh itfelfe and fo continue in burning: and here may be noted that the oyle may be powred in at the top of the vef fell at alitite hole, \& then made faft againe that the aire get not in.

> PROBLEM, LXV.

Of the play at Keyles or nine Pinnes?

YOu will carce beleve that with one bowle and at one blow playing frecly, one may frike downe all the Keyles at once: yet from Mashomaticall principles ic is eafie to bee demonfrated, that if the hand of him that playes was fo well aflured by experience, as reafon induceth one thereto : one might at one blow frike downe all the Keyles, or at leaft 7 or 8 , or fuch a number as one pleafecth.
For they are but 9 in alldifpofed or placed in a perfect /quare, having three every way. Let us fuppofe then that a good player beginning to play at I fomewhat low, thould fo
frike
ftrike it, that it fhould frike down the Keyles 3 and 5, and thele might in their violence Atrike down the Keyles 3,6 , and 9 : and the bowle being in motion may ftrike downe the Keyle 4, and 7; which 4 Keyle may frike the Keyle 8: and fo all the 9 Keyles may beeftriken downe at onces

## Probiem. LXVI. <br> Of Spectracles of pleajurs.

SImple SpeClacles of blew, yeallow, red or greene colour, are proper to recreate the fight, and will prefent the objects diedinlike colour that the Glaffes are, onely thofe of the gresse doe Comewhat degenerate; inftead of thewing a lively colour it will reprefent a pale dead colour, and it is becaufe they are notdyed greene enough, or receive not light enoughfor greene: and colour thefe images that pafice through thefe Glafles unto the bottome of the cye.

## Nathematicall Recreation.

## 

## EXAMINATION.

1$T$ is cerraine that not onely Glaffes dyed greer, but all other Glaffes coloured, yeeldes the appearances of objects jt rong or weake in colour according to the quantity of the dye, more or leffe, as one being vory yellow, another a pale yellows now all colours are not propor to Glaffes to give colour, bence the defelf is not that they want facultie to reccive light, or refift the penetration of the beames, for in the fame Glaftes thofe wobich are moft dyed, gives alwayes the objects more bigh coloured and obfcure, and thofe which are leffe dyed gives them more pale and cleare: and this is dayly made manifoft by the painting of Glaffes which binders more the penetration of the light than dying doth, where all the matter by fire is forced inio the Glafte,leaving it in all parts transparaint.

Spectacles of Cryftall cst mith diverfe Angles dimond-wifo doth make a marvelous multiplicaticn of the apperrances, for looking towards a houfe it becomes as a Towne, a Towne becomes like Citie, amarined man feems as ambole company cauled foly by the diverfity of refractions; for as many plaines as there arc on the oust fide of the Spectacle, fo many times witt the object be multiplyed in the appearance, becaufe of diverfe. images caft into the eye.


## Mathematicall Recreation.

but this of Gallilens gives a man an Eagles eye, or an eye that pearceth the heavens: firf it difco. vereth the fottie and Braddowed opacows bodies that are found abo ut the Sunne, which darkenctlo and dimunifheth the plendor of that beautifull and Binining Luminary: Secondly, it Betwes the new planets that accompany Saturne and Iupiter: thirdly, in V enus is feene the new, full, and quartall increafe; as in the Moone by herfeparation froms the Sunne: forithly, the artificiall fructure of this inffrument belpeth is to foe an innumer able number of ftars, which otherwife are obfcured by reafon of the natur all weakenelfe of our fight, yea the ftarres in via lactea are feene mof afpa= rantly; where there foemes no farres to be, this inftrument natkes apparantly to be feene, and further delivers them to the eye in their true and lively colour, as they are in the beavens: in which the $\beta$ lendor of fowse is as the Sunne in his moff glorions beamty. This Glaffe bath alfo a moft excellent ufe in obferving the body of the Moone in time of Eclipfes, for it argments it manifold, and moft manifeftly Brewes the true forme of the cloudy fubftance in the Sunne; and by it is feeme when the Baddom of the earth begins to eclip $\int$ e the Moone, and when totally bee is over baddazped befides the celeftiell ufes which are made of ibis Glaffe it hath another noble property; it farre exceedert the or dixary perPeetive Glaffes, which are ufod to fee things remote upon the earth, for as this Glaffe reacheth up to the beavens and excelleth them there in bis performance, , on the carth it claimeth pren

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beminency: for the objects which are fartheft remore, and moft obfcure, are feene plainer than thofe which are neere at hand $\sqrt{2}$ corning as it were all fmall and triviall fervices, as leaving them to an inferigur belpe: great ufe maybe made of this Glafte in difoovering of Shippes, Armies, \&c. 2 (ow the apparell or parts of this inftrument or Glafle, is very meane or fimple, which makes it the more adnairable ( Seeing it performes fuch great fervice) baving but a convex Glaffe thickeft in the middle, to unitc and amaffe the rayes, and make the object tbe greater: to augmenting the vifuali Angle, as alfo a pipe or truncke to an maffe the Species, and binder the greatnes of the light which is about it: (to fee well, the object muft be well inlightened, and the eye in oblcuritic;) then there is adjoyned unto it a Glaffe of a Bort fight to diftinguif the rayes, whech the other would make more confufed if alone. As for the proportion of thofe Glaffes to the Trunke thomgh there be certaine rules to make them, yet it is oftex by bazurd that there is made an ex. cellent one, there being fo many difficulties in the adion, therefore many ought to be tryed, feeing that exalt proportion, in Geometricall calculation camnot ferve for diverfory of figbts in the obfervation.

## Prosiema LXVII.

Of the eAdamant or Magnes, and the needles touched therewitb.

VVHo wonld beleeve if he faw not with his oyes, chat a needle offeel beiag once touched with the magnes, turnes not once, not ayeare, but as long as the world lafteth; his end towards the Nor th and Sonth, yea though one remove it, and turne it from his polition, it will come againe to his points of North and South. Who would have ever thought that a brute ftone blacke and ill formed, rouching a ring of iron, thould hang it in the aire: and that ring fuppore 2 fecond, that to fupport a third, and fo unto 10,12 , or more, according to the frength of the magnes; making as it were a chaine without a lime, without fouldering together, or without any orher thing to fupport them onely;but a mof occult and hidden vertie, yet molt evident in this effect: which penitrateth infencibly from the firft to the fecond, from the fecond to the third, ofc.

Is it not a wonder to fee that aneedle touched once will draw other needles; and fo a nayle, the point of a knife, or other peeces of iron. Is it not a pleafure to fee how the magnes will turne file duft, or move needles, or nayles being upona Table, or upon a peece of paper; for as foone as the magnes turnes, or it movesover, it moues alfo: who is icthat would not bee ra- fee a hand of iron, write upon a planke, withous fecing the Megnes which calt feth that motion behinde the planke, of to make an image of iron to rumme up and downe a Twrret:noul infivite of fich inven tions is proper to bo extraced from the ploperties of the wagnes.

What is there in the world that is more capable to caft a deeper aftonifhment in our mindes, than a great maffic fubftance of iron to hang in the aire in the mideft of a building without any thing in the world touching it, only but the aires? And hiftories affure us, that by the aide of a magnes or adamant, placed at the roofe of one of the Turkifs Synagogues in Clieca: the Gpulcher of that infamous Mahomet refts fuf. ponded in the aire; and Plinie in his naturdl! hiforie writes that the Architecter Dinocrates -a Degin to vault the Temple of Arfinot in Alexar dria, with flore of magnes to produce the tike deceit, to hang the fepulcher of that Coddeffelikewife in the aire.

I should paffe the bounds of my counterpoife, if I thould divulge all the fecrets of this fone, and thould expole my felfe to the laughter of the world: if $I$ thould brag to thew other the caule how this appeareth, than in its owne

## Mathematicall Recreation.

zaurall fympathy, for why is it that a magnes Tith one end will caft the ir or away, and attract it with the other; from whence cometh it that all the magnes is not proper to give a true touch to the needle, but onely in the two Poles of the frome: which is knowne by hanging the fone by a threed in the aire untill it be quiet, or placed upon a peece of Corke in a difh of water, or upon fome thinne board, for the Pole of the ftone will then turne towards the Poles of the world, and point out the North and South; and fo flew by which of thefe ends the needle is to betouched.

From whence comes it that there is a variasion in the needle, and pointeth not out truly the North and South of the world, but onely in Some place of the earch.

How is it that the needle made with pegges and inclofed within two Glaffes, fheweth the height of the Pole, being elevated as many degrees as the Pole is above the Horizon.

Whats the caufe that fire and Garlicke takes away the propertie of the magnes: There are many great hidden mifteries in this fone, which have troubled the heads of the molt learned in all ages; and to this time the world remaines ignorant of declaring the true caufe thereof.

Some fayes that by helpe of the CMagnes perfous which are abfent may know each orhers minde, as if one being here at London, and another at Prage in Germany: if each of them had a reedle touched with one magres, then the yertae is fuch that in the fame time that the
needle which is at Prage fhall moove, this that is at London fhall alfo; provided that the parties have like fecret notes or alphabers, and the ob. fervation be at a fet houre of the day or night; and when the one party will declare unto the other, then lee that party move the needte to thefe letters which will declare the matter to the other, and the mooving of the other parties needle fhall open his intention.

The invention is fubtile, but I doubt whether in the world there can be found fo greata ftone, or fuch a Magnes which carries with it fuch vertue: neither is it expedient, for treafons would be then too frequent and open.

## 

EXAMINATION.

THe experimentall difference of rejection, and att raction proceedes not frowo the different nnture of tones, but frows the quality of the iron, and the vertue of the ftone confifteth onely and epecial. ly in bis Poles; mbich being banged in the aire, zurnes one of bis ends alwayes naturally sowards the South, and the otber toreards the North: but if a rod of iron be towched with one of the onds thereef, it hath the like property in turning North and South, as she magnes bath: notwitbfianding the end of the iron rod touched, bath a contrary pofition to that end of the fone that touched it; yet the fame end will attrate it, and the other endreject it: and $f$ o
miver

## Mathemasicall Recreation.

comtr arily this mal eafily be experimented upos two needles toncbed with one or different ftones, though thej have one and the fame poffition; for as you come Wuto she apply one end of the magnes weare wne thè, the North of the owe will abborre the North of the etber, but the North of tbe one wil alwayes approach so the South of ibe arber: and the fame affection is in she flones thenfelves. For the finding of the Poles of the magnes, it maybe done by bolding a fmall needle betmeene your fingers fofily, and $r_{0}$ mooving it from part to part over the frome wntill if be beld perpesdicalar, for that floll be ose of ibe Poles of the ftone mbicb, ow may marke out; in like manner finde out she otber Pole: Now to finde ous which of thofe Poles is North or South, plece a needle being sonched with one of the Poles upon a (mooth covvex body, (as the neyle of ones finger or fuch like,) and marke mbich way the end of the needle that was towebed tmeneth: if to the South, then the point shat toucbed it now the South Pole, \& $x$ c. and it is moft certaine and according to reafon and experience: that if it be fufpended in aquitabrio in the aire, or fupperted upon the water, it will turne contrary to the needle sbat toucheth it; for then the Pole that was marked for the South foato turse to the North, \&ic.

## Mathematicall Recreation! <br> Problem. LXVIII.

## Of the properties of E Eolipiles or bowles to blow the fire.

THefe are concave vefiels of braffe or copper, or other materiall which may indure the fire: having a fmall hole very narrow by which it is filled with water, then placing it to the fire, before it bee hot there is no effect feene; but affoone as the heate doth penitrate it, the water begins to rarifie and iffueth forth with a hideous and marvellous force; it is pleafure to fee how it blowes the fire with great noyfe.

Vitravious in his firft booke of $A$ rchitedure, Cap. 8. approves from thefe In gines, that the winde is no other thing than a quantitic of vapours and exhalations agitated with the aire by rarifaction and condenfation, and wee may draw a confequence from it, to fhew that a little water may ingender a very great quantitie of vapours and aire: for a Glaffe of mater throwne into an - Eolispile will keep blowing neare a hole houre, fending forth his vapoures a thoufand times greater than it is extended.


## Mathematicall Recreation.

Now touching the forme of thefe veffels, they are not made of one like faftion: fome makes them like a bowle, fome like a head painted reprefenting the winde, forne makes them like a peare: as thoughone would put it to roft at the fire, when one would have it to blow, for the tale of ic is hollow, in forme of a frnueth, having at the toppe a very little bole no greater than the head of a pinne.
Some doe accuftome to put within the e Eo. lipile a crooked funsell of many foldings, to the end that the winde that impetuounly rowles to and fro within, may imitate the noyle of thunder.
Others content themfelves with a fimple funsell placed right upward, fomewhat wider at the toppe than elfe where like a Cone, whofe bafis is the mouth of the fusnell: and there may be placed a bowle of iron or braffe, which by the vapoures that are caft ont will caufe it to leape up, and dance over the mouth of the e $\pm$ o. lipile.
Laffly, come apply neare to hole fmall wind. mills, or fuch like, which eafily turne by reafon of the vapours; or by help of two or more bowed funsells, a bowle may be made to turne: thefe Elopilites are of excelient ufe for the melting of mettalls sand fuch like.
Now it is cunning and fubtiltie to fill one of thefe e Eolipiles with water at fo little a hole, and therefore requires the knowledge of a $P$ bilofopber to finde it out : and the way is thus.

Heate the extolipiles being empty, and the
aire which is within it will become extreamaly rarified; then being thus hot throw it into wa* ter, and the aire will begin to bee condenfed: by which meanes it will occupie leffe roome, therefore the water will immediately enter in at the hole to avoide vacuitie: thus you have fome praticall (peculation upoa the exolipile.

Of the Thermometer: or an inffrument if 20 meafure the degrees of beat and sold in the aire.

THis Inffrument is like a Cylizdricall pipe of Glaffe, which hath a littie ball or bowle at the toppe: the finall end of which is placed into a veffell of water below, as by the figure may be feenc.

Then put fome coloured liguor into the Cy . lindricall glaffe, as blew, red, yealsw, greene, or fuch like: fiuch as is not thicke. This being done the ufe may he thus.

Firft, I fay that as the aire inclofed in the Thermometer is rarifyed or condenfed, the zeater will evidently alcend or defcend in the Cylinder: which you may try eafily by carrying the Themometer from a place that is hot untoa place that is cold, or without removing of it; if you foftly apply the palme of the hand upon the balle of the Thermometer: the Glaffe being fo thinme, and the aire fo capable of rarifaction,

## Mathematicall Racrearion.

that at the very inftant you may fee the waier defcend: and your hand being taken away, it will foftly afcend to his former place againe. This is yet more fencible when one keates the ball at the toppe with his breath, as if one would fay a word in his eare to make the water to defcend by conmand: and the reafon of this motion is, that the aire hea. ted in the Thermomee rer, doth rarifie and

$\qquad$ dilate, requiring a
$\qquad$ greater place; herice prefleth the water and cauleth it to defcends contrariwife when the aire cooleth and cond denfeth, it occupieth leffe roome; now nature abhorring vacuity, the water naturally afcendeth. In the fecond place I fay, that by this meanes one may know the degrees of heate and cold, which are in the aire each houre of the day; for afmuch as the exterior aire is either hot or cold, the aire which is inclofed in the Thermometer doth likewife either rarifie or condenfe, and therefore the water afcends or defcends; fo you thall fee that the water in the morning is mounred high, afrerward by litile. and litcle it will defcend to wards noone or midday; and towards evening it will againe afcend: to in wixter it will mount fo high, that all the Cylinder of the Thermometer will bee full, but
in Summer, it will defcend fo low that farce there will be perceaved in it any water atall.
Thefe that will determine this change by numbers and degrees, may draw a line upon the Cylinder of the Thermomater; and divide it iato 4 degrees, according to the ancient $P$ hilofopbers, or into 4 degrees according to the Pbypitians, dividing each of thefe 8 into $S$ others to have in all $\sigma_{4}$ divifons, and by this way they may not onely diftinguifh upon what degree the water afcendeth in the morning, at midday, and at any other houre: but alfo one may know how nuch one day is botter or colder than another: by marking how many degrees the water afcendeth or defcendeth, one may compare the botteft and coldeft dayes in a whole yeare together with thefe of another yeare: againe one may know how much botter one roome is than a. nother, by which alfo one might keepe a cham. ber, a furnis, a foove, \&cc. alwayes in an equalitie of heate, by making the water of the Thermometer reft alwayes upon one and the famedegree: in briefe, one may judge in fome meafure the burning of fevers, and neare unto what ex. tenfion the aire can bee rarified by the greateft heate.

Many make ufe of thefe glaffes to judge of the weather, tor it is obferved that if the water fall in 3 or 4 houres a degree or thereabout, that raine infueth; and the water will ftand at that ftay, untill the weather change: marke the water at your going to bed, for if in the morning it hith defcended raine followeth, but if it bee
mounted higher, it argueth faire weather: fo in very cold weather, if it fall fuddainly, it is frow or fome fleekey weather that will infue.

## Probiem. LXX.

Of the proportion of bumaine bodies of firad: tues, of Colofus or buge images, and of monftrous Giants:

PYthagoras had reafon to fay that man is the meature of all things.
Firft, becaure he is the moft perfect amongft all bodily creatures, and according to the Maxime of Philo fophers, that which is moft perfeas. and the firft in ranke, meafureth all the reft.
Secordly, becaufe in effect the ordimary meafure of a foote, the intch, the cubit, the pace, have taken their names and greatneffe from humaine bodies.

Thirdly, becaufe the fimmetrie and concordancie of the parts is fo admirable, that all workes which are well proportionable, as namely the building of Temples, of Shippes, of Pillars, and fuch like peeces of Architetture, are in fome meafure fathioned and compofed after his proportion. And we know that the Arke of Noab built by the commandement of God, was in length 300 cubits, in bredth 90 fubits, in height or depth 30 cubits, fo that the length containes the bredth 6 times, and 10 times the depth: now a man being meafured tion in length, breadth, and depth.

Filalpandus treating of the Temple of Salo. mon, that chiefetaine of workes was modulated all of good Architecture, and curioully to be obferved in many peeces to keepe the lame propertion as the body to his parts: fo that by the grearneffe of the worke and proportionable fymmetrie, fome dare affure themfelves that by knowledge of one onely part of that building, one might know all the meafures of that goodly ftructure.

Some Architects fay that the foundation of boufes, and bafis of columnes, are as the foote; the top, and roofe as the head; the reft as the body: thofe which have beene fomewhat more curous, have noted that as in bumaine bodies, the parts are uniforme as the nofe, the mouth, \&c. thefe which are double are put on one fide or other, with a perfect equallitie in the famee Ar. chitecture.

In like manner, fome have beene yet more curious than folid; comparing all the ornaments of a Corinth to the parts of the face, as the brow, the eyes, the no $\int$ e, the mouth; the rounding of pillars, to the writhing of haire, the chanells of columnes, to the fouldings of womens robes, \&ec.
Now brilding being a worke of the bett $A$ r. tiff, there is much reafon why man ought to make his imitation from the chiefe worke of nature; which is man.

Hence it is that Vitrrvious in his third book,

## Mathematicall Recreasion:

## Mathematicall Recreation.

the sarfe, the fpace betweene the rofe and the chinne, the length of the eares, the greatneffe of the thumbe, are perfectly equall one to the other.

What would you fay to make an admirable report of the other parts, if I fhould reckon them in their leaft; but in that I defire to be excufed, and will rather extract fome conclufion upoin that which is delivered.

In the firft place knowing the proportion of a mzan, it is eafie to Painters, image-makers, \&c. perfectly to proportionate their worke; and by the fame is made moft evident, that which is related of the images and fatues of Greece, that upon a day diverfe workemen having enterprifed to make the face of a man, being fevered one from anorher in fundry places, all the parts being made and put together, the face was found in a molt lively and true proportion.

Secondly, it is a thing moft cleare that by the helpe of proportion, the body of Hercules was meafured by the knowledge of his foote onely; a Lyon by his claw, the Gyant by his thumbe, and a Man by any parte of his body. For $\{0$ it was that Pythagoras having meafured the length of Hercules foote, by the fteps which was left upon the ground, found out all his height: and fo it was that $P$ hydias having onely the claw of a Lyon, did figure and draw out ail the beaftaccording to his trie type or forme; fo the exquifite Painter Timantus, having painted a Pigme) or Dwarfe, which he meafured with a fadome made with the intch of a Gyant; it was fuffici-

## Mathematicall Recreation.

To be fhort, we may by like methode come cafily to the knowledge of many fine antiquities touching Statres, Coloffes, and monftrous Gyants, onely fuppofing one had found but one onrat ly part of them, as the bead, the band, the foote, or fome bone mentioned in ancient Hiftories.

> of Statues, of Colof fus, or buge images.?
$T$ Itruvins relates in his fecond booke that the Architee Dinecrates was defirous to put out to the world fome notable thing, went to Alexander the great, and propofed unto him a high and fpeciall peece of worke which he had projected: as to figure out the mount Athos in forme of a great Statue, which fhould hold in his right hand a Tome capable toreceive ten thoufand mén: and in his left hand a veffell to receive all the water that floweth from the mountaine, which with an ingine fhould caft into the Sea. This is a precty project, faid Alexander, but becaufe there was not field roome thereabout to nourifh and retaine the Citizens of that place, Alexander was wife not to entertaine the defigne:
Now let it bee required of what greatneffe this Statue might have beene, the Towne in his right hand, and the receiver of water in his lef: hand if it had beene made.
For the Statue, it could not bee higher than the mountaine it felfe, and the mountaine was about a mile in height plume or perpendicular;
therefore the hand of this Stat ue ought tobee the Io ${ }^{\text {th }}$ part of his height, which would bee 500 foote, and fo the bredth of his hand would be 250 foote; the lengch now multiplyed by the bredth, makes an burdred twenty five thoufand Cquare feete; for the quantitie of bis band to make the towne in, to lodge the faid ro thom. fand men, allowing to each man neere about ${ }^{2}$ foote of faperare grownd: now judge the capacitic of the other parts of this Colof $f$ us by thas which is already delivered.

Secondly, Plinie in his 34 booke of his nathe rall Hifory, fpeakes of the famous Colof fus hat: was at $R$ bodes, betweene whofe legges a Shipe might paffe with his failes open or difplayed, the Statue being of 70 cubits high: and othr Hiftories rcports that the Sarazins having broken it, did load 900 Camells with the mettle of it, now what might be the greatnes and weight of this Statue.

For anfwere it is ufually allowed for a a amo mells burthen 1200 pound weight, therfore all the Colofws did, weigh $108 \mathrm{cco0}$ pound weight, which is ten hundred and forecore thoufand pound weight.

Now according to the former rules, the bead being the tenth pait of the body, this Statues bead fhould bee of 7 oubits, that is to fay, 10 foote and a halte; and feeing that the nof, the brow, and the thumbe, are the third part of the face; his nofe was 3 foote and a halfe long, and fo much alfo was his thumbe in length: now the thichneffe being alwayes the third part of

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the length, it fhould feeme that his thumbe was a foote thicke at the leaft.

Tbirdly, the faid Plinie in the fame place reports that Nero did caufe to come out of France into Itally, a brave and bold Statuemaker called Zenodocw, to erect him a Coloffus of braffe, which was made of 120 foot in beight, which Nero caufed to bee painted in the tame height. Now would you know the greatneffe of the members of this Coloffos, the breadth would be 20 foote, his face 12 foote, his thumbe and his sofe 4 foote, according to the proportion before delivered.
Thus I have a faire foeld or fubject to extend my felfe upon, but it is upon another occafion that it was undertaken; let us Ipeake therefore a word touching the Gyants, and then paffe away to the matter.

## Of monftrows Gyants.

FOa will hardly beleeve all that which I fay touching this, neither will I beleeve all that which Authors fay upon this fubject: notwithftanding you nor I cannot deny but that long agoe there hath beene men of a moft prodigious greatneffe; for the holy writings witneffe this themfelves in Deut. Chap. 3. that there was a certaine Gyant called Ogge, of the Towne of Rabath, who had a bed ot iron, the length thereof was 9 cmbits, and in bredth 4 cubits.
So in the firt of Kings Chap. 17. there is

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mention made of $\mathcal{G}$ oliab, whofe height was a palme and $\sigma$ cubits, that is more then 9 foote, he was armed from the bead to the foote, and his Curiat onely with the iron of his lance, weighed five thourand and fixe handred ficles, which in our common weight, is more than 233 pound, of 12 ouncesto the pound. Now it is certaine that the ref of his armes taking his Target, Helmet, Brafelets, and other Armour together, did weigh at the leât 5 hundred pound, a thing prodigious; feeing that the ftrongeft man that now is, can hardly beare 200 pound, yet this Gyant carries this as a vefture without paine.
Solinus reporteth in his 5 Chap. of his Hiforie, that during the Grecians warre after a great overflowing of the rivers, there was found upon the fands the carkaffe of a men, whofe length was 33 cubits, (that is 49 foote and a halfe) therefore according to the proportion delivered, his face fhould bee 5 foote in length, a thing prodigious and monfrous.

Plinie in his $y$. booke and 16. Chap. faith, that in the Ile of Crete or Candie, a mountaine being cleaven by an earrthquake, there wasa body flanding upright, which had 46 cubits of height: fome beleeves that it was the body of Orion or Othus, (but I thinke rather it was fome Gbofe or fome delufion,) whofe hand fhould have beene 7 foote, and his nofe two foot and a half long.But that which Plutarch in the life of Sertorius seports of is more frange, who faith that in Timgy a Moratize Towne;

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where it is thought that the Gyant Antheus was buried, Sertorius could not beleeve that which was reported of bis prodigious greatneffe, caufed his fepuicher to bee opened, and found that his body did containe 60 cubits in length, then by proportion hee fhould bee 10 cubits or 15 foote in bredih; 9 foore for the length of his face, 3 foote for bis thumbe, which is neare the capacitic of the Colaffus at Rhodes.

But behold here a fine fable of symphoris Caxpefius, in his booke intituled Hortus Gallicus, who fayes that in the Kingdome of Sicile, at the foote of a mountaine neare Trepane, in opening the foundation of a bouse, they found a Cave in which was laid a Gyant, which held in tead of a ftaffe a grear poft like the maft of a Shippe: and going to handle it, it-mouldered all into afhes except the bones which remained of an exceeding great meafure, that in his head there might be eafily placed 5 quarters of corne, and by proportion it fhould feeme that his length was 20 cubits, or 300 foote: if he had faid that hee bad beene 300 cubits in length, then he might have made us beleeve that Noabs Arke was but great enough for his fepulcher.

Who can beleeve that any man ever had 20 cubits, or 30 foote in length for his face, and a nofe of ro foore long? but it is very certaine that there hath been men of very great flature, as the holy Scriptures before witneffeth, and many Authours worthy of beliefe relateth: 10fepbus Acofta in his finf booke of the Indians Hifory, Chap. 19. a late writer, reportech that

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at Peru was found the bones of a Gyant, which was 3 times greater than thefe of ours are, that $1 \mathrm{~s}, 18$ foote: for it is ufually attributed to the talleft ordinary man in thefe oar times but $\sigma$ foote of length; and Hiftories are full of the defcription of other Gyants of 9,10 , and 12 foote of height, and it hath beene feene in our times fome which have had fuch heights as thefe.

Problem. LXXI.

Of the game at the Palme, at Trappe, at Bombes, Taile.maile and others.

T-He Mathematickes ofeen findeth place in fundry Games to aide and affift the Gamo. fers, though not unknowne unto them? hence by Matbematicall principles, the games at Tennis may be affitted; for all the moving in it is by right lines and reflections. From whence comesit, that from the appearances of flat or convex Glaffes, the production and reflection of the fpecies are explained, is it not by right lines? in the fame proportion one might fufficiently deliver the motion of a balle or bowle by Geometricall lines and Angles.

But the exercife, experience, and dexteritic of the player feemes more in this action than any any other precepts: notwithftanding I will deliver here fome maximes, which being reducad to prattice, and joyned to experience, will

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give a great advantage to thore which would make ufe of them in fuch gamings.

And the firt maxime is thus: When a Bowle toucheth another Bowle, or when a trapficke-ftriketh the Balle, the moving
 of the balle is made in a right line, ; which is drawne from the Center of the Borole by the point of contingencie.

Secondly, in all kinde of fuch motion; when a Balle or Bowle sebounds, be it either againf wood, a wall, upona Drumme, a pavement, or upon a Racker; the incident Augle is alwayes equall to the Angle of reflection.

Now following thefe maximes it is eafie to conclude, firft in what part of the wood or wall, one may make the Bomle or Balle goe to reflect or rebound, to fuch a place as one would: Secondly, how one may caft a Bowle upon another, in fuch fort that the firft or the fecond fhall goe and meete with the third, keeping the reflection or Angle of incidence equall. Thirdly, how one may touch a Bowle so fend it to what part one pleafech: fuch and many other practices may bee done. At the exercifes at Keyles there muft be taken heed that the motion, llacke or diminiGheth by litcle and little, and may Mathematicall Recreation: may bee noted that the Maximes of reflections cannot be exaclly obferved by locall motion, as in the beames of light and of other quallities, whereof it is neceflary to fupply it by induitry or by frength, otherwife one may be fruftrated in that refpect.

> Problem. LXXII.

## Of the Game of fquare formes.

N$V_{m b e r s ~ h a v e ~ a n ~ a d m i r a b l e ~ f e c r e c i e, ~ d i-~}^{\text {dit }}$ verny applyed, as before in part is thewed, and here I will fay fome thing by way of tranfmutation of numbers.

It is reported that at a certaine paffage of a fquare forme, there were 4 gates oppefite one to another, that is, one in the middle of each fide, and that there was appointed 9 men to defendeach front thereof, fome at the gates, and the other at each corner or Angle, fo that each Angle ferved to affit two faces of the 厅quare if neede required: Now chis Square paffage being thus manned to have each fide 9 , it hapned that 4 Souldiers comming by, defired of the Governour of the paffage, that they might bee entertained into fervice, who told them hee could not admit of more then 9 , upon each fide of the Square : then one of the Souldiers being verfed in the eArt of numbers, faid that if he would take them into pay, they would eaGily place themfelves amongft the reft, and yet

## Mathematicall Recreation.

keepe ftill the order of 9 , for each face of the Square to defend the Angles and Gates, to which the Governowrs agreed, \& thefe Souldiers being there fome few weekes li-
 ked not their fervice, but indeavoured to remove themfelves, and fo laboured with fome of the reft; that each of thefe foure Souldiers tooke away bis Cumrade with him, and fo departed: yet left to defend each fide of the pafSage, and how may this be.

Its anfwered thus, in the firft forme the men were as the figure $A$, then each of thefe 4 Souldiers placed themfelves at each Gate, and removing one man fromeach Angle to each Gate, then would they be alfo 9 in each fide according to the figure $\mathcal{B}$. Laftly, thefe 4 Souldiers at the Gates take away each one his Cumrade, and placing two of thefe men which are at each Gate to each'Angle, there will bee ftill 9 for each fide of ths 「guare, according to the figure $C$. In like manner if there were $12 \mathrm{men}^{2}$ how might they be placed about a Square that the firft fide Ghall have 3 every way, then difordered, fo that they might be 4 every way; and laftly being tranfported might make 5 every way, and this is according to the figures, $F$. G. H.

## Mathematicall Recreation.

PROBLEM. LXXIII.

- How to make the fringlof a Viole fencibly Wake, without any one touching it.

THis is a miracle in mizfacke, yet eafie to bee experimented; take a-tiode or orher Inftrament, and choofe two frings, fo that there bee one betweene them; make thefe two frings agree in one and the fame tune: then move the Fiole bow upon the greater ftring, and you fhall fee a wonder: for in the fame time that that Shakes which you play upon, the other will likewife fencibly fhake without any one touching it; and it is more admirable that the foring which is betweene them will not thake at all: and if you put the firt ftring to another tune or note, and loofing the pin of the fring, or ftopping it with your finger in any fret, the other fring will not fhake: and the fame will happen if you take two Violes, and ftrike upon a fring of the one, the flring of the other will fencibly fhake.

Now it may bee demanded how comes this fhaking, is it in the occult fympathie, or is it in the ftrings being wqund up to like notes or tunes, that fo eafily the other may receive the impreffion of the aire, which is agitated or moved by the thaking or the trembling of the 0 ther: and whence is it that the Viole bow moved upon the firft friag, doth inftantly in the fame tim: aqve the third fring and not the feconds

## Mashematicall Recreation.

if the caufe be not either in the firt or fecond: 1 leave to others to difcation.

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## EXAMINATION.

I$N$ this Examination we have fomething elfe to imagine, than the bare fympatbie of the Cords one to another: for fieft there ought to be confidered the different effect that it produceth by extenfion upon one and the fame Cord in capacitic: then wohat might be produsced upon different Cords of length axd bigneffe to make them accord in a unifon or eftavo, or fome confort internsediate: this being naturally examined, it will be facill to lay oper a way to the knowledge of the true and immediate caufc of this noble and admirable Phenomeny. Nom this will fencibly appeare when the Cords are of equall length and greatneffe, and fot to an mifon; but when the Cords differ from their equalitie, it will be lefte Sencible: bence in one and the fame Infrument, Cords at a unifon fall excite or foake more than that which is at an octavo, and more than thofe which are of an intermediate proportionall confort: as for the otber conforts they are not exempted, though the effect be not to fercible, yet more in one than in another: and the experiment will Seeme more admirable intaking two Lutes, Vioies \&c. and in feting them to one ture: for then in couching the Cord of the one, it will and not onelyfo but alfo a barmony.
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## PROBLEM. LXXIIII.

Of a veffell which containes three feverall kindes of liguor, all put in at one bung-bole, and drawne out at one tappe fewerally without mixture.

THe veffell is thas made, it muft be divided into three $\int$ slls for to containe the three $/ i$ : quors, which admis to be Sacke, Clarret, and whitezaine: Now in the bung-bole there is an Ingine with three pipes, each extending to his proper fell, into which there is put a broach or funnell pierfed in three places; in fach fort that placing one of the holes right againt the pipe which anfwereth unto him, the other two pipes are fopped; then when it is full, turne the furs. nell, and then the former hole will be ftopped and another open, to catt in other wine without mixing it with the other.

Now to draw out alfo without mixture, at the bottome of the veffell there muft be placed a pipe or broach which may have three pipes, and a cocke pierfed with three holes fo artificially done, that turning the cocke, the hole which anfwereth to fuch of the pipes that is placed at the bottome, may iffue forth fuch wine as belongeth to that pipe, and turning the Cocke to another pipe, the former bole will bee fopped:

## Mathematicall Eegreation.

and fo there will iffue forth another kinde of wine without any inixtures; but the Cocke may bee fo ordered that there may come out by it two wines together, or all
 three kindes at once: but it feemes beft when that in one vefo feli and at one Cocke, a man may draw feverall kindes of wine, and which he pleafeth to drinke.

## Probiem. LXXV。

Of Burning-glafes.

1N this infuing difcourfe I will thew the invention of Promethens how to fteale fire from Hesven, and bring it downe to the Earth; this is done by a little roand Glaffe, or made of fleele, by which one may light a Candle and anake it flame, kindle Fire-brans to make them burne, melt Lead, Tinme, Gould, and Silver, in litle time: with as great eafe as though it had beene put into a Crnzet over a grear fire.

Have you hot read of Archimedes of Syrachfes, who when he could not come to the Ships of Marcellus, which affeiged that place, to binder and impeach their aproaith, fhee flutg huge
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fones by his Ingines to finke them into the Sea, and transformed himelfe into Iupiter; thundering downe from the highent Towers of the Towne, his thunderbolts of lightning into the Sbippes, caufing a terrible burning, in defpite of $\mathcal{X e p t u n e}$ and his watery region: Zonaras witneffeth that Proclus a brave Mathem atician, burned in the fame manner the! Shippes of Vitalian, which was come to affeige Conffantinople; and dayly experience may let you fee great effects of burnisg, for a Bowle of Cryftall polifhed, or a Glafe thicker in the middie than at the edges, will burne exceedingly; nay a bottle full of water expofed to the Sunnte will barne when the Sunne fhineth hot, and children ufe with a Glaffe to burne Flies which are againft the walles, and their fellowes cloathes.
But this is nothing to the burning of thofe Glaffes which are hollow, namely thefe which are of feele well polifhed, according to a parkbolicall or ovall fection: A fpharicall glafe, or that which is according to the fegment of a $S p h a r e$, burnes very effectually about the fourth part of che Diamiser; notwithttanding the Parabolie and Eclipticke fections have a great effect: by which glafes there is allo diverfe fgures

## Mathematicall Recreation?

figures reprefented furth to theeye.
The caufe of this burning is the uniting of the beames of the Sunne, which heates mightily in the point of concosurfe or inflammation, which is either by tranfimiffion or refection: Now it is pleatant to behold when one breatheth in the point of concourse, or throweth fuall duft there, or forinkles vapours of hot water in that place; by which the pyramsidall point, or point of inflammation is knowne. Now fome Authors promifeth to make Glaffes which thall burne a great diftance off, but yee not feene vulgarly produced, of which if they were made, the Parabolie makes the greatelt effect, and is generally held to bee the invention of eArchimedes or Proclus.
Maginus in the s. Chap. of his Treatife of fphericall Glaffes, thewes how one may ferve himfelfe with a concave glaffe, to light fire in the fhaddow or neare fuch a place where the Sunge thines not, which is by belpe of a flat Glaffe, by which may be made a percuffion of the beames of the Sunne into the concave Glaffe, adding unto it that it fervesto good ufe to put fire to a Mine, provided that the combuftible matter bee well applyed before the concave Glaffe; in which hee fayes true: but becaufe all the effect of the prastice depends upon the placing of the Gla Te and the Paroder which he fpeakes not of: I will deliver here a rule more generall.
How one may place a Burning-glaffe with his combaltible matter infuch fort, that at a con-

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\mathrm{K}_{2}
$$ fhall take fire and burne: Now it is certaine that the poins of inflammation or burning, is changed as the Sume changeth place, and no more nor leffe, then the fhaddow turnes abous the file of a Dyall; therefore have regard to the Suns motion, and his height and place: a Bowle of Cryforl in the fame place thac che toppe of the file is, and the Powder or other combuftible matter under the meridian, or houre of $12,1,2,3,2 x c$ or any other houre, and under the Sunnes arch for that day: now the Sunne comining to the houre of 12 , to $5,2,3$, \&ec. the Sume catting his beames through the Cryfath Bowle, will fire the materiall or combutible thing, which meets in the point of burning: the Tike may be obferved of other Burning-glaffes.

##  <br> EXAMINATION.

1 $T$ is certaime in the firft part of this Probleme that Conicall concave and fphericall Glaffer, of what matter foezer, being placed to receive the beames of the Sume will excite heate, and that heate is fo much the greater, by hom mach it is neere the point of concur $f_{s}$ or inflamation. $B_{n}$ that Archimedes or Proclus did fire or kimrne Shippes with Juch Glaffes, the ancient. Hifories are filent, yea themfelves fay nothing;befistes the great difficultie that doth oppofe it in

## Mathematicall Recreation.

remotereffe, and the matter that the effect is to worke upon: Now by a common Glaffe mee fire things necre at hand, from which it feemes very facill to fuch which are leffe read, to dos it at a farre greater diffances, and fo by relation fome deliver to the world by fuppofition that which never was done in aftion: thiswe fay the rather, not to take away the moft excellent and admirable effect whith are in Burning-glaffes, but to Bees the varsety of antiquity, and truth of Hiftory: and as touching to burne at a great diftance as is faid of fome, it is abfolutely impoffible; and that the Parabolicall and Ovali Glaffes were of Archimedes and Proclus invention, is much anocertaine: for befides the compruition of fuch Glafles, they are more difficult than the ob $b \mathrm{nfc}$ concave ones are, and further, they caft rot a great beate but neere at band; for if it bee caft farre off, the effect is little, and the heate reake: or otherveife fuch Glaffes muft be greatly extchded to contract many beames to amaffe a fufficient quantity of beames in Parabolicall and Conicall Glanes, the point of inflammation ought to concurre in a point, which is very difficult ta bee done in a due proportion: Moreover if the place be farre remote as is fuppofed before, fuch a Glafle cannot be ufed but at a great inclivation of the Sunne, by which the effect of burning is diminiShed, by reafon of the weakeneffe of the Sunnebeames.
And bere may be noted in the laft part of this Probleme, that by reafon of obftacles if one plaix Glaffe be not fufficient; a fecand Glafie may bee

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K_{3} \text { applyed }
$$ it cannot be done, yet by a double reflexion the Sun-beames may be caft into the faid Caverne or Mine; and though the reflected beames in this cafo be weake, yet upon a fit cumbuftible master it mill not faile to dos the effect.

## Problem. LXXVI.

> Containing many pleafant $\mathrm{q}^{2}$ refions by ray of Aritbmeticke.

IWill not infert in this Probleme that which is drawne from the Greeke Epigrams, but propofing the 2neftion immediatly will give the anfivere alto, without flaying to fhew the manner how they are anfwered; in this I will not be tyed to the Greeketearmes, which I account not proper to this place, neither to my purpofe; let thefe reade that will Diophanta Scheubelius upon Euclide and others, and they may be fatisfied.

## Of the exfle and the cMule.

1T happened that the Mule and the $A$ fe upon a day making a voyage, each of them carryed a Barrell full of wirs: : now the lafice Affe felt ber felfe over loaden, comphained and bowed under her burthen; which the Mule fecing, faid unto her being angry, (for it was in the time when beafts fpake) thou great $A f f e$, wherefore com-

## Mathematicall Recreation.

complaineft thou? if I had but onely one meafure of that which thou carrieft, I fhould be loaden twice as much as thou art, and if 1 fhould give a meafure of my loading to thee, yet my burthen would be as much as thine.
Now how many weafures did each of them carry? Anfwere, the Mule did carry 7 meafures, and the Affe 5 meafures: for if the Mule bad one of the meafures of the AJes loading, then the CMule would have 8 meafwes, which is double to 4: and giving one to the $A \int f$ e, each of them would have equall burthens: to wit, 6 menfures a peece.

## Of the number of Souldiers that fought before old Troy.

Homer being arked by Hefiodus how many Grecian Souldiers came againft Troy, who anfwered him thus; the Grecians, faid Homer, made 7 fires or had 7 Kitchins, and before every firc, or in every Kitchin there was so broam ches turning to roft a great quantitie of fefh, and each broach had meate enough to fatisfie 900 men: now judge how many mon there might be. Anfwere, $3^{1} 5000$, that is, three hum. dred and fifteene thoufand men, which is cieare by multiplying 7 by 50 , and the product by 900 makes the faid 315000 .

$$
\text { K } 4
$$

## Of the number of Crowmes that

 two men had.IOhn and Peter had certain number of crownes, lohn faid to Peter, if you give me to of your cxownes, I hall have three times as much as you have: but Peter faid to Iobn if you give me ro of your crownes I faall haves times as much as you have: how much had each of them? Anfwere, Iohn had 15 crownes and 5 fevenths of a crowne, and Peter had 18 cromnes, and 4 fevenths of a crowne. For if you adde 10 of $P c_{\text {. }}$ ters crovenes to thefe of Iobns, then fhould Iobn have 25 cromics and 5 fevenths of a crowne, which is triple to that of Peters, viz. 8, and 4 feventhes: and Iobngiving Io to Peter, Peter fould have then 28 croweres, and 4 feventhes of a crowne, which is 2mintupla, or 5 times as much as $I o b m$ had left, viz. 5 crownes aad 5 feventhes.

In like manner two Gamefters playing together, $A$. and $B$ : after plap $A$. faid to $B$, give me 2 crownes of thy money, and I thall have twice as much as thou haft: and $\mathcal{B}$. faid to $\mathcal{A}$. give me 2 crownes of thy money, and I fhall have 4 times as much as thou haft: now how much had each? Anfwere, A. had 3 and 5 fewenthes, and $B$. had 4 and 6 feventhes.

## Mathematicall Recreation.

## About the boure of the day.

5Ome one asked a Matbematician what a clocke it was, who anfwered that the reft of the day is foure thirds of that which is paft: now judge what a clocke it is. Antwere, if the day were according to the lemes and ancient Romaws, which made it alwayes to bee 12. houres, it was then the s - houre, and one feveath of an houre, fo there remained of the whole day $6 \frac{6}{7}$ that is, 6 houres, and 6 feventhes of an houre. Now if you take the $\frac{1}{3}$ of $5 \frac{x}{7}$ it is $\frac{12}{7}$ or 1 and $\frac{5}{7}$ which multiplyed by 4 makes 6 and $\frac{6}{7}$ which is the remainder of the day as before: but if the day had beene 34 houres, then the houre had beene 10 of the clocke, and two fev enthes of an houre, which is found out by dividing 12 , or 24 by $\frac{7}{3}$.

There might have beene added many curious propofitions in this kinde, but they would bee too dificult for the moft part of pcople: therefore I have omitted them.

## Of Pythagoras Schallers.

Dribagoras being asked what number of Schollers hee had, anfwered, that halfe of them ftudied Matbematickes, the fourth part Pbyfcke, the feventh part Rethoricke, and befides he had 3 zomen: now judge you faith he, how many schollers I have. Anfwere, he had in all 28; the halfe of which is 14, the quarter
of which is 7 , and the feventh part of which is 4 : which 14,7 , and 4 , makes 25 , and the other 3 to make up the 28, were the 3 momen.

## Of the number of Apples given amongft the Graces and the crivufes.

THe threc Graces carrying Apples upon 2 day, the one as znany as the other, meet with the 9 cutrufes, who asked of them fome of their apples; fo each of the Graces gave to each of the cMufes alike, and the diftribution being made, they found shat the Graces and the Mufes had one as many as the other: The queItion is how many apples each Grace had, and how many they gave to each Auffe. To anfwere the quiffisn, joyne the number of Graces and CMufes together which makes I 2 , and fo many apples had cach Grace: Now may you take the double, triple, \&c. of 12 . that is 24 , $36,8 \mathrm{c}$. conditionally, that if each Grace had but 12 , then may there be allotted to each $M u f e$ but one onely; if 24 , then to each 2 apples; if 36 , then to each MuSe 3 apples; and fo the dittribution being made, they have a like number, that is,one as many as the other.

## Of the Teftament or laft will of a dying Father.

A
Dying Father left a thoufand crownes amongft his two children; the one being legittimate, and the other a Baftard, conditionally

## Matbematicall Recreation.

nally that the fifth part which his legitrimate Sonne fhould have, thould exceed by 10 , the fourth part of that which the Baftard fould have: what was each ones part? Anfwere, the legittimate Sonne had 577 crownes, and $\frac{7}{3}$ and the Baftard 422 cromnss and $\frac{2}{3}$ : now the fift part of 577 and 7 ninthes is 115 , and $\frac{5}{9}$ and the fourth part of 422 and $\frac{2}{9}$ is 105 and $\frac{5}{5}$ which is leffe then I is $\frac{5}{9}$ by 10, according to the Will of the Teftator.

## Of the Cuppes of Crefur.

Rafus gave to the Temple of the Gods fixe Cups of Gould, which weighed together 600 Drammes, but each Cup was heavier one than another by one Dramme: how much did each of them therefore weigh? Anfwere, the firft weighed Io2 Drammes and a halfe; the lecond ror Drammes and a halfe; the third 100 Drammes and $\frac{x}{2}$; the fourth 99 and a halfe; the fift 98 and a halfe; and the fixt Cup weighed 79 Drammes and 2 halfe: which together makes 600 Drammes as before.

## Of Cupids eApples.

CUpid complaired to his mother that the ,Mujes had taken away his apples, Clio, (aid he, tooke from me the fift part, Euterpe the twelfth part, Thalia the eight part, Melpomene the twenticth patt, Erates the feventh part, Terpomene the fourth part: Polyhymnia tooke away 30, Vrasia 120, and Calliope 300 : 10 there

Thereare ank infinito of fuch like queftions anowgft the Greeke Epigrammes : but it would be unpleafant to expreffe them all: I will orely adde one more, and fiew agenerall rule for all the regi.

## Of a Mans Age.

AMan was faid to paffe the halfe part of his life in childhood, the fourth part in his youth, the third part in Manhood, and 18. yeares befides in olde age : what might his Age be?the anfwer is, 72 . yeares : which and all others is thus refolved:multiplie $\frac{\pi}{6} \cdot \frac{5}{4} \cdot$ and $\frac{3}{3}$.together, that is, 6 .by 4 ,makes 24 .and that againe by 3 . makes 72.then take thethird part of 72 . which is 24 . the fourth part of it, which is 18 , and the fixth part of it which is 12 .thefe added together make 54. which taken from 72 . refts 18 . this divided by 18. (fpoken in the 2uefion) gives 1 , which multiplyed by the fumme of the parts, viz. 72. makes 72 , the $A n f$ wer as before.

## Of the Lion of Bronze placed upcna Founa taine with bis Epigramme.

OVt of my right eye if I let water paffe,I can fill the Cifterne in 2 . dayes: if I let it paffe out of the left eye, it wil be filled in 3 . dayes, if it paffe out of my fecte the Cifterne will bee 4. dayes a filling; but if I let the water paffe out of my mouth, I can fill the Cifterne then in 6 .

## Mathematicall Recreation.

houres: in what time fhould I fill it, if I powre furth the water at all the palfages at ouce.
The Greekes (the greateft talkers in the world) varioully applie this queffion to divers ftatues, and pipes of Fountaines: and the folution is by the Rule of 3 ,by a generall Rule, or by Algeber.

They have alfo in their eAnthologie many other queftions, but becaufe they are more proper to exercife, than to recreate the $\int \rho_{\text {pirit, }}$ I paffe them over as before with filence.

## Probiem. LXXVII.

> Diversexcellent and admirable experiments upon Glaffes.

THere is nothing in the world fo Beautifull as light: and nothing more recreative to the fight, than Glaffes which reflect: therefore I will now produce fome experiments upon them, not that I will dive into their depth (that were to lay open a mifterious thing) bus that which may delight and recreate the firits: Let us fuppofe therefore thefe priaciples, upon which is built the demonftration of the apparances which is made in all fort of Glaffes.

Firf, that the rayes or beames, which reflectethupona Glafe, maketh the Angle of Incident equall to the Angle of Reflection, by the firt Theo.of the Catoptick. of Euc.
Secondly, that in all piaine Glaffes, the Images are feene in the perpendicular line to the Glaffe Images are feene in the right line which paffeth from the object and through the Center in the Glaffe. Theo. 17 and 18.
And here youreto underftand that there is not meant onely thefe which are fimple Glaffes or Glaffes of freele, but a!l other bodies, which may reprefent the vifible Image of things by reaton of their reflection, as water, marble, mettle, or fuch like. Now take a Glaffe in your hand and make experiment upon that which followcth.

## Experiment upon fat and plaine Glaffes.

FIrft, a man cannot fee any thing in thefe dicular line before it, neither can hee fee an object in thefe Glaffes, if it be not in fuch a place, that makes the Angle of ixcidence equall to the Angle of reflexion: thercfore when a $G^{\text {laffe }}$ Atands upright, that is, perpendicular to the How rizon, you cannot fee that which is above, exthe glaffe be placed downe flat : and to fee that on the right hand, you mult bee on the left hand, \&c.

Secondly, an Image cannot bee feene in a Glaffe, if it be not raifed above the furface of it; or place a Glafle upon a wall, you fhall fee nothing which is upon the plaine of the wall; and place it upon a Table or Horizontall Plaine, you thall fee notaing of chat which is upon the Thirdly,

## Mathematicall Recreation.

Thiraly, in a plaine glafe all that is reene appeares or feemes to finke behinde the $\mathrm{Gla} \mathrm{ff}_{\mathrm{e}}$, as much as the Image is before the Glafle: as before is faid.

Fourthly, as in water a Glaffe lying downe flat, or Horizontall, Towers, Trees, Men, or any height doth appeare, inverfed or upfide downe; and a Glaffe placed upright, the right hand of the Image feemes to bee the left, and the left reemes to be the right.

Fiftly, will you fee in a Cbamber that which $s$ done in the ftreet, without being feene: then a Glafe muft bee difpoled, that the line upon which the Images come on the Glaffe, make the Angle of incidence equall to that Angle of reflexion.
Sixtly, an height (as fuppofe DE.) may be meafured by a plaine Glaffe; as let the Glaffe be $G$. placed downe upon the ground, and let the eye bee at $C$. fo farre removed from the Glaffe, that the eye at C. may fee the toppe of the Tree $E$ : in the Angle or edge of the Glaffe at $A$, but in the line of reflexion $C A_{5}$ then meafure the diftance betweene your foote $B_{s}$ and the point A:andalforhe dittance betweene the Glaffe $A$, and the foote of tht Tree $D_{2}$ viz. $A D$. Now as often as $A B$. is

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 Mathematicall Recreation. found in $A D$, fo often doth the height of the Tree E D. containe the diftance from your eye to the foote, vir. $C B$ : for the Triangles $A, B, C$, and $\mathcal{A}, \mathcal{D}, \varepsilon$, are like $T$ riangles: therefore as $\mathcal{B} \subset A$. to $A D$, fo $C B$, to $E D$, or alternately as BeA. to $B C$, foe $A D$. to $D E$.Seventbly, prefent a Candle upon a plaine Glaffe and looke flauntingly upon it, fo that the Candle and the Glaffe bee neere in a right line, you fhall fee $3.45 . \& \mathrm{c}$ Images; from one and the fane Candle.

Eightly, take two plaine Glafes, and hold them one againft the other, you fhall alternately fee them oftentimes one within the other, yea within themfelves, againe and againe.

Nintbly, if you hold a plaine Glaffe behind your head, sc another before your face, you may fee the hiader part of yourbead, in that Glaffe whick y ou hould before your face.

Tenthly, you may have a fine experiment if you place two Glafes togeather, that they make an acute angle, and fo the leffer the angle is, the more apparances you fhall fee, the onedirect,the other inverfed, the one approaching, and the otherretyring.

Eleventbly, it is wonder and altonifhment to fome, to fee within a claffe an Image without knowing from whence it came, and it may be done many wayes:as place a Glaffe higher than the cye of the behoulder, and right againft it is fome Image; foit refteth not upon the behou': der, but doth calt the Image upwards. Then place another object, fo that it reflect, or cait
the Image downeward to the eye of the fpectator, u ithout perceiving it being hid behind fomething, for then the Glaffe will reprefent a quire contrarything, either than that which is before she Glaffe, or that which is about it.

Tmelthly, if there bee ingraved behind the backfide of a Glaffe, or drawne any Imatge upon it, it will appeare before as an Imege, without any appearance : or portratare to be perceived.

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## EXAMINATION.

THis 12. Article of ingraving an Tmage bebind the Glaffe, will be of no great confes quence, becange the linaments will feeme Soobfoure, but if there were painted fome Image, and then that covered according to the wuall covering of Glaffes behind, and So made up like an ordinary looking Glaffe baving an Image in the nsiddle, in this reppect it would be fufficient pleaSant: and that which mould admaire the Ignorant, and able to exercife the moft fubtilleft , and that principally if the Glaffe bee in an obfoure place, and the light which is given to it be fomewhat farre off.

PLace a Glaffe neare the floare of a Chanaher, Glafe, fo that thefe which are below. may not perceive it, and difpofe a btight Image under Glaffe, and it will caule admoriation to thofo which are below that know not the caufe; The fame may be done by placing the Imarge in a Cbimber adjoyning, and fo make it to be feene upon the fide of the wall.

In thete Cbanell Images which fhew onefide a deaths bead, and another fide a faire face: and righr before fome other thing: it is a thing $e$ vident, that fetting a plaine Glafe fidewile to this Image you fhall fee in it a concrary thing, then that which was prefented before fidewife.
Lafiy, it is a fine fecret to prefentunto a plaine Glafe writing with fnch induftrey, that one may reade it in the Glaffe,\& yet out of the Glaffe there is nothing to be knowne, which will thus happen, if the writing be writ baekward: But that which is more ftrange, to fhew a kind of writing to a plaine Claffe, it fhall appeare another kind of writing both againft fence and forme, as if there were prefented to the $G$ laffo WEL. it would fhew it MEr if it were written thus MIV, and prefented to the Glaffe, it would a appeare thus VIM; for in the firt, it the Glaffly flat then the things are inverfed that are perpendicular to the Glafe eif the Glaffe and the objet be uprigbt, then that on the right hand, is turned to the left, at in the latter.
And here I ccafe to foeake further of there plaine Glaffes, eyther of the Admirable multioplications, or appearances, which is made in a greas rumber of them ; for to conterat the fight
in this particular, one muft have recourfe to the Cabinets of great Perforages who inrich them. lelves with mof beautifuliones.

## Experimentsupon Gibbous, or convex Sphericall Glaffes.

Fthey be in the forme of a Bowle, or part of La grear Globe ot Glaffe, there is fingular contentinent to contemplate on them.
Firf, becaufe they prefent the objects leffe and more gracious, and by how more the Images arefeparated from the Glaffe, by fo much the more they deminifh in Magnitude.
Secondly, they that fhew the Images playting, or foulding, which is very pleafant, efpecially when the Glaffe is placed downe, and behold in it fome Blanching, fecling, of c. The upper part of a Gallerie, the porch of a Hall, $\sigma c_{\text {. }}$. tor they will be reprefented as a great veffell having more belly in the middle then at the two ends; and Foffs , and Ioifs of Timber will feeme as Circles.
Thirdly, that which ravifherh the fpirits, by the eye, and which fhames the beft perfpective Painting that a Pasnter can make, is the beautifull contraction of the Images, that appeare within the fphericitie of thefe finall gleafes, for prefent the Glaffe to the lower end of a Gallarie, or at the Corner of a great Court full of People; or towards a grear ftreet. Church, fortification, an Army of men, to a whole Cittie; all the faire Architecture, and apparances with

## Matbematicall Recreation.

be feene contracted within the circuit of the Glaffe with fuch varietie of Colours, and diftinftions in the leffer parts, that I know not in the world what is more agreeable to the fighs and pleafant to behold, in which you will not have an exact proportion but it will be variable, according to the diftance of the Object from the Glaffe.

> Experimenss upon hollow, or Concave Sphericall glaffes.

1Have heretofore fpoken how they may burne, being made of Claffe, or Mettle, it remaines now that I deliver iome pleafant ufes of them, which they reprefent unto our fight, and fo much the more notable it will be, by how much the greater the Glafe is, and the Globe from whence it is extracted.

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## EXAMINATION.

I$N$ this wee may obferve that a fection of 2,5 . or 4. Inches in diamiter, may be fegments of Spheares of $2.3 .0 r$ 4.foote, nay of fo many fadome.for it is certaine that among $A$ thefe which comprehend a great portion of a leffer \{pheare, and thefe which comprehend a little fegment of a great \{pheare whether they be eqwall or not ix feition, there will happen an evident difference

## Mathematicall Recreation.

in one and the fams experiment, in the number, fituation, quantitie, and figure of the 1 mages of one or many differext objeals.

MAginus in a little Tractat that he had upon there Gifles, wita ferb oll fe that he hath caufed many to bee polifhed for fundry great Lords of Italy, and Germanie, which were fegments of Globes of 2.3 . and 4 . foot diamiter; and I wifh you had fome fuch like to fee the experiments of that which followeth; it is not dificult to have fuch made, or bought bere in Towne, the contentenent herein, would beare with the coft.

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## EXAMINATION.

TOuching Maginus bee bath nothing ayded us to the knowledge of the truth by bis extractout of Vitelius, but left it : expecting it from athers, rather than to be plunged in the fearch of it himselfe, affectivg rather the forging of the matter, and compofition of the Glaffes, than Geometrically to eft ablifh their effects.

FIrf $f$ therefore inConcave Glaffes, the Images are feene fometimes upon the furface of the Glaffes, fometimes as though they were within it and behind it, deeptly funke into it, fometimes they are feene before, and without the Glaffe, fometimes betweene the object and the

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 Matbermaticall Recreation:Glaffe; fometimes in the place of the eye, fometimes farther from the Glafe then the objert is: which comes to paffe by reafon of the divers concourfe of the beames, and change of the place of the Images inthe line of flection.

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## EXAMINATION.

THe relation of the fe apparances palfe currant amongf moft men, but becaufe the curious may not receive prejudice in their experiments, fome thing ought tobee faid thereof to give it more lively tosich, in the true caufes of thefe apparances; in the firft place it is impolfible that the Image can be upon the furface of the Glaffe, and it is a principall point to declare truly in whichplace the Image is feene in the Glaffe : thefe that aresnorelearned in Opicall knomledge affirme the costrary, and nature it felfe gives it a ertaineplace accerding toits pofition; being al. mayes feene in the line of reflection, mhioh Alhazen, Vicellious, and others full of great know. ledoe, have confirmed by their reritings: but in their particular they mere two much occupied by the authority of the Ancients, who were not fuffo ciently circumpect in experience, upon robich the prixciples of this fubjeEt ought to be buiit, and fearched not fully, into the true caufe of the le ap. parances, feeing they leave unto pofterities ma$3 y$ falcaties in their writings, and theere that fols lowed

## Mathematicall Recreation.

lowed then for the moot part fell into the like errors.
As for the Images to bide in the eye, it cangot be but is impertinent and absurd; but it followeth that, by bow much neerer the object approachectla to the Glaffe, by fo much the more the appearances feences to come to the eye: and if the ge be without the point of concourse, and the objet alpo; as long as the object approacheth thereto, the representation of the I mage comet neere the 'ye, but paling the point of concourse it goes back agains: thefe appearances thus approaching doth not a little aftonifh the fe which are ignorant of the cause: they are inverfed, if the eye be without the point of concourfs wail the object bee mishin, but contrarily if the eye be betmeene the pins of concourse and the Gaffe, then the Imagee are direct: and if the eye or the object be in the point of concourse, the Glafie will be entighteed, and the Images confused; and if there were but a Burke of fire in the find point of concoxcfe, all the Glaffe mould deme a burning firebrand, and we dare fay it mould occurre without chance, and in the night be the moot certaine and fubtilef light that can be, if a Candle were plaaced there. And whofoever Shall enter into the Perch of the truth of new experiments in this subject, without doubt bee sill confirme what wee here Reake of: and will fronde new lights with a convexviable position to is bl Glaff, be w rill have reflexion of quantities, of truth, and fine Secrets in nature, yet not knowne, which be may cafily comprehend if he have but as indifferent $\sqrt[f]{\mathrm{L}}$ ht, and may allure nor trouble if; a thing too much abjurd to nature.

And it is as abfolute verity in this fcience, that the eye being once placed is the line of reflexion of any object, and moved in the fame line: the object is feene in one and the fame place insmutable; or if the Image and the cye move in their owne lines, the reprefentation in the Glaffe feemes to inveft it Selfe continually with a different figure.

N
Ow the Image comming thus to the eye, thefe which know not the fecret drawes their $\int$ word when he fees an Image thus to iffue out of the Glaffe, or a Piftoll which fome one hoids behinde: and fome Glafles will fhew a foord wholly drawne out, fe parated from the Glafe, as though it were in the aire: and it is dayly exercifed, that a man may tonch the $I_{0}$ mage of his hand or his face out of the Glaffe, which comes out the farther, by how much the Glaffe is great and the Center remote.

## 

## EXAMINATION.

Now that a pintulle being prefontsed to a Glaffe bebinde a man, and Sbould tome out of the Glaffe and make bim afraid, that ftands before feeming to hoote at hims; this cannot bee,

## Matbematicall Recreation.

for no objert mbatfoever prefented to a concave Glaffe, if it be not neerer to the Glaffe then the ege is, it comes not out to the fight of the party; therefore be weedes not feare that which is faid to be bebisude bis backe, and somes oni of the Glaffe, for if it doth come out, it muft then neceffarily be before his face: /o in a concave Glaffe, who fe Center is farre remote; if a sword, ficke, or fuch like be prefented to the Glaffe, it Ball torally be feene to come forth of the Glaffe, and all the band that bolds it. And bere generally note, that if $n$ Image bee feene to if ise out of the Glaffe to come tovards the face of any one that $\mathcal{F}$ ands by, the objeth Brall be likemife feene to thruft towards that face in the Glaffe, and may eafrily be knowne to all the fiaxders by: So many perfons ftanding before a Glaffe, if one of the company take a sword and mould make it ifne fortb tow ards any other that fands there: let bins chufe his image in the glaffe, and carry the fword right towards it, and the effect will follow. In like manner ones hand being prefented to the Giaffe, as it is thruft towards the Cenrer, fo the reprefentation of it comes towards it: and $\int 0$ the hands will feeme to be united, or to touch one another:

[Rom which may bee concluded, if fuch a Glafe be placed at the feeling or planching of $2 H_{\text {all }}$, fo that the face bee Horizontall and looke downeward; one may fee under it as it were a man hanging by the feete; and if there were many placed to, one could not enter into that place without great feare or fcarcing: for Mathematicall Recreation. one fhould fee many men in the aire as if they were hanging by the feete.

##  <br> EXAMINATION.

TOuching a Glaffe tyed at a feeling or planclaing, that one may fee a man bang by the feere in the aire, and fo many Glaffes, many men may be feene: mithont caution this is very ab. furd, for if the Glaffe or Glaffes bee not fo great that the Center of the pheare upon which it was made, extend not neere to the lead of him that is under it, it will not pleafantly appeare; and though the Glafte fould be of that capacitie that the Center did extend fo farre, yet will not the Images bee feene to them which are from the Claffe, but onely to the e mbich are under it, or neere unto it : and to them it will notably appeare, and it would be moft admirable to bave a Galleric vated ower with fuch Glaffes, which would wonderfully aftonifo any one that enters into it: for all the things in the Gallery would be feene to hang in the aire, and you could not walke without incountering ayrie apparitions.

S
Econdly, in flat or plaine Glaffesithe Image is feene equall ta his object, and to reprefent a whole man, there ought to bea Glaffe as great as the Image is: In convex Glaffes the $I$ mages are feene alwaies leffe, in concave glafes

## Mathematicall Recreation.

they may be feene greater or leffer, but not truly proportionable, by reafon the diverfe reflexions which contracts or inlargeth the Species: when the eye is betweene the Center and the furface of the Glaffe, the Image appeares fometimes very great and deformed, and thofe which have but the appearance of the begiuning of a beard on their chinne, may cheare up themfelves to fee they have a great beard; thefe that feeme to be faire will thruft away the Glaffe with defight, becaufe it will transforme their beautie: thefe that put their hand to the Glaffe will feeme to have the hand of a Gyant, and if one puts his finger to the Glafe it will be feene as a great PYymamide of flefh, inverfed againft his finger.
Thirdly, it is a thing admirable that the eye being approached to the point of concourfe of the Glaff, there will bee feene nothing but an intermixture or confufion: but retyring backe a little from that point, (becaufe the rayes doth there meete,) he thall lee his Image inverled, having his head below and his feet above.

Fourthly, the diverfe appearances caufed by the motion of objects, either retiring or approaching: whether they turne to the right hand or to the left band, whether the Glaffe be hung againft a wall, or whether it bee placed upon a Pavement, as alfo what may be reprefented by the mutuall afpect of concave Glafes, with plaine and convex Glaffes: but I will with filence paffethem over, onely fay fome thing of two rare experiments more as followeth.

## Mathematicallikecreation.

The firf is to reprefent by helpe of the $S_{w r y}$ fuch letters as one would upon the front of a house: fo that one may reade them; Caraginus do. h deliver the way thus. Write the letters faith he fufficiently bigge, but inverled upon the furface of the Glafe with fome kinde of colour, or thefe letters may bee written with $20 a x$; (the eafier to bee taken out againe:) for then placing the Glafe to the Sunne, the letters which are written there will bee reverberated, or reflected upon the wall: hence it was perhapsthat Pytbagoras did promile with this invention to write upon the Meose.

In the fecond place, how a man may fundry wayes helpe himielfe with fuch a $G l a f f e$, with a lighted Torch or Candle, placed in the point of concourfe or inflammation, which is neare the fourth part of the Diamiter: for by this meanes the light of the Candle will be reverberated into the Glaffe, and will be caft backe againe very farre by parrallell lines, making to great a light that one may clecrely fee that which is done farre off, yea in the campe of an Enimic: and thofe which fhall fee the Glaffed farre off, will thinke they fee a Silver Bafin inlighrened, or a fire more refplendant then the Torch. It is this way that there are madecertaine Lanthorses which dazell the eyes of thofe which comes agaiaft them; yet it ferves fingular well to enlighten thofe which carry them, accornpodating a Candle with a little hollow Glaffe, fo that it may fuceffively bee applyed to the point of inflammation.

## Mashematicall Recreation.

In like manner by this reffected light, one may reade farre off, provided that the letters be indifferent grear, as an Epitaph placed high, or in a place oblcure; or the letter of a friend which dares not approach without perill or fufpition.

## 

## EXAMINATION.

THis will not bee farce fencible upon a wall remote from the Glaffe, and 6xt indifferent. by foene spos a wall which is neare the Glaffe, and withall it muft be in obscuritic or foadored: orelfe it will not be feen. To caft light in the night to a place remote, with a Candle placed in the poins of concourfe or inflammation, is one of the moff notableft properties which can be Berwne in a concave Glaffe: for if in the peint of inflammation of a parabolicall fection, a Candle bee placed, the light will bee reflected by parallell lines, as a columne or Cylinder; but in the Sphew ricall fection it is defective in part, the beames bee ing not united in one point, but fomeerbat fcattering: notwithftanding it cafteth a very great beantifnll light.

LAfly, thefe which feare to hurt their fight by the approach of Lampes or Candles, may by this artifice place at fome corner of a Chambersa Lampe with a hollow Glafe behinde
it，which will commodiounly reflect the light upon a Table，or to a place affigned：fo that the Glaffe bee fomewher raifcd to make the light to ftreeke upon the Table with fharpe Angles，as the Sunne doth when it is but a little elevated above the Horizos：for this lighe thall exceed the light of many Candles placed in the Roome，and bee more pleafant to the fight of him that ufeth it．
Ofother Glafjes of pleafore.

FIrfe，the Columnary and Tyramidall Glafes that are contained under right lines；doth reprefent the 1 mages as plaine Glaffes doe；and if they bee bowing，then they reprefent the $I-$ mage，as the concave and convex glafes doe．

Secondly，thofe Glaffes which are plaine，but have alcents of Angles in the middle，will Shew one to have foure eyes，two mouthes，two nojes，$\sigma c$ ．

## 

## EXAMINATION．

THefe exper iments will be found different ac． cording to the diverfe meeting of the Glaffer， which commonly are made foning wife at the end， by which there will be two diver So superficies in the Glaffe，making the exteriour Angle Some－ what raifed，at the interiour onely one fiperficies，

## Matbematicall Recreation.

which ysay bee covered according to ordinary Glaffes to gaufe a reflexion, and fo it will be but one Glaffe, whichby refrattion according to the different thickenefle of the Glaffe, and different Angles of the fouing forme, doe differently preo fent the Images to the eye, as foure eyes, two mouthes, troo nofes; fometimes three eyes, one mouth, and one nofe, the one large and the other lony, fometimes two eyes onely: with the mouth and the nofe deformed, zwhich the Gleffe (imponitrable) will not Shew. And of there be an interionr folid Angle, according to the difference of it, (as if it be more $b$ barpe) there will be reprefented two diftine double linages, that is, two entire vifages, and as the eAngle is oper, by fo much the more the donble Images will resnite and enter one within another, which will prefont fometimas a whole vifage extended at large, to have foure eyes, two noles, and two mourhes; and by moring the Glaffe the Angle will vanifh, and So the two Juperficies mill be tarned into one, and the duplicitie of Images will alf 6 vanisp and appeare but one onely: and this is eafily experimented with two little Glaffe of ficell, or fuch like fo united, that they make diverfe Angles and inclinations.

THirdly, there are Glaffes which make men feeme pale, red, and coloured in diverfe manners, which is caufed by the dye of the Glaffe, or the diverfe refraction of the Species: and thefe which are made of Silver, Latine, Steele; fre doth give the Ingeg a diverfe colour alfo.

In which one may fee that the appearances by fome are made faire, younger or older than they are; and contraraly others will make them foule and deformed: and give them a contrary vifage: for if a Glaffe bee cut as it may be, or if many peeces of Glaffe bee placed together to make a conveniable reflexion: there might be made of a - Mole (as it were) a mountaine, of one Haire a Tree, a Fly to be as an Elephant: bur I Thould be toolong if I fhould fay all that which might be faid upon the property of Glaffes. I will therefore conclude this difcourfe of the properties of thefe Glafes with thefe foure recreative Problemes following.

## Probiem: LXXVIII.

1. How to Beew to one that is fupitious, what is done in another Chamber or Roome: notwithfianding the interpofition of the wall.

FOr the performance of this, there muft bee placed three Glaffes in the two Chambers, of which one of them fhall bee tyed to the planching or feeling, that it may be commonto communicate the Species to each Glafo by reflexion, there being left fome hole at the top of the wall againf the Glaffe to this end: the two other Glaffes mult be placed againft the two walls at right $A$ ugles, as the figure here fheweth at $B$. and $C$.

Then

## Mathematicall Recreasion?

Then the fight at $\varepsilon$. by the line of incidence $F E$, fhall fall upon the Glaffe $B A$, and reflect upon the fuperficies of the Glafe B $C$, in the point $G$; fo that if the eye be at $G$, it fhould fee $E$, and $E$, would reflect upon the third Glaffe in the point $H_{2}$ and the eyc that is at aich righ - IM

## the pore

erraik $L$, will fee the Iraige that is at $E$. in the point of the Catbeti:

which Image fhall come to the eye of the fufpicious, viz. at $L$. by helpe of the third Glaffe, upon which is made the fecond reflexion, and fo brings unto the eye the object, though a wall be betweene it.

## Corolaire. 1. Ta sibbian afo cis

BY this invention of reflexions the affiegents of a Tomne may be ferne upon the Rampart: notwithltanding the Parapet;which the affeiged may doe by placing a glaff in the hollow of the Ditch, and placing another upon the toppe of the wall, fo that the line of incidence commings to the bottome of the Ditch, make an Angle equall so the Angle of refexion, then by this fcituation and reflexion, the Image of the affeigment will bee feene to him that is upon the Ramparf.

## Mathematicall Recreation.

Corolaire, 2.

BY which alfo may bee inferred, that the fame reflexions may bee feene in a Regular Polygon, and placing as many Glaffes as there are fides, counting two for one; for then the object being fet to one of the GIaffes, and the eye in the other, the Image will be feene eafily.

## Corolaire. 3.

FArther, notwithflanding the interpofition of many Walls, Chambers, or Cabinets, one may fee that which paffeth through the moft remotelt of them, by placing of many Glaffes as there are openings in the walls, making them to receive the incident Angles equall:that is, placing them in fuch fort by fome Geometricall affiftant, that the incident points may meete in the middle of the Glafles: but here all the defect will be, that the Images palfing by fo many reflexions, will be very weake and farce obfervable.

## Rrobiemo LXXIX.

How with a Musket to frike a marke, not looking towards it, as exals as ons aymsed at it.

ASlet the eye be at $O$, and the marke $C$; place a plaine Glafe perpendicular as e $\mathcal{B}$ : fo the marke $C$ © Thall bee feene in Gashetic $A$, viz.

## Mathematical Recreation.

viz. in $D$, and the line of reflexion is $D$ :now let the Musket FE, upon a reft, be mored to and fro untill it be ferne in the line OD, which admit to be $H G$ : fo giving
 fire to the CMinsket, it hall undoubtedly frize the marks.

## Corolatres.

From which may be gathered, that owe may exally Grote out of a Musket to a place. which is not Sene, being laundered by

$$
\begin{aligned}
& \text { Some obffacle, or other inge } \\
& \text { terpoftion. }
\end{aligned}
$$

AS let the eye be at $M$, the marker $C$, and the wall which keeper it from being feenes admit to be $2 \mathbb{B}$ :then fut up a plane Glaffe as $A B$, and let the Musket be $G H$, paaced upon his reft $P$ 0 . Now because the make $C$ is feene as D s move the Musket
 to and fro untill it doth agree with the line of reflexion MB S,
which fuppofe at $L$, fo fall it be truly placed, and giving fire to the Musker, it fhall not faile to ltrike the faid marke at $C$. I

## (1) Problem. LXXX.

TAke two Glaffes, and place them at right Angles one unto the other, as admit $A B$, and $C B$, of which admit $C B$ Horizontall, sclet the eje be at $H, \&$ the object or image tobe $\mathcal{D}$

> How to make an Image to be feene banging in the aire, baving his bead downeward. $E$; fo $D$ will bee refle ctedat $E$, fo to $N$, foD pag 104 to $H, E$ : then at $G$, $f o$ to $M$ and then to H ; and by a double rece flexion $\varepsilon D$ will feeme Fighrerpreb. Ni्य $s$ in $2 R$, the highed 1 Booke: 2.
point $D$ in $R$, and the point $E$ in 2 inver red as was faid, taking $D$ for the head, and $E$ for the feete; fo it will be a man inverfed, which will feeme to be flying in theaire: if the Image had wings unto it, and had lecretly fome motion: and if the Glaffe were bigge enough to receive many reflexions, it would deceive the fight the more by admiring the changing of colours that would be feene by that motion.

## Problem. LXXXI.

How to make a company of reprefentive Souldiers feeme to be a, Regiment, or how few in number may bee muttiplyed to feeme to be wany is number.

TO make the experiment upon men, there muft be prepared two great glaffes; but in fead of ic we will fuppoferwo leffer, as o $H$. and $F F$, one placed right againft another perpendicular to the Horizon, upon a plaine levell $T$ able: between which Glaffes Ied there bee ranged in Battalion-wife upon the fame Table an number of fmall men,
 according to the fquare $G, H, I_{3} F$, or in any other forme or poture: then may you evidently fee how the faid battle will bee multiplyed and feene farre bigger in the appearance than it is in effect

## Corolaire.

BY this invention you may make a little Cabinet of foure foote long, and two foote large, (more or leffe) which being filled with

## Mathematiceell Recreation:

Rockes or fuch like things, or there being put into it Silver, Gould, ftanes of lutter, lewels, $6 \subset$. and the walls of the faid Cabinet being all covered or hang with plaine ©laffo; thefe. vifibles will appeare manifoldly increafed, by resfon of the multiplicitie of reflexions, and a: the opening of the faid Cabinet, having fet fometbing which might hide then from being feene, thofe that looke into it will be aftonifhed to fee fo few in number which before fee. mod to be fo many.

> Problem. LXXXII.
> Of fine and pleafant Dyalls:

cOuld you choofe a more ridiculous one than the naturall $\mathcal{D}$ yall written amongft the Greeke Epigrams, upon which fome found Poet made verfos; fhewing that a man carryeth about him alwaies D yall in his face by meanes of the nofe and teeth; and is not this a jolly Dyall, for he neede not but open the noosth, the tines fhall bee all the teeth, and the nofe fhall ferve for the file.

## of a Dyall of hearbes.

CAn you have a finer thing in a Garder, or in the middle of a Compartement, than to fee the lines and the number of bowres reprefented with little buhie branbes, as of Hyfore
being or fuch which is proper to be cut in the borinders; and at the top of the ftile to have a fanne to frew which way the minde bloweth: this is affoiter very pleafant and ufefull.

## Of tbe Dyall upon the fungers and the hand.

TS it not a commoditic very agrecable, when Lone is in the field or in fome village without any other Dyall, to fee onely by the band what of the clocke it is, which gives it very neare; and may bee practifed by the left band in this manner.
Take a ftraw or like thing of the length of the Index, or the fecond finger, hald this fir on very right betweene the thumbe and the right finger, then ftretch forth the hand and turne yous backe and the palme of your band towards the Sunne; fo that the fhaddow of the mufcle which is under the thumbe touch the line of life, which is betweene the middle of the two other great lines, which is feene in the palme of the band; this done, the end of the baaddone will kew what of the clocke it is: for at the end of the great finger it is 7 in the morning or 5 in the evening; at the end of the Ring finger ic is 8 in the morning, or 4 in the evening; at the end of the litele finger or firft joynt, it is 9 in the morning, or 3 in the afternoome; 10 and 3 at the fecond joynt, I 1 and z at the third joynt, and midday in the line following, which comes from the end of the Index.

## Mathematicall Recreation. <br> Of a Dyallwbicb was about an Obee liske at Rome.

vVAs not this a pretty fetch upon a pavement, to choofe an Obeliske for a Dyall, having 106 foote in height, without removing the Baffs of it? Plinie affures us in his 26 booke and 8 Chap. that the Emperour Augufins having accommodated in the field of Mars an Obeliske of this height, he made about it a pavement, and by the induftry of Manilius the Mathematitian, there was enchaced markes of Copper upon the Pavement, and placed alio an apple of Gould upon the toppe of the faid Obeliske, to know the boure and the courfe of the Swnxe, with the increafe and decreafe of dayes by the fame fhadow: and in the fame manner doc fome by the fladdow of their head or other file, make the like experiments in e Afremomsie.

## Of Dyalls with Glafles.

PTolomise writes, as Cardanes repores, that long agoe there were Glaffes which ferved for Dyalls, and prefented the face of the behoulder

## Mathematicall Recreation.

houlder as many times as the boure ought to be, twice if it were 2 of the clocke; $g$ if it were 9 , \&xc. But this was thought to be done by the helpe of water, and not by Glafes; which did leake by little and little out of the veffell, difcovering anon one Glaffe, then anon two Glaffes, then $3,4,5$ Glaffes, ofe. to thew fo many faces as there were boures, which was onely by leaking of mater.

## Of a Dyall whichbath a Glaffe in the place of the sill.

VVHat will you fay of the invention of cMathematicians, which finde out dayly fo many fine and curious novelties? they have now a way to make Dyalls upon the wainfcote or feeling of a Chamber, and there where the Sumne can never fhine, or the beames of the Sunne cannot directly ftrike : and this is done in placing of a little glaffe in the place of the file which refecteth the light, with the fame condition that the Baddow of the filte theweth the houre: and it is eafie to make experiment upon a common Dyall, changing onely the difpofition of the Dyall, and tying to the end of the file a peece of plaine Glaffe. The Almaines ufe it much, who by this way have no greater trouble, but to put their wofes out of their beds and fee what a clocke it is; which is reflected by a littic hole in the mindow upon the rall or feeling of the Chamber.

## EXAMINA-

## Sathematicall Recreation.

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## EXAMINATION:

I2 this there it two experiments comiderable, the firft is with a very little Glaffe placed fo that it may be open to tho beames of the Sunne; the otber bath repect to a pacious or great Glaffe placed to a very little hole, fo that the Sun may Bine on it, for then the fladdow which is caft upon the Dyall is converted into beames of the Sunne, and will reflect and bee caf upon a plaine oppofite: and in the other it is a bole in the window or fuch like, by which may paffe the beames of the Sunne which reprefenteth the extreamity of the ftile, and the Glaffe reprefenteth the plaine of the Dyall, upon which the beames being caft in manner of thaddowes refletteth upon a plaine oppofite: and it is needfull that in thisfecond way the Glaffe may be 臽ations as before to receive the delireaments of the $D$ yall.

Otherwife you nay draw the lineaments of a Dyall upon any plaine looking-glafe which reflocteth the Sunne-beames, for the applying a Atile or a pearle at the extreamitic of it:and place dio the Sunne, the reflexion will be anfwerable to the delineaments on the Glaffe: but bere note that the Glaffe ought to be great, and fo the deiineaments tbereon.

But that which is moft noble is to draw houre lines upon the outfide of the Glafte of a window, and

## Mathematicall Recreation.

and placing a filo thereto upon the owtfide, the Shaddow of the fitile will be feene within, and jo you bave the boure more certaine wishout any difficulsie.

## Of Djalls with mater.

SVch kinde of Dyalls were made in ancient times, and alfo thefe of fand: before they had skill to make Sun-dyalls or DJalls with wheeles; for they ufed to fill a veffll with ma. ter, and having experience by tryall that it would runne out all in a day, they did mark within the veffell the houres noted by the running of the water; and fome did fet a peece of light board in the veffell to fwimme upon the top of the water, carrying a little ftatne, which with a frall fficke did point out the howre upon a columse or wall, figured with houre notes as the veffell was figured within.

Vitravius writes of another manner of maser-


Dyall more dificult; and Baptiftea Porta amonglt his naturall Secrets, delivers this invention following. Take a vefell full of water like a Chaldrom, and another veffell of glaffe like unto a Bell, (with which fome accuftome to cover (Melons:) and let this dron, having a fmall hole at the bottome, then when it is placed upon the water, it will finke by little and little: by this one may marke the houres on the furface of the Glafle to Terve another time. But if at the beginning one had drawn the water within the fame ve ffell of glafe in fucking by the little hole, the water would not fall out, but as faft as che aire would fucceed it; entering flowly at the little hole : or contrarily the houres might bee diftinguithed by diminution of water, or by augmentation.

Now it feetnes a fafer way that the water paffe our by drop and drop, and drop into a $C y$ lindricall Glaffe by thelpe of a Pipe: for having marked the exterior part of the Cylinder in the houre nores, the water it felfe which falls within it, will fhew what of the clocke it is, farre better than the ranning of fand; for by this may you have the parts of the houres mof accurate, which commonly by fand is not had: and to which may be added the houres of other Cown. treyes with greater eafe. And here note that as foone as the water is out of one of the Glaffes you may turne it over into the fame againe out of the other, and folec it runne an new.

PROBLEM. LXXXIII.

Of Camons or great e Artillery. Souldiers, and others would willingly fee this Probleme, which containes three or foure $f$ ubtile queftions: The firft is how to charge a Cannors ì without $P$ owder.

This may be done with aire and water only, having throwne cold mater into the Cannon, which might be fquirted forceably in by the clofure of the mouth of the Pcece, that fo by this preffure the aire might more condence; then having a round peece of zoood very juft, and oyled well for the betrer to nide, and thruft the Bullet when it fhall be time: This peece of mood may bee held faft with fome Pole, for feare it be not thruft out before his time : then let fire bee made about the Trunion or hinder part of the Peece to heate the aire and water, and then when one would fhoote it, let the pole be quickly loofened: for then the aire fearching a greater place, and having way now offered, will thruft out the wood and the bullet very quicke: the experimence which wee have in long trunkes fhooring out pellats with dire only, theweth the verity of this Probleme.
2. In the fccond queftion it may be demanded, how much time doth the Bullet of Cannon feend in the aire before it falls to the ground.

THe refolution of this 2 geffion depends upon the goodneffe of the Perce and charge thereof, feeing in each there is great difference. It is reported that Ticho Brabe, and the Landf. grave did make an experiment upon a Cannon in Germany, which being charged and fhot off; the Bullet fpent two minutes of time in the aire before id fell : and the diftance was a German mile, which diftance proportionated to an houres time, makes 120. Italian miles.
3. In the third queftiex it may be asked, how it comes to palfe, that a Cannon Booting upwards, the Buller flies with more violence. than being gos point-blanke, or foooting downeward.

IF we regard the effect of a Cannon when it is to batter a wall, the 2 uefion is falle, feeing it is moft ovident that the blowes which fall
perpendicular upon a wall, are more violent than thefe which ftrikes byaf-wile or glaunfingly.

But confidering the ftrength of the blow only, the Queftion is moft true, and often experimented to be found true : a Pecce mounted at the beft of the Randon, which is neare halfe of the right, conveyes her Bullet with a farre greater violence than that which is fhot at, Point blanke or mounted paralell to the Horizon.

The comon reafon is, that fhooting high, the fire carries the bowle a longer time in the aire, and the aire moves more facill upwards, than downewards, becaufe that the ayrie circles that the motion of the bullet makes are finonelt broken. Howloever this be the generall tener, it is curious to find out the inequallity of moving of the aire; whether the Bullet fly upward, downeward, or right forward, to produce a rencible difference of motion: and fome thinke that the Cannon being mounted, the Bullet preffing the Powder maketh a greater refiftance,and to caufeth all the $P$ owder to be inflamed before the Bullet is throwne out, which makesit to be more violent than otherwife it would be. Whenthe Cannon is otherwife difpofed, the contrary arives, the fire leaves the Bullet, and and the Brlet rouling from the Potrder refilts leffe: and it is ufually feene, that fhooting out of a Musket charged onely with Powder; to thoote to a marke of Paper placed Poumt blanke, that there are feene many frall holes in the

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paper, which cannot be other than the graines of Poroder which did not take fire: but this latter accident may happen from the overcharging of the Peece, or the length of it or windy, or dampeneffe of the $P$ owder.
From which fome may thinke, that a Cannon pointed right to the Zenith, fhould fhoote with greater violence, than in any other mount or forme wharfoever: and by fome it hath beene imagined, that a Bullet fhot in this fafhion hath beene confumed, seelt, and loft in the aire, by seafon of the violence of the blow, and the activitie of the fire, and that fuadry experiments wnth beene made in this nature, and the Bulles never found. But it is hard to beleeve this afo fertion: it may rather be fuppofed that the Bul. let falling farre from the Peece cannat be difcerned where it falls: and fo comes to be lon.
4. In the fourth place it may be asked, whether the difcharge of a Cannon be fo much the greater, by how much it is longer.

1T feemeth at the firit to bee molt true, that the longer the Peece is, the more violent it fhootes: and to fpeake generally, that which is direction by a Trunke, Pipe, or other concavi-f tie, is conveyed fo much the more violent, on better, By how much it is longer; either in refpect of the fight, bearing, water, fire, of c.and the reaion feemes to hold in Cannons, becaute in thele that arelong, the fire is retained a lonser time in the concavitic of the Peece, and fo

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throwes out che Bullet with more violence; and experience lets us fee that taking Cannons of the fame boare, but of diver fitic of length from 8 foote to 12 ; that the Canson of 9 foote long hath more force than that of 8 foot long, and 10 more than that of 9 , and fo unto 12 foote of length. Now the ufuall Cannon carries $\sigma$ co Paces, fome more, fome leffe: yea, fome but 200 Paces from the Pecce, and may hoote into foft earth is or 17 foote, into fand or earth which is loofe, 22 or 24 foore; and in firme ground, about 10 or is foot, \&ic.
It hath beene feene lately in Germany, where there was made Peeces from 8 foote long to 17 foote of like boare, that fhooting out of any Peece which was longer than 12 foote; the force was diminihed, and the more in length the Peece increafeth, the leffe his force was; therefore the length ought to bee in a meane meafure; and it is often feene, the greater the Cannon is, by fo much the fervice is greater: butto have it toe long or too fhort, is not convenient, but a meane proportion of length to bee taken; otherwife the flaue of the fire will bee overpreffed with aire: which hinders the motion in refpect of fubflance, and diftance of getting out,


Of prodigious progreffon and multeplication, of Crentures, Plants, Frsites, Numbers, Gold, Silver, ơc. when they are alwayes angmexted by cortaine proportion.

HEre we flall flhew things no leffe admirable, as recreative, and yet fo certaine and eafie to be demonftrated, that there needes not but Multiplication only, to try each particular: and firlt,
Of graines of Muftard. Seed.

FIr $f$, therefore it is certaine that the increafe of one graine of Muftard-feed for 20 yeares space, cannot bee contained within the vifible world, nay if it were a hundred times greater than it is: and holding nothing befides from the Center of the earth even unto the firmament, but onely fmall graines of $M 1$ uffard-feed. Now becaufe this feemes but words, it muft be provelby Att; as may bee done in this wife, as fuppofe one Muflard-feed fowne to bring forth a tree or branch, in each extendure of which might be a thoufand graines: but we will fuppole onely a rhoufand in the whole tree, and let us proceed to so yeares, every feed to bring forth yearely a thouland graines; now multiplying aiwayes by a thoufand, in leffe then 77 years

## $M$

 dallh \&ite $\sqrt{9}$ want Wherese tygetan whate albe wiu zthent and of whorer rate th thentt prias 0 riy $y$ pri! araned wi ; W xliply ver: an wors in sathin idinft res $g$ whet i
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you fhall have fo many graines which will furpaffe the $\int$ ands, which are able to fill the whole frmament: for following the fuppofition of Archimedes, and the moft probable opinion of the greatneffe of the firmament which Tico Brahe hath left us; the number of graines of fand will be fufficiently expreffed with 49 Ciphers, but the nnmber of graines of Muftard-feed at the end of 17 yeares will have 52 Ciphers: and morcover graines of Muftard-feed, are farre greater than thefe of the fands: it is therefore evident that at the feventeenth yeare, all the graines of Muftard-feed, whicn thall fucceffively fpring from one graine onely, cannot be contained within the limits of the whole firmament; what fhould it be then, if it chould bee multiplyed againe by a thoufand for the 18 geare: and that againe by a thoufand for every yeares increafe untill you came to the zo years? its a thing as cleare as the day, that fuch a heap of Muffard-seed would be a hundred thoufand tinses greater than the earth: and being onely but the increafe of one graine in 20 yeares.
of Pigges.

SEecondly, is it not a ftrange propofition, to fay that the great Turke with all his Revenues, is not able to maintaine for one yeares time, all the Pigges that a Som may pigge with all her race, that is, the increale with the increafe unto is yeares: this feemes impoffible, yet it smoft true; for let us fuppofe and put the care
that a Sow bring forth but 6, two males, and 4 females, and that each female fhall bring forth as many every geare, during the fpace of 12 yeares, at the end of the time there will be found above 33 millisns of Pigges: now allowing a crowne for the maintenance of each Pigge for a yeare, (which is as little as may be, being but neare a halfe of a farthing allowance for earh day;) there muft bse at the lealt fo many crownes to maintaine them, one a yeare, viz. 33 millions, which exceedes the Turkes revenue by much.
Of graines of Corne.

THirdly, it will make one aftonimed to thinke that a graine of Corne, with his increafe fucceffively for the face of 12 yeares will produce in grains 244140625000000000000 , which is able to load almoft all the creatures in the world.

To open $w^{\text {ch }}$, let it be fuppofed that thefirft yeare one graine being fowed brings forth 50 , (but fometimes there is feen 70 , fometimes 100 fold) which graines fowen the next yeare, every one to produce 50 , and fo confequently the whole and increafe to be fowen every yeare, untill 12 yeares bee expired, there will bee of increafe the aforefaid prodigious fumme of grains, viz. 244140625000000000000 , which will make a cubicall heape of 6258522 graines every way, which is more than a cubicall body of 31 miles every way: for allowing 40 graines

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in length to each foote, the Cube would bee 136463 foot every way: from which ic is evident that if there were two hundred thouland Citties as great as London, allowing to each 3 miles Square every way, and 100 foot in heighr, there would nor bee fuificient roome to containe the aforefaid quantitie of Corne: and fuppofe a bufhell of Corne were equall unto two Cubicke feete, which might containe twenty hundred thoufand graines, then would there be 122070462500000 bufhells, and allowing 30 burhells to a $T$ rune, it would bee able to loade 8138030833 veffells, which is more than eight thoufand one hundred and thirty eigh millions, fhippe loadings of 500 Tunne to each fhippe: a quantitic fo great that the Sea is fcarce able to beare, or the univerfall world able to finde veffells to carry it: And if this Corne fhould bee valued at halfe a crowne the bufbelk, it would amount unto $152588078: 2500$ pounds fterling, which I thinke exceedes all the Treafures of all the Princes, and of other particular men in the whole morld; and is not this good husbandry to fowe one graine of Corne; and to continue ic in fowing, the increale onely for 12 yeares to have fogreat a profit.

## Of the increaje of Sheepe.

FOurthly, thofe that have great flockes of Sheepe may bee quickly rich if they would preferve their Sbeepe without killing or felling of them: fo that every shecpe produce one each will multiply and increafe unto 61689,00 , which is above 60 millions, and 16 bundred thoufand Skeepe : now fuppofing them worth but a crowne a peece, it would amount unto \$422400 pounds ferling, which is above 15 millions, and foure bundred and twenty thous and pounds, 2 faire increale of one Sheepe: and a large portion for a Chirde if it chould bee allorted.

## Of the increaje of Cod-fiß, Carpes, 6 .

FIftly, if there be any creatures in the world that doth abound with increafe or fertilitie, it may be rightly attributed to fif; for they in their kindes produce fuch a great multitude of egges, and brings forth fo many littlo ones, that if a great part were not deftroyed continually, within a little while they would fill all the Sea, Ponds, and Rivers in the world; and it is cafie to fnew how it would come fo to paffe, onely by fuppofing them to increafe without taking or deftroying them for the fpace of 10 or 12 yeares: having regard to the foliditie of the waters which areallotted for to lodge and containe thefe creatures, as their bounds and place of reft to live in.

## Of the increase and multiplication of men.

$S$
Ixtly, there are fome that cannot conceive how it can be that from eight perfons (which

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was faved after the deluge or Noabs fleod) hould fpring fuch a world of people to begin 2. Monarchie under Nimrod, being but 200 yeares after the flood, and that amongtt them thould be raifed an army of two bundred thonfand foghting Men: But it is eafily proved if we take but one of the Children of $\mathcal{N o a h}$, and fuppofe that a new generation of people begun at every 30 yeares, and that it be continued to the feventh gemeration which is 200 yeares; for then of one onely family shere would bee produced one bundred and eleves thonfand foules, three hundred and five to begin the world: though in that time men lived longer, and were more capable of multiplication and increafe: which number fpringing onely from a fimple production of one yearely, would be farre grea. ter, if one man hould have many wives, which in ancient times they had: from which it is alfo that the Children of Ifrael, who came into Egyp? but onely 70 foules, yet after 210 yeares captivitic, they came forth with their hoftes; that there was told fixe busdred thoufand fighting men, befides old people, women and children; and he that fhall feparate but one of the families of lofeph, it would bee fuificient to make up that number: how much more fould it bee then if wee fhould adjoyne many families together?

## Of the increafe of numbers.

Eventhly, what fumme of money fhall the Ditie of Londos bee worth, if it fhould bee fold, and the mony be paid in a yeare after this

## Mathematicall Recreation.

 manner : the firt woocke to pay a pinne, the fecond moole 2 pinnes, the third wecke 4 pinnes, the fourth wocke, 3 pinnes, the fift weeke 16 pinses: and fo doubling untill the 52 weelees, or the yeare be expired.Here one would thinke that the value of the pinnes would a mount but to a mall matter, in comparifon of the Treafures, or riches of the whole Citic: yet it is moft probable that the number of pinnes wouldamount unto the fum of 451959962868 i2 15 , and if we fhould allow unto a quartcr a hundred thoufand pinnes, the whole would contame nintic eight millions, foure hundred thouland Tunne: which is able to loade 45930 Shippes of a thoufand Tunne a peece: and it wee fhould allow a thoufand pinnes for: a penny, the fumme of money would amount unto above eighteene thoufand, eight bandred and thirty millions of pounds ferling, an high price to fella Citic art: yet certaine, according to that firtt propofed. So if 40 Townes were fold upon condition to give for the firft a penay, for the fecond 2 pence, for the third 4 pence, Go, by doubling all the reft unto the laft, it would amount unto this number of pence, 10995 1627775 , which in ponnds is 7581298444 , that is foure thoufand five handred and fourefcore millions of pounds and * morc.

## 'Mathematicall Recreation.

Of a man that gathered up Apples, Stones, or fucblike upon a condition.

EIghtly, admit there were an hundred $A p p l e S_{2}$ Stones, or fuch like things that were placed in a fraight line or right forme, a pace one from another, and a basket being placed a pace from the firf: how many paces would there be made to put all there Stanes into the basket, by fetching one by oue: this would require neare halfe a day to doe it, for there would be made terne thoufand and a bundred paces before he fhould gather them all up.

> Of Changes in Bells, in mufic all Inftruments, tranfmutation of places, in numbers, letters, men or fuch like.

NInthly, is it not an admirable thing to confider how the skill of numbers doth eafily furnif as with the knowledge of myfterious and hidden things, which fimply looked into by others that are not verfed in A Arithmeticke, doe prefent unto them a world of confufion and difficultie.
As in the firft place, it is often debated amongt our common Ringers, what number of Changes there might be made in $5,6,7,8$, or more Bells: who fpend much time to anfwere their owne doubts, entering often into a Labyrinth in the ferchthereof:or if there were rovoyces, how many feverall notes might there
be? Thefe are propofitions of fuch facillitie, that a child which can but multiply one number by another, may eafily refolve it, which is bur only to multiply every number from the unitie fucceffively in each others product, unto the terme affigned : fo the $\sigma$. number that is againft $\sigma$. in the Table, is 720 , and fo many Changes may be made upon 6 Bells, upon 5 there are 120 , © 6 .

In like manner againt 10 in the Table is ${ }_{3} \sigma_{2} 8800$, that is, three millions, fixe humdred twen y eight thoufand, eight hundred $\&$ fourefcore: which fhewes that Io voyces may have fo many conforts, each man keeping his owne note, but onely altering his place;and fo of fringed Inftruments: \& the Gamanth may be varied according to which, anfwerable to the number againft $X$, viz. 1124001075070399680000 nores, from which may be drawne this, or the like propofition.

Suppofe that 7 Schollers were taken out of a free Schoole to bee fent to an Univerfitie, there to be entertained in fome Colledge at commons for a certaine fumme of money, fo that each of them have two meales dayly, and no longer to continue there, that fitting all together upon one bench or forme at every meale, there might be a diverfe tranfmutation of place, of account in fome one of them, is comparifon of another, and never the whole company to be twice a. like in fituation: how long may the Stemard entertaine them? (who being not skilled ia this fetch may anfwere unadvifedly.) It is moft certaine that there will bee five thoufand and

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 forty feverall pofitions or changingin the featings, which makes
years time not wanting 30 dayes

Hence fro this mutabilitie of tranfmutation, it is no marvell that by 24 letters there arifeth and is made fuch variety of languages in the world, and luch infinite number of mords in each lan- $\quad 36_{2} 8800$ guage; feeing the di- 39916800 veritice of Jyllables 479001600 produceth that ef- 6227020800 fect; and alfo by 87178291200 the interchange- 1307674368000 ing and placing/ 20922789888000 of letters a- 355087537926000 monght the 6402375683928000 vowels, and 12:64513799463:000 among ft 2432902759892640000 théfelves 51090957957745440000 maketh 1124001075070399680000 thefe 25852024726619192640000 fylld 620448593438860623360000 bles:w ${ }^{\text {ch }}$ alphabet of 24 letters may be varied fo many times, vi. 620448593438860623360000 which is fixe bundred twenty thoufand, foure bundred forty eight millions, five bundred ninety tbree thoufand, foure husdred thirty eight millions of millions, and more.
Now allowing that a man may reade or fpeake one hundred thoufand word's in an boure, which is twice more words than there are contained and if there were foure thoufand fixe bundred and fifty thoufand millions of men, they could not fpeake thefe words; (according to the hourely proportion aforefaid in threefcore and ten thoufand yeares; which variation and tranfmutation of letters, if they fhould bee written in bookes allowing to each leafe 28000 words, (which is as many as poffibly could bee inferted, ) and to each booke a reame or 2 a quire of the largeft and thinneft printing paper; fo that each book being about is inches long, 12 broad, and $\sigma$ thicke: the bookes that would be made of the tranfmutation of the 24 letters a forefaid, would bee at leaft 38778037089928788 : and if Library of a mile fquare every way, of 50 foot high, were made to containe 250 Galleries of 20 foote broad a peece, it would containe foure bundred millions of the faid bookes: fo there muft be to containe the reft no leffe than 96945092 fuch Libraries; and if the bookes were extended over the furface of the clobe of the earth, it would a decuple covering unto it: a thing feeming moft incredible that 24 letters in their tranfmutation fhould produce fuch a prodigieus number; yet moft certaine and ins fallible in computation.

## of a servant bired upan certaine conditions.

A Servant faid unto his mafter, that hee

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he would but onely lend him land to fowe one grine of Corne with all his increafe for 8 yeares time; how thinke you of this bargaine: for if he had but a quarter of an intch of ground tor each graine, and each graine to bring forth jearely of increafe 40 graines; the whole fum would amount unto, at the terme aforefaid, 6553500000000 graines: and feeing that three thoufand and fixe bundred millions of inaches doe but make one mile fquare in the fuperficies, it thall bee able to receive forutecne thoufand avd foure bundred millions of graines, which is 14400000000 : thns dividing the aforefaid 6553600000000 , the 2notient will bee 455, and fo many fquare miles of land mut there be to fow the increafe of one graine of Corne for 8 yeares, which makes at the leaft foure bundred and twenty thoufand Acres of land, which rated but at five fhillings the Acre fer Ansum, amounts unto one bupdred thoufand pound; which is twelve thouland and five bundred poxsd ayeare, to bee continued for 8 yeares; a pretty pay for Mafter Servants 8 yeares fervisf.

> Pros:
Ртовдем: LXXXV.

Of Founta:nes, Hydriatiques, Machinecke, and other experiments upon water, or other liquor.

1. Firft how to make water at the foote of a monntaine to afcend to the top of it, and fo to defcend on the otber Fide.

TO doe this there muft bee a pipe of lead, which may some from the Foustaine $A_{\text {, }}$ to the top of the Mosntaine $\mathcal{B}$; and foto defcend on the other fide a little lower than the Fonntaine, as at $C$ : then make a hole in the $P$ ipe at the toppe of the Momntaine, as at B, and ftop the end of the Pipe at $A$ and $C$; and fill this Pipe at $B$ with water: and clore it very carefully agaise at $B$, that no
 aire get in: then unfop the end at $A$, and at $C_{\text {; }}$ then will the water perpetually runne up the hill, and defcend on the other fide, which is an invention of great confequence to furnifh Tillages that want water.
2. Secondly,
2. Secondly, how to know what wine or other liguar there is in a veflell without opening the bung-bole, and without making any other bole, than that by which it runs out at the toppe.

IN this Probleme there is nothing but to take a bowed pipe of Glaffe, and put it into the faucets bole, and Itopping it clofe about : for then you fhall fee the rine or liguor to alcend in this Pipe, untill it bee juft even with the ligror in the veffell; by which a man may fill the veffell, or pat more into it: and fo if need were, one may empty one weffell into another without opening the bung-bole.
3. Thirdly, how is it that it is faid that a veffell bolds more water being placed at the foote of A Mountaive, thon ft anding upon the toppe of it.

THis is a thing mof certaine, becaufe that water and all other liguor difpofeth it felfe spherically about the Center of the earih; and by how much the veffell is nearer the Center, by fo much the more the furface of the water makes a leffer $\beta$ beare, and therefore every pare more gibbous or fwelling, than the like part in a greater $\beta$ beare: and therefore when the fame veffell is farther from the Center of the earth, the furface of the water makes a greater $\beta$ beare, and therefore leffe gibbous, or fwelling over the vefoll: neare the Center of the earth holds more water than that which is farther remote froin it; and fo confequently a veffelf placed at the bottome of the Mountaine holds more water, than being placed on the top of the Mountaine: Firf, therefore one may conclude, that one and the fanc veffell will alwayes hold more: by how much it is nearer the center of theearth. Secondly, if a veffitat be very neare the Center of the earth, there will bee more water above the brims of it,
 than there is within the veffell. Thirdly, a veffell full of water comming to the Center will fpherically increafe, and by little and little leave the veffell; and paffing the Center, the veffell will be all emptied. Fourthly, one cannot carry a Paile of water from a low place to a bigher, but it will more and more run out and over, becaule that in afcending it lies more levell, but defcending it fwelles and becomesmore gibbow.
4. Forirthly, to conduct water from the toppe of - one Mountaine, to the top of another.

A S admit on the top of a Mointaine there lis a foring, and at the toppe of the other

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It tuf) Mountaine there are inbabitants which wants water: now to make a bridge from one Mountaine to another, were dificicult and too great a charge; by way of Pipes it is eafie and of no great price:for if at the $\int$ pring on the toppe of, the Mountaine be placed a Pipe, to defcend into the valley, and afcend to the other Monntaine, the water will runne naturally, and continually, provided that the fpring be fomewhat higher than the paffage of the water at the inbabitants.
5. Fifly, of a fine Fountaine which 乃ounts water very high, and with great violence by turning of a Cocke.

LEt there be a veffell as $A B$, made clofe in all his parts, in the middle of which let $C$ $D$ bea Pipe open at $D$ neare the bottome, and then with a Squirt fquirt in the water at $C$, flapped above by the cocke or fascet Cr with as great violeace as poffible you'can; and turne the Cocke immediately.Now there being an indifferent quantitic of water \& aire in the veffit, the water keepes it felfe in the bottome, and the aire which was graatly preffed,feekes for more place, that,

$\qquad$ tanning turning the cocke the mater iffucth forth at the Fipe, and Ayes very high; and that efpecially if the veffell bee a little heated: fome make ufe of this for an Ewer to walh hands withall, and therefore putting a moveable Pipe above $C$, fuch as the figure fheweth: which the mater will caufe to turne very quicke, pleafurable to behold.
> 6. Sixetly, of atrchimedes forew, which makes mater ascend by defcending.

THis is nothing elfe but a Cylinder, about the which is a Pipe in forme of a forew, and when one turnes it, the water defcends alwaies in refpect of the $P$ ipe: for it paffeth from one part which is higher to that which is lower , and at the end of the engine the water is found bigher than it was at the fpring. This great enginer admirable in all CMathematicall Arts invented this Inftrmment to walh King Hieroies great veffelts, as fome Authors fayes, alfoto water the fields of $E$ gypt, as Diodorns Witueffeth: and Cardawus reporteth that a Citizen of Mislan having made the like eno gise, thinking hime felfe to bee the firlt ine. venter,conceived fuch exceeding joy, that be became foll, 2 .

Againe fratlint arsevole , tanathe id: itis Ifro it, bift circ dalway efcendin manetot tillout. famove dike, w us of th w: fot doat liguc Ilmotio atrasy $b$ tred of Iif about artance: y drawn timed fom ter may whithef gwill haturnir Hafcend heresvo inght th ipmotic Fard, the Whaign.

## Mathematicall Recreation.

Againe a thing may afcend by deicending, if apiprall line bee made having wany circulations or revolutions; the laft being alwayes leffer than the firft, yet higher than the Plaine fuppofed: it is moft certaine that then putting a ball into it, and turning the pirall line fo, that the firlt circslation may bee perpendicular, or touch al wayes the fuppofed Plaine:the ball fhall indefcending continually afcend, untill at laft it come to the higheit part of the fpirall line, \& fofall out. And here efpecially may be noted; that a moving body as water, or a Buller, or fuch like, will never afcend if the belicall revolution of the forew be not inclining to the Horizon: fo that according to this inclination the ball or liquor, may defcend alwayes by a continuall motion and revolution. And this experiment may be more ufefull, naturally made with athreed of iron; or latise turned or bowed bea lically about a Cylinder, with fome diftinction of diftances betweene the Helices; for then having drawne out the Cylinder, or having hung or tied fome weight at it in fuch fert, that the water may eafily drop if one lift up the faid thred: thefc belices or revolutions, notwithftanding will remaine inclining to the Horixon, and then turning it about forward, the faid weight will afcend, but backward it will defcend. Now if the revolutions bee alike, and of equallitie amongt themfelves; and the whirling or curning motion be quicke, the fight will be fo deceived, that producing the a tion it will feeme to the ignorant noleffe than a miracle.

> 7. Seventbly, of another fine Fountaine of pleafure.

THis is an engine that hath two wheeles with cogges, or teeth as $A B$, which are placed within an Ovall C D, in fuch fort, that the teeth of the one, may enter into the notches of the other; but fo jult that neither aire nor water may enter into the O vall coffer, either by the middle or by the fides, for the wheele mutt joyne fo neare to the fides of the ceffer, that there be no vacuitie: to this there is anaxelree with a handle to each wheele, fo that they may be turned, and $A$ being turned, that turneth the other wheele that is oppofite: by which motion the aire that is in $E$, and the water that is carried by the hollow of the wheeles of cach fide, by continuall motion, is conftrained to mount and flie out by the funnell $F$ : now to make the water runne what way one would have it, there may be applyed upon the toppe of the $\mathcal{P i p g} F$, two other moveable Pipes inferted one within another; as the figare fheweth. But here note thatthere may accrue fome inconveniency in this machanicke, lecing that by quicke turning the cogges


## Mathematicall Recreation.

or teeth of the wheeles running one againft 2nother, may neare breake them, and fo give way to the aire to enter in, which being violently inclofed will efcape to occupie the place of the water, whofe weight makes it fo quicke: howfoever, if this Machine be curioully made as an able workeman may eatily doe, it is a moft foveraignie engine, to caft water high and farre off for to quench fires. And to have it to raine to a place affigned accommodate a fecket having a Pipe at the middle, which may point towards the place being fet at the top thereef, and fo having great difcretion in turning the Axis of the whede, it may worke excceding well, and continnelong.

## 8. Engky iof fine watering potte for gardens.

THis may be made in forme of a Bottleac= cording to the laft figure or fuch like, having at the bottome many fmall holes, \& at the necke of it another hole fome what greater than thefe at the bottome, which hole at the toppe you muft unftop when you would fill this watering pot, for then it is nothing but putting the lower end into a paile of water, for fo it will fill it felfe by degrees: and being full, put your thumbe on the hole at the necke to fop it, for then may you carry it from place to place, and it will not fenfibly runne out, yet fomething will if it were fo clofe flopped, and all in time contrary to to the ancient tenet in Philofopby, that sire will not pentrate.

9 Ninthly, bow easily to take wine out of a veffell at the bung-bole, without 'piercing of a bole in the veffer.

TN this there is no need but to have a Cane or - Pipe of Glaffe or fuch like, one of the ends of which may be clofed up almoft, leaving forme fall hole at the end; for then if that end be feet into the weffell at the bung-hole, the whole Cane or Pipe will bee filled by little and litell, and once being fut frappe the other end which is without: and then pull out the Cate or Pipe, fo will it bee full of wine; then opeing a little the rope above, you may fill a Glaffe or other Pate with it, for as the wine iffueth out, the dire commeth into the cane or Pipe to fupply vacuity.
10. Tenthly, bow to measure irregular badies by belpe of water.
One throw in the body or magnitude into a befell, and keeps that which floweth out over, laying it is alwayes equall to the thing caff into the water: but it is more neater this way so powre into a veffell such a quantity of water, which

## Matbematicall Recre ation.

which may be thought furficient to cover the body or magnitude, and make a marke how high the water is in the veffell, then powre out all this water into another weffell, and let the body or magnitude be placed iato the firlt veffell; then powre in water from the fecond veffell, untill it afcend unto the former marke made in the firft vefell; fo the water which remaines in the fecond veffell, is equall to tine body or magnitude pur into the water: but here note that this is not exact or free from error, yet nearer the truththan any Geometrician can otherwife poffibly meafure, and thefe bodyes that are not fo full of powers are more truly meafured this way, than others are.

## 11. To finde the weight of water.

$S$Eeing that $\frac{514}{1000}$ part of an ounce weight, makes a cubicall inch of water: and every pound weight Haverdepoife makes 27 cubicall intches, and $\frac{9}{2}$ efere, and that 7 Gallons and a halfe wine meafure makes a foote cubicall, it is eafie by inverfion, that knowing the quantitie of a veffell in Gallons, to finde his content in cubicall feete or weight: and that late famous Geometrician CMafer Brigs found a cubicall foote of mater to weigh neare 62 pound weight Haverdepoize. But the late learned Simon Stevin found a cubicall footc of water to weigh 65 pound, which difference may arife from the inequallitie of water; for fome waters are more ponderous than others; and fome difference meafure of a foote: thus the weight and yuantitie of a folid foote fettled, it is eafie for Arithmetitians to give the cantents of vefells or bon dies which containe liquids.
12. To finde the charge that a veffell may carry, as Sbippes, Boates, or fuck like.

THis is generally conceived, that a veffell may carry as much weight as that water weigieth, which is equall Lunto the veffell in bigneffe, in abating onely the weight of the vofo fell: we fee that a barrell of wine or water call into the water, will not finke to the bottome but fwimme eafily, and if a Shippe had not iron and other ponderofties in it, it might fwimme full of water without finking: in the fame manner ifthe veffell were loaden with lead, fo much thould the water weigh: hence it is that Marriners calls Shippes of so thoufand T Mnnes, becaufe they may containe one or two thoufand Tunne, and fo confequently carry as much.
13. How comes it that shippe baving fofely Sayled in the vafte Ocean, and being come in. to the Port or barkour, witbont any tempeft will finke domse right.

THe caufe of this is that a veffell may carry more upon fome kinde of water than upon other; now the water of the Sea is thicker and heavier than that of Rivers, Wells, or Fourtains;
herefore the loading of a veffell which is accounted fufficient in the Sea, becomes too great in the barbour or fweet water. Now fome thinke that it is the depth of the water that makes veffells more eafie to fwimme, but it is an abule; for if the loading of a shippe bee no heavier than the water that would occupie that place, the Ship fhould as eafily fwim upon that water, as if it did fwim upon a thourand fathom deepe of water; and if the water be no thicke than a leafe of paper, and weigheibbut an ounce under a heavy body, it will fupport it, as well as if the water under it weighed ten thoufand pound weight: hence it is if there be a veffell capable of a little more than a thoufand pound weight of water, you may put into this veffell a pecee of mood, which mall weigh a thouland pound weight; (but lighter in his kinde than the like of magnitude of water:) for then powring in but a quarte of water or a very little quantitic of water, the mood will fwimme on the rop of it, (provided that the wood touch not the fides of the veffell: ) which is a fine experiment, and feemes admirable in the pet formance.
14. How a groffebody of mettle may is is fwimose upon the water.

THis is done by extending the mettle Into a thinne Plate, to make it hollow in forme of a veffell; fo that the greatnefle of the veflell which the aire with it containeth, be equall to
the magnitude of the mater, which weighes as mach as it; for all bodies may fwimme without finking, if they occupie the place of water equall in weight unto them, as if it weighed 12 pound, it mult have the place of 12 pound of pater: hence it is that wee fee floating upon the mater great veffells of Copper or Brafle, when they are hollow in forme of a Chaldron. And how can it be otherwife conceived of $I$. lands in the Sea that fwimme and floate? is it not that they are hollow and fome part like unto a Boate, or that their earth is very light and fpongeous, or having many concavities in the body of it, or much wood within it.

And ic would bee a pretty propofition to thew how much every kinde of mettle fhould bee inlarged, to make it fwimme upon the man. ter: which deth depend upon the proportions that is betweene the weight of the water and each mettle. Now the proportion that is betweene mettles and water of equall magnitude, according to fome Authors is as followeth. A magnitude of 10 pound e Gould. $187 \frac{2}{2}$ weight of water will re-c. Silver. 104 guire for the like magni-6 Copper. 91 tude of

$$
\begin{aligned}
& \text { Iron. } 8 \mathrm{E} \\
& \text { Tinme. } 75
\end{aligned}
$$

From which is inferred, that to make a peece of Copper of 10 pound weight to fwimme, it muft bee fomade hollow, that it may hold 9 times that weight of mater and fomewhat more, that is to fay, 9 I pound: fecing that Cop-

## Mathematicall Recreation.

per and water of like magnitudes in their ponderofities, are as before, as IQ to 91.

## 15. How to eigh the lightweffef the aire.

PLace a Tallance of wood turned upfide downe into the water, that fo it may fwim, then let water be inclofed within fome body, as within a Bladder or fuch like; and fuppofe that fuch a quantitie of aire fhoald weigh one pound, place it under one of the Ballances, and place under the other as much weight of lightneffe as may counter-ballance and keepe the other Ballanse that itrife not out of the mater: by which you fhall fee how much the lightneffe is.

But without any Ballance doe this; take a Cubicall hollow veffell, or that which is Cylindricall, which may fwimme on the water, and as it finketh by placing of weights upon it, marke how much; for then if you would examine the weight of any body, you have nothing to doe but to put it into this veffell, and marke how deepe it finkes ; for fo many pound it weighes as the weights put in doth make it fo to finke.

## MathematicaßRecreation:

16. Being given a body, to warke it about, and Sow how much of it will finke in the water, or fuinsme above the water.

THis is done by knowing the weight of the body which is given, and the quantitie of water, which weighes as much as that body; for then certainely it will finke fo deepe, untill it occupieth the place of that quantitic of mater.
17. To finde how much feverall mettle or other bodies doe weigh leffe in the water than in the aire.

TAkea Bailance and weigh (as for example) 9 pound of Gould, Silver, Lead, or Stone in the aire, fo it hang in aquilibrio; then comming to che water, take the fame quantitie of Gould, Silzer, Lead, or Stone, and let it foftly downe into it, and you frall fee that you fhall neede a leffe counterpoife in the other Ballance to counter-ballance it: wherefore all folids or bodyes weich leffe in the water than in the aire, and fo much the leffe it will be, by how much the water is groffe and thicke, becaufe the weight findes a greater refiftance, and therefore the water fupports more than aire: and further, becaufe the mater by the ponderoftie is difpleafed, and fo ftrives to be there againe, preffing to it, by reafon of the other waters that are about it, according to the proportion of his

## Mathematical Recreation.

his weight. Alrbimedes demonltrateth, that all bodies weigh leffe in the water (or in like liguor) by how much they occupie place: and if the water weigh a pound weight, the magnitide in the water hall weigh a pound leffe than in the tire.

Now by knowing the proportion of water and mottles, it is found that Gould lofeth in the water the 19 part of his waight: Copper the 9 part, Quickefliver the 15 part, Lead the 12 part, Silver the so part, Iron the 8 part, Sine the 7 part and a little more: wherefore in materiall and absolute weight, Gould in refpect of the water that it occupieth weigheth 18 , and $\frac{3}{4}$ times heavier than the like quantitic of mater, that is, as $18 \frac{3}{4}$ to the 2 nickefilver 15 times: Dead II and $\frac{3}{5}$, silver 10 and $\frac{2}{3}$, Capper 9 and $\frac{1}{20}$, Iron 8 and $\frac{1}{2}$, and 7 ene 8 and $\frac{1}{2}$. Contrarily in reflect of greatneffe, if the water be as hemvy as the Gould, then is the mater almoft 19 times greater than the magnitude of the Gould, and fo may you judge of the, reft.
18. How is it that a ballance having like weighs in each fcale, and banging in equilibrio in the eire: being placed in another place, (without removing any weight) it Ball cease to bang in aquilibrio Sencibly: yeaby a great difference of weight.

His is eafie to berefolved by confidering
different mettles, which though they weigh

## Matbematicall Recreation.

weigh equall in the dire, yet in the water there will bee an apparant difference; as fuppofe fo that in the fcale of each Ballance be placed 18 pound weight of feverall mettles, the one Gowld and the other Copper, which being in aquilibrio in the aire, placed in the woater, will not hang fo, becaufe that the Gould lofeth neare the 18 part of his weight, which is about I pound, and the Copper loleth but his a part, which is 2 pound : wherefore the Gold in the water weigheth bue 17 pound, and the Copper 16 pound, which is a difference moft fencible to confirme that point.
> 19. To bew what waters are heavier one than another, and how much.

PHy fitians have an efpeciall refpect unto this, judging that water which is lighteft is moft healthfull and medicinall for the bedy; and Ses-men know that the heavieft waters doe beare moft, and it is knowne which water is heavieft thus. Take a peece of maxe and faften lead unto it, or fome fuch like thing that it may but precifely fwimme, for then it is e quall to the like magnitude of water; then put ic into another veffell which hath contrary water, and if it finke, then is that water lighter than the other : but if it finke not fo deepe, then it argueth the water to be heavier or more groffer than the firt mater; or one may take a peece of wood, and marke the quantitie of finking of it into feverall waters, by which you
may judge which is lightelt or heavieft, for in that which it finkes moit, that is infallibly the lighteft; and fo contrarity.
20. How to make a Pound inf water weigh as much as $10,20,30$, or bundred pound of Lead; nay as much as a thousand, or ten thoufand pound weight.

THis propofition feemes very impoffible, yet water inclofed in a veffell, being conftrained to dilate it felfe, do:h weigh to much as though there were in the concavitie of it a follid body of water.

There are many wayes to experiment this propofition, but to verifie it, it tnay be fuificient to produce two excellent ones cnely: which had they not beere really acted, little credit might have beenegiven unto it.
The firft way is thus: Take a Magnitude which takes up as much place as a bundred or a thoufand pound of water, \& fuppofe that it were tied to fome thing that it may hang in the aire; then make a Ballance that one of the fcales may inviron it, yet fo that it touch not the fides of it: but leave face enough for one pound of water: then having placed 100 pound weight in the other foale, throw in the water abour the CMugnitade, fo that one pound of mater fhall weigh downe the hundred pound in the otber Ballance.
The fecond way is yet more admirable: take 2. common Ballance that is capable to receive

10 or 20 pound of $m a-$ ter, then put into ita magnitade whichinay take up the place of 9 or 19 pound of mater, which malt bee bung at fome Iron or beanse which is placed in a wall; fo that it hang quiet: (now it is not materiall whether the magnitude be hollow or maifie) fo that it touch not the Ballance in which it is put: for then having put the lead or weight into the other Ballasce, powre in a pound of mater into the Ballance where the magnitude is, and you fhall fee that this one pound of water fhall counterpoife the 10 or 20 pound of lead which is fet in the other Ballance.

## Problem. LXXXVI.

## Of fundry Queftions of Arithmeticke, and firft of the number of fassds.

1T may be faid incontinent, that to undertake this were impoffible, either to number the fands of Libya, or the Sands of the Sea; and it was this that the Poets fung, and that which. the vulgar beleeves; nay, that which long agoe certaine Pbilofophers to Geloiz King of Sici-

## Mathemasicall Recreation?

Y:eported, that the graines of fand were innumerable: But I antwere with Archimedes, that not onely one may number thefe which are at the border and about the Sea; but thele which are able to fill the whole world: if there were nothing elfe but fand, and the graines of fands admitted so bee fo fimall, that 10 may make but one graine of Poppy: for at the end of the account there neede not to expreffe them, but this number 30840979456 , and 35 Ci phers at the end of it. Clavius and Archimedes makes if fomew hat more; becaufe they make a greater firmament chan Ticho Brabe doth; and if they augment the Vniverfe, it is eafie for us to augment the number, and declare affuredly how many graines of fand there is requifite to fill another world, in comparifon that our vifible world were but as one graine of fand, an atome or a point; for there is nothing to doe but to multiply the number by it felfe, which will amount to ninety places, whereof twenty are thefe, $95{ }^{1} 43798134910955936$, and 70 Ciphers at the end of it: which amounts to a moft prodigious number, and is cafily fupputated: for luppofing that a graine of Poppy dorb containe 10 graines of ford, there is nothing but to compare that little bowle of a graine of Poppy, with a bowle of an inch or of a foote, and that to be compared with that of the earth, and then that of the earth with that of the firmament; and fo of the reft.
2. Divers
2. Divers mettles being melted together in one body, to finde the mixture of then.

THis was a notable invention of Archimedes, related by Utriviou in his eArchitecture, where he reporteth that the Gould-- mith which King Hier imployed for the making of the Goulden Cromne, which was to be dedicated to the gods, had ftolen part of it and mixed Silver in the place of it : the King fufpicious of the worke propofed it to Archimedes, if by Art be could difcover without breaking of the Crowne, if there bad beene made mixture of any other mettle with the Gould. The way which he found out was by bathing himfelfe, for as hee entred into the veffell of water, (in which he bathed himfelfe) fo the water afcended or flew out over it, and as hee pulled out his body the water defcended: from which he gathered that if a Bowle of pure Gould, silver, or other mettle were call into a veffell of water, the mater proportionally according to the thing caft in would afcend; and fo by way of Arith. meticke the queftion lay open to bee refolved: who being fo intenfively taken with the invencion, leapes out of the Bath all naked, crying as a man tranfported, I have found, I have found, and fo difcovered it.

Now fome fay that he tooke two Maffes, the one of pure Gould, and the other of pure Silver, each equall to the weight of the Crowne, and therefore unequall in magnitude or greatneffe;
adthen knowing the feverall quantities of hraor which was anfwerable to the Crowne, and the feverall CMafes, he fubtilly ce liected, that the Crowne occupied more place within the water than the Malfe of Gould did: it appeared hat there was Silver or ot her mettle melt with is. Now by the rule of pofition; fuppole that ach of the three Mafies weighed 18 pound a pece, and that the Maffe of goisld did occupie the place of one pound of 2 aster, that of Silver a pound and a halfe, and the Crozure orse pound ind a quarter only:chen thus he might operate: the Maffe of Silver which weighed 18 pounds, aft into the water, did caft out halfe a pound of water more than the Maffe of Gould, which weighed 18 pound; and the Crowne whick weighed aifo 18 pound, being put into a weffelf full of water, threw out more water than the Maffe of Gold by a quarter of a pound, (becurf of mixt mettle which was in it:) theretore by the rule of proportion, if halfe a pound ot water (the exceffe) te anfiverable to 18 pound of silver, one quarter of a pound of excefle thall be anfwerable to 9 pound of Silver, and fo much was mixed in the Crowne.
Some judge the way to bee more facill by weighing the Crowne fift in the aire, then in the water ; in the aire it weighed 18 pound, and if it were pure Gould, in the mater it would weigh but 17 pound; if it were Copper it would weigh but 16 pound; but becaufe wee will ruppofe that Gould and Capper is mixed together, it will weigh leffe then if geand,
yet more than 16 pound, and that according to the proportion mixed: let it then be fuypofed that it weighed in the mater 16 pound and 3 whe, a quarters, then might one fay by proportion, if the laj the difference of one pound of lofle, (which is 1, of wh betweene 16 and 17 ) bee anfwerable to 18 , mpty, pound, to what thall one quarter of difference be anfwerable to, which is betweene 17 and I $6 \frac{3}{4}$, and it will be 4 pound and a halfe; and fo much Copper was mixed with the Gould.

Many men have delivered fundry wayes to refolve this propofition fince eArchimedes invention, and it were tedious to relate the diverlities.
Baptifa Benedictus amonglt his eAritbmeticall Theoremes, delivers his way thus: if a Maffe of Gold, of equall bigneffe to the Crowne did weigh 20 pound, and anotber of Silver at a capacitic or bigneffe ar pleafure, as fuppofe did weigh 12 pound, the Crosene or the mixt body would weigh more than the silzer, and lefler than the Gould; (uppofe it weighed 16 pound which is 4 pound lefle than the Gosld by 8 pound, then may one fay, if 8 pound of difference come from 12 pound of Silver, from whence comes 4 pound which will be 6 pound, and fo much sifver was mixed in it, 6.6 . larefo exfon 0 tmpty hall of liguc amner tor the whefull ave alil uly to 2 it of $v$ the 24 tonis im ing ther

## Mashematicall Recreation.

uppod 9 . Three men bousbt a quantitie of mine, each Id and Juid alike, and each mas to bave alike; it happeorion und at the laft partition that there wads 21 Barwhich rells, of which 7 were full, 7 halfe full, and eth, and thefe numbers $2,2,3$; or $3,3,1$, may ferve for direction, and fignifies that the fritiperfon ought to have 3 Barrells full, \& as many empty ones, and one which is halfe full; thiee thall have 7 veffels and 3 Barrels, and a halfe of liquor: and one of the other thall in like manner have as much, fo there will remaine for the third man I Barrell full, 5 which are halfe full, and I empty, and fo every one thall have alike both in veffells and wine. And generally to anfwere fuch queftions, divide the number of veffells by the number of perfons, and if the 2 notient be not an intire number, the queftion is impoffible ; but when it is an intire number, there mult be made as many parts as there are 3 perfons, feeing that each part is leffe than the halfe of the faid 2uotient: as dividing $2:$ by 3 there comes 7 for the 2 notient, which may be parted in thefe thre parts, $2,2,3$, of 3,3,1, each of which being leffe than halfe of 7 .

$P_{3}$<br>4. Thare

## Mathemstical Recrcation.

4. There is a Ladder which fands upright a. Afte, gainfe a wall of 10 foote bigh; the foot of it is law, pulled out 6 foote from the reall upon the Pavemert: bow much bath the top of the Ladder defeended.

He anfwere is, 2 foot; for by Pytharorm rule the fquare of $\mathcal{D}$ B, the Hypotenime is equall to the fquare of $D A 6$, and $A B 10$. Now if $D_{\text {e }}$ bee 6 fort, and $A B$ Io foot, the fquares are 36 and 100, which 36 taken from 100 refts 64 , whofe Rsote-quadrat is 8 ; fo the foot of the Ladder being now at $D$, the toppe will bee at $C, 2$ foote lower than it was when it was at 3.

## PROELBM. LXXXVII.

Witty Swits or debates botweene Cains and Seme prayec Which pronius, pon the forme of fowres; which bargai Geometriciass call Ifoperimoter, or C- juft as quall in circuit on compaffe.

MArvell not at it if I make the C Kathemana notigt having
longel tickes take place at the Barre, and If I fet fide: forth

## Masbematicall Recreation.

forth here Bartolew, who witneffeth of him. Felfe, that being then an ancient Doctor in the Law, he himfelfe tooke upon him to learne the dements and principles of Geometry, by which he might fet forth certaine Lawes touching the divifions of Fields, Waters, Ilasds, and other incident places: now this fhall be to shew is palfing by, that thefe fciences are profitable and behovefull for Indges, Connsellors, or fuch, to exphine many things ng oo. whick falles our in Lames to avoid ambiguities, contentions, and Cuits often.

## 1. Incident.

CAims had a field which was directly fquare, having 24 meafures in Circuit,' that was 6 oneach fide: Sempronius defiring to fit himfelfe, prayed Cains to change with him for a field which fhoald bee equivalent unto his; and the bargaine being concluded, he gave him for counterchange a peece of ground which had juft as much in circuit as his had; bur it was not fquare, yet 2nadrangular and Reltangled heving 9 nealures in lesgth for each of the two longent fides, and 3 in bredth for each thorter fide: Now Caius which was not the moft fub-
tilleft nor wifeft in the world excepted his bargaine at the firft, but after wards having conferred with a Land meafurer and Mathematitian, found that he was overreached in his bargaine, and that his field contained 36 íquare meafures, and the other field had but 27 meafures, (a thing eafie to be knowne by multiplying the length by the bredth:) Sempronius contefted with him in fuite of Law, and argued that figures which have equall Perimeter or circuit, are equall amongit thernielves : my field, faith he, hathequall circuit with yours, therefore it is equall unto it in quantitic. Now this was fufficient to delude a Indge which was ignorant in Geometricall proportions, but a Mathematician will eafily declare the deceit, being affured that figures which are Ifoperimeter, or equall in circxit, have not alwayes equall capacitie or quantitic: fecing that with the fame circuit, there may bee infinite figures made which thall be more and-more capable, by how much they have more Angles, equall fides, and approach nearer unto a circle, (which is the moft capableft figure of all,) becaufe that all his parts are extended one from another, and from the middle or Center as much as may be: Co we fee by an infallible rule of experience, that a fquare is more capable of quantitie than a Triangle of the fame circuit, and a Fentagone more than a fquare, and to of others, fo that they be regular figures that have their fides equall, otherwife there might be that a regulat Triangle, having 34 meafures in circuit might

## Matbermaticall Recreation.

 might have more capacitie than a rectangled Parallelogram which had alfo 24 meafures of circuit, as if it were II in length and $I$ in breadth, the cercuit is fill 24; yet the quantitic is but II: and if it had 6 every way, it gives the fame Perimeter, viz, 24. but a quantitic of $3^{6}$ as before.
## 2. Incident.

$C$Empronius having borrowed of Cains 2 facke of Corne, which was 6 foot high and 2 foote broad, and when there was queftion made to repay it, Sempronius gave Caius backe two fackes full of Corne, which had each of them 6 foot high and I foot broad: who beleeved that if the fackes were full hee was repaid, and it feemes to have an appearance of truth barely looked on. But it is mof evident in demonftration, that the two fackes of Corme paid by Sempronius to Cains, is but halfe of that one facke which he lent him: for a Cylinder or facke having one foot of diameter, and 6 foot of length, is but the 4 part of another Cylinder, whofe length is 6 foot, and his diameter is 2 foot: therefore two of the leffer Cylinders or fackes is but halfe of the greater; and fo Crius was deceived in halte his Corne.

> 3. Incident.

SoOme one from a common Eountaine of a Citie hath a Pipe of water of au inch diame.

## 218 Mathematicall Recreation.

 ter; to have it more commodious, he hath leave to take as much more water, whereupon hee gives order that a Tipe be made of two inches diameter. Now you will lay prefently that it is reafon to bee fo bigge, to have juft twice as much mater as he had before: but if the CMbgiftrate of the Citic underttood Geometricall proportions, hee would foone caufe it to bee amended, and fhew that hee hath not onely taken twice as much water as hee had before, but foure times afmuch;for a Circular hole which is twe inches diameter is foure times greater than that of one inch; and therit? fore will caft out foure times afmuch witerids: that of one inch, and fo the deceit is double tico in this.Moreover if there were a heape of Corne of 20 foot every way, which was borrowed to be paid next yeare: the party having his Corne in heapes of 12 foote every way, and of 10 foote every way, proffers him 4 heapes of the greater, or 7 heapes of the leffer, for his owne heape of 20 every way, which was lent: here it feemes that the proffer is faire, nay with advantage, yet the loffe would be neare 1000 foot. Infinite of fuch caufes doe arife from Geometricall figures, which are able to deceive a Indge or Magiftrate,

## Matbematical Recreation.

Magiftrate, which is not fomewhat feene in Mathematicall Docmments.

## PROBLEM. LXXXVIII.

## Containing fundry Quefions in matter of Cofmography.

FIrft, it may be demanded, where is the middle of the world; I feake not here Mathematically, but as the vulgar people who aske where is the middle of the world: in this fence to feeake abfolutely there is no point which may be faid to be the middle of the furface; for the middle of a Globe is every where: notwithflanding the Holy Scriptares fpeaketh refpetively, and makes mention of the middle of the earth, and the interpreters apply it to the Citie of Ierufalem placed in the middle of $P A$ lefina, and the habitable world; that in effect taking a mappe of the world, and placing one foot of the Compafos upor Ierufalem, and extending the other foot to the extremity of Ewrope, eAfia, ande 1 frica; you fhall fee that the Citie of Ierufalem is as a Center to that Circle.
2. Secondly, bow much is the depth of the earth, thie height of the beavens, and the compafe of the world.

FFom the furface of the earth unto the Center according to ancieat traditions, is 3436 miles,
miles, fo the whole thickeneffe is 6872 miles, of which the whole compafie or circuit of the earth is 21600 miles.

From the Center of the earth to the Moone there is neare 56 Semidiameters of the earth, which is about 192416 miles: unto the Sunne there is 1142 Semidiameters of the earth, that is in miles 39249 12; from che ftarry firmament to the Center of the earth there is 14000 Semi. diameters, that is, 48184000 miles, according to the opinion and oblervation of that learaed TichoBrahe.

From thefe meafures one may collect by $A$ rithmeticall fupputations, many pleafant propofitions in this manner.

Firf, if you imagine there were a hole through the earth, and that a milfoxe fhould bee let fall dowse into this hole, and to move a mile in each minute of time, it would be more than two dayes and a halfe before it would come to the Center, and being there it would hang in the aire.

Secondly, if a man fhould goe every day 20 miles, it would bee three yeares wantugg but a fortnight, before he could goe once about the earth; and if a Bird thould fly round about it in two dayes, then muft the motion be 450 miles in an houre.

Thirdly, the choone runnes a greater compaffe each houre, than if in the fame time haee fhould runne twice the Circumference of the whole earth.

Fourthly, admit it bee fuppofed that one

## Mashematicall Recreation.

thould goe 20 miles in afcending upwards the heavens every day, hee fhopld bee above is yeares before hee could attaine to the Orbe of the cMoone.

- Fifthly, the Sunne makes a greater way in one day than the CWoone doth in 20 dayes, becaufe that the Orbe of the Sumes circumference is at the leaft 20 times greater than the Orbe of the Moone.
Sixthly, if a milfone fhould defcend from the place of the Sunne a thoufand miles every houre, (which is above 15 miles in a minute, farre beyond the proportion of motion) it would be above 163 dayes before it would fali downe to the earth.

Seventhly, the Sumne in his proper fohcare moves more than feven thoufand five hundred and feventy miles in one minute of time: now there is no Builtot of Cannon, Arrow, Thannderbolt, or tempelf of winde that moves with fuch quick eneffe.

Eighthly, it is of a farse higher nature to confider the exceeding and unmoveable quickmeffe of the ftarry firmament, for a farre being in the Equator, (which is juft betweene the Poles of the world ) makes 12598666 miles in one houre, which is two busdred, nine thoufand sine busdred and ninety foure wiles in one minure of time: \& if a Horfeman fhould ride every day 40 mailes, hee could tet ride fuch a compaffe in a thoufand yeares as the farrygitmery ment moves in one houre, which is more than if one chould gove about the earth a thouland
times in one houre, and quicker than poffible thought can be imagined: and if a farre fhould fly in the aire abour the earth with fuch a prodigious quickenefle, it would burne and confume all the morld here below. Behold therefore how time paffert and death haffeth on: this made Copernicus, not unadvifedly to attribate this motion of Primum mobile to the earth, and not to the farry firmament: for it is beyond humaine fence to apprehend or conceive the rapture and violence of chat motion being quicker than thought; and the word of God teftifieth that the Lord made all things in namber, menfure, weight, and time.

## Pronlem. LXXXXII.

To finde the Bifcextile yeare, the Dominicall letter, and the letters of the moneth.

LEt 123 ,or 124 ,or 185 ,or 26 ,or 27 , (which is the remainder of 1500, or 1600 ) be divided by 4 , which is the number of the Leapeyeare, and that which remaines of the divifion Thewes the Leape yeare; as if one remaine, it Thewes that it is the firftyeare fince the Bifex. tile or Leape yeare: if two, it is the fecond jeare, of $f_{6}$ and if nothing remaine, then it is the BifSextile or Leape yeare; and the Quotient flewes you how many Biffexeriles or Leapr yeares there are contained in fo many yeares.

## Mashematicall Recreasion.

## To finde the Circle of the Sunby the $\beta$ angers.

LEt $123,34,25,26$, or 27 , bee divided by 28, (which is the Circle of the Sanne, or whole sevolution of the Dominicall letters) and that which remaines is the number of joynts, which is to bee accounted upon the fingers by Filius effo Dei, calum bonus accipe gratis: and where the number ends, that finger it fheweth the yeare which is prefent, and the words of the verfe fhewes the Dominicall letter.

> Example,

DIvide 123 by 28 for the yeare, (and fo of other yeares) and the Quotient is 4 ,and there remaineth 11 , for which you muit account It words; Filisu efto $\mathcal{D}_{\text {e }}$, ơr. upon the joynts beginning from the firft joynt of the Index, and you fhall have the anfwere.

For the prefent to know the Deminicall letter for each moneth, account from Ianuary unto the moneth required, including Ianuary; and if there bee $8,9,7$, or 5 , you mult begin upon the end of the finger from the thumbe and account, Adam degebat, dec. as many words as there are soneths, for then one foall have the letter which begias the moneth; then to know what day of the moneth it is, fee how many times 7 is comprehended in the number of dayes, and take the reft: fuppofe 4.2 ccount upon the firt finger within and without by the joynts
unto the number of 4 , which ends at the end of the finger: from whence it may bee inferred that the day required was Wedne $\mathrm{S}_{\mathrm{d}}$ ay, Sunday being attributed to the firft joynt of the firtt finger or Index: and fo you have the prefent yeare, the Dominicall letter, the letter which begins the Moneth, and all the dayes of the Moneth.

## Problem. LXXXXIIT.

## T'o finde the New and Fall CMoone in each Moneth.

ADde to the Epact for the yeare, the Moneth from March; then fubrract that furplus from 30, and the reß is the day of the Moneth that it will bee New Moone, and adding unto it ${ }^{4} 4$, you thall have that Fwll Moone.

## Note.

THat the Epalt is made alwayes by adding It unto 30, aad if it paffe 30 , fubtract 30 , and adde II to the remainder: and fo ad infinitwm: as if he $\varepsilon$ pact were 12 , adde 11 to it makes 23 for the Epact, next yeare, to which adde 11 makes 34 ; fubtract 30 , refts 4: the Epset for the yeare after, and is for the yeare following that, and for the next, and 7 for the next, \&cc.


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03/ty
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# Masbematicall Recreation. <br> Prodiem. LXXXXIIII. 

To finde the Latitwide of a Conntrey.

THefe that duell betweene the North Pcle and the Trepicke of Cancer, have their Jpring and /smmer betweene the 10 . of $M$ arch, and the 13 .of $S \mathrm{fptember}$ : and therefore in any day betweene that time, get the funnes diftance by influmentall obfervation from the zeniinat nioone, and adde theideclination of the $\int$ sune for that day te is : fo the Aggragate, or fuch is the Latitwde, or Poles beight of that Countrey. Now the declination of the funve for any day is found out by Tables calculated to that end: or Mechavically by the Glebe, or by Inftrament it may be indifferently had : and here notethat if tha day be betweene the 13 . of Septumber and the io. of March, then the Sunnes declination, for that day must be taken out of the ditance of the funne from the zexith at noone': fo Chall you have the Latitude, as before.

## proeiew. LXXXXV.

Of the Climats of countries, and so finde in what Climate any conntrey is under.
Cimats as they are taken Geographically (f)

## Mathematicall Recreation.

of the longelt day of any piace, is halfe an houre longer, or fhorter than it is in another place (and 10 of the fhortell day) and this account to beginfrom the Equinoctiall Circle, feeing all Comatries under it have the Chorteft and longelt day that can bee but 12 . bowes; But all orher Cowneriss that are from the EquinoEtiall Circle cither towards the North or Soxth of it unto the $P$ oles themfelves, are fayd to bee in fome one Climate or other, from the Equinoetia!! to either of the poles Circles, (which are in the Latitude of $66 . \mathrm{gr} \cdot 30 . \mathrm{m}$.) betweene eacs of which poler Circles and the Equinottiall Circle shere is accounted 24 Climats, which siffer one from another by halfe an bours time: then from each Poler Circle, to each Pole there are reckoned 6 .other Climats which differ one from arother by a months time :fo the whole earth is divided into 60 . Climats, 30 being allotted to the Northerne Hemiipheare, and 30. to the Southerne fiemijpheare. And here notethat though thefe Climats which are betweene the EquinoETiall \& the poller Circles are equall one unto the other in refpect of time, to wit, by halfean boure, yet the Latitude, breadth, or intersall, contained betweene Climate and Climite, is not eguall : \& by how much any Clim mate is farther from the Equinoctiall than another Climate, by fo much the leffer is the internall berweene that Climate and the next: fo thefe that are neareft the Equinoctial are largeft; and thefe $w^{\text {ch }}$ are fartheft off moft contracted: Is to find what Climate any Conntrey is under:

## Mathemasicall Recreation?

fubtrait the length of an Equinoctiall day io wit, 12 , boures from thelength of the longef day of that (ountriy; the remander being doubled fletwes the (fimate: So at London the longett day is neare 16. howres and a half; ;12. taken from it there semaines 4. boures and a halfe which doubled wakes $s$. baife hosres, that is, 9 . Climats; fo London is in the g.Climate.

## ProbiEm. IXXXXVI.

> Of Longitude and Latitude of the Earth and of she Stertes.

1Ongitride of a Countrey, or place, is an arcke Lof the eEquator contained betweene the Meridian of the Azoros, and the Meridian of the place; and the greateft Liongituse that car be is 360 degrees.

> Note.

That the firf Meridinn may betakea at pleafure upon the Terieftriall Glabe or Mappe, forthat fome of the ancient e $1 / 2$ onomers would have it at Hercules Pillars, which is at the fraighis at Gibralter: Ftolomy placed it at the (anay Iland, but now in thefe latiter times it is held to bee neare the Azores. But why it was firft placed by Ptolomy at the Canary Ilands, was becaule that in his time thefe Ilands were the fartheft welterne parts of the world that wasthen difcovered: And why it retaines his place now at Saint cMichels neare the

$$
02 \text { Azores }
$$ Azores, is that becaufe of many accurate obfervations made of late by many expert Nnvigator sand Mathomaticians, they have found the Needle there to have no variation, but to poine North and South: that, is to each Pole of the - world : and why the Lonfitude from thence is accourted Eaftiwards, is from the motion of the Sunne Eaffward; or that Ptolomy and others did hould it more cenvenient to teg in from the mefferse part of the world and fo account the Longitude Eafferard from Conntrey to Coxntrey that was then knowne; till they came to the Eafterne part of $\mathcal{A}$ Fa, rather than to make a begiuning upon that which was nuknowne: and having made up their account of reckoning the Lorgitude from the Wefferne part to the $E A$. flerne part of the world knowne, they fuppofed the reft to be all fea; which fince their deaths hath beene found almoft to be another habitable world.

## Tofnde the Longitixde of a Coustry.

IF it be upon the Globe, bring the Coxatrey to the Brafen Meridian, and whatfoever degree that Meridian cuts in the Egsino CTisII, that degree is the Longitude of that Place: if it be in a. Mappe, then marke what CMeridian pafferh over it; fo have you the Longisude thereof: if no Meridian paffe over it, then take a paire of Compatjes, and meafure the diffance berweenc the Placeand she pext Moridian, and tply it

## Matbematicall Recreation.

to the divided parallel or efquator; fo have you the Longitude required.

## Of the Latitude of Conatries.

LAtirnde of a Cosntrey is the diffance of a Conntrey from the Equinoctiall, or it is an Arke of the Meridian contained betweene the Zenith of the place and the Equator; which is twofold, viz. either North Latitude or South Latitude, eyther of which extenderh from the Equinoctiall to eyther Pole; fo the greateft Latitude that can be is but go. degrees: If any Northerne Cenntrey have the Articke Circle verticall, which is in the Latitude of $66 . \mathrm{gr} \cdot 3$ e.m.the $\int$ nnne will touch the Horizon in the North part thereof, and the longeft day will be there then 24 . houres: if the Countrey have leffe Latitude tham 66 . degrees 3 0.m. the funne will rife and fet; but if it have more Latitrude than $66 . \mathrm{gr} .30, \mathrm{~m}$, it will bee vifible for many dayes: and if the Cosntrey bee under the Pole, the funne will make a Circulak motion above the Earth and be vifible for a halfe yeare: Counder the Pole there will bebut one day, and ane right in the wholeyeare.

## Matbematicall Recreation.

## To finde the Latitude of Countries.

Fit be upon a Globe, bring the place to the Brafen Meridiar, and the number of degrees a hich it mecteth therewith, the Lat:tude of place. Or witha pairc of Compafestake the diftance betweene the
Countrey and the $E_{-}$ quiractiall, whichapplyed untothe Eguinactiall will thew the Lam titude of that Countrey; which is equall to the Poles height; if it te upon a CMappe. Then marke what parallel paffech over the Countrey and where it croffeth the CMeridian, that hall be the Latitude : but if no parallel paffeth over it, then take the diftance betweene the place and the next paralleil, which applyed to the divided CMeridian from that parallell will thew the Latitude of that place.

## To finde the diffance of Places.

1Fitbe upon a Globe : then' with a paire off Compaffes take the diftance betweene the two places, and apply it to the divided Meridian or e $\neq$ quator, andthe number of degrees fhall thew the diftance; each degree becing 601 miles,
miles. If it be in a Mappe (according to Wrights projection) take the diftance with a parte of Compaffes betweene the twn places, and apply this diftance to the divided Meridian on the Mappe right againit the two places; foas many degrees as is contained betweene the feete of the Compafles, fo much is the diftance betweene the two places. If the diftance of two places be required in a particular CMappe then with the Compafes take the diftance betweene the two places, and apply it to the fcale of Miles, fo have you the diftance: if the fale bee too Churt, take she fale betweene the Compafes, and apply that to the two Places as often as you can, to have you the diftance required.

## Of the Longitude, Latitude, Declinatio on, and diftance of tbe Starres.

THe Declixation of a farre is the neareft diftance of a farre from the e Equator; the Latitude of a flarre is the nearelt diftance of a farrefrom the Eclipticke: the Losgitude of a farre is an Arke of the Eclipticke contained betweene the beginning of Aries, and the Cir cle of the farres Latitnde, which is a Circle drawne from the Pole of the Ecliptick unto the farre, and fo to the Eclipticke. The diftance betweene two farres in heaven is caken by a Crofieftaffe or other Inftrument, and upon a Globe it is done by takingbetweene the feet of the Compaffes the two ffarres, and applying it tweene thole two farres.

> How it is that two Horfes or other creatures being foled or brought forth into the world at one and the fame time, that after certaine diayes travell the one lived longer then the sther, notwithftanding they dyed togather in ome and the fansemo- mext alfo.

THis is cafie to be anfwered ; let one of them travell towarde the Weft and the other towards the Eaft : then that which goes towards the Weft followeth the Sunne : Thall have the day fomewhat longer than if there had beene notravell made : and that which goes Eaft by going againft the Sunne, thall have the day fhorter: and fo refpect of travell though they dye at one and the fel fe fame houre and moment of time, the one fhall be older than the other.
From which confideration may be inferred that a Chriftian, a Iew, and a Zarazen, may have their Sabbaths all upon one and the fame day, though notwithitanding the Zarazen houlds his Sabathupon the Friday, the Iew upon the Saturday, and the Chrittian upon the Sonday: For being all threerefident in one place, if the Zarazen and the Chriftian begin their travell upon the Saturdiy, the Chititian going Weft: zand the Zarazen Eaftwards, fhall compaffe the

## Mathematicall Recreation.

G-obe of the earth, the Chriftian at the conclufron fhall gaine a day and the Zarazen fhall lofe a day, and fo meete with the Iew every one upon his owne Sabbath.

## Certaise fine Obfervations.

VNer the Equino iall the Needle hangs in aquilibrio, but in thefe parts it inclines under the Herizer, and being under the $P$ ole it is thought it will hang verticall.

In thefe Conntries which are without the Tropicall Circles, the Sunne comes Eaf and Weft every day for a halfe yeare; but being under the Equinoftiall the Smane is mever $\varepsilon_{a f}$, nor Weft but twice in the yeare, to wit, the 10 . of March and the 13 . of September.
If f Jippe be in the Latitude of $23 . \mathrm{gr} .30 . \mathrm{m}$. that is, if it have eyther of the Tropickes verticall : then at what time the Sunnes Altitude is equall :o his diftance from any of the Equinostiall points, then the Swane is due Eaff $^{2}$ or Wef.
If a Bippe be betweene the Equinoltiall and eyther of the Tropicks, the Sumne will come twice to one point of the Compafe in the forenoone, that is, in one and the fame pofition.
Vnder the Equinof iall neare Guinea there is but two forts of windsall the yeare, 6. months a Northerly winde, and 6. months a Sowtherly wisde, and the flux of the Sea is accordingly.
If two Ships under the Equinogiall be Iö0. lengwes afunder, and fhould fayle Northerly
untill they were come under the Articke Circle? they forould then be but 50. leagues afunder.

Thele which have thee Articke Circle verticall : whenthe Sume is in the Tropicke of Cane cer: the Sunue fetteth not but toucheth the wefterne part of the Horizon.
If the complement of the Ssunes beight at noone be found equall to the Suns Declination for that day, then the Equinodiall is verticall:or a fippe making fuch an obfervation, the Equinoctiall is in the Zenith or direct over them: by which Navigators know when they croffe the line, in their travels te the Indies, or other parts.

The Sunne being in the Equinoctiall, the extremity of the ftill in any Sunne dyall upona plane; maketh a right line, otherwife it is Elip. ticall, Hyperbolicall, ctc.

When the fhadow of a man, or öther thing upon a Florizontall plaine is equall unto it in length, then is the Sunne in the middle point betweene the Horizon and the Zenith, that is, 45 .degrees high.

Probleme LXXXXVII: -
To make a Triangle that Ball bave tbree right eAngles.

O
Penthe Compafes ar pleafure : and upon $A$, defcribe an Arke BC. then at the fame opening, place one of the feet in $B$, and defcribe

## Mathematicall Recre ation.

fcribe the Arke AC. Laftly, place one of the feet of the Compafes in $C$. and defribe the Arke $A \mathcal{B}$. fo fhall you have the Pphericall exqxilaterall Triangle $A B C$. right angled at $A$, at
 $B$, and at $C$. that is, each angle comprehended 90. degrees:
which can never be in any plaine Triangle, whether it be Equilaterall, Ifocelle, fcaleve, Orthogonall, or Opigonall.

## Proelem. LXXXXVIII.

To divide a line in as many equall parts as one will, without compaffes, or without feeing of it.

THis Propofition hath a fallacie in. is, and cannot be practifed but upon a Maincordion: for the Mathematicall line which proceedes from the flux of a point, cannot be divided in that wife : One may have therefore an Inftrument which is called Maincordion, becaufe there is but one cord : and if you defire to divide your line into 3 . parts, run your finger upon the frets untill you fourd a third in muficke: if you would have the fourth part of the line, then

23 Mathematicall Recreation.
then finde the fourth found a fif, \&cc. fo gall you have the anfwer.

## Preziex. LXXXXVIIII.

## Todraw a line which foall incline to another like, yet never meete: againft the Axiome of Parallels.

THis is done by helpe of a Conoyde line, produced by a right line upon one and the fame plaine, held in great account amongt the Ancients, and it is drawne after this manner.
Draw a right line infinitely, and upenfome end of it, as at $I$, draw a perpendicular lime Ie A. augment itto $H$. then fró $A$. draw lines at pleafure to interfect the line $I . M$. in each of which lines from the right line, I. M: transferre ${ }^{1} \mathrm{H}_{\mathrm{H}}$. viz.
 KB.LC.OD. $\mathrm{T}_{\mathrm{E}}$. 2F.MG. then from thofe points draw the Ine H.B.C.D.E. F. E. which will not meet with the line $I M$. and yet incline nearer and meareruato it.
my isof is fro fath

# Mathemasicall Recreation. 

## Problem. Co

> To obferve the variation of the compayfes, or seedle in anyplaces.

FIrft defrribe a Circle upon a plaine, fo that the Sumne may fhine on it both before noone and afternoone $:$ in the center of which Circle place a Gnomon or wire prependicular as $A T$. aud an houre before noone marke the extremitie of the fhaddow of $\mathscr{A} B$. which fuppofe it be at $C$.defcribe a Circle at that femidiameter CDF then after noone marke when the top of the fodew of \& B. toucheth the C3rcle, which admit in $D$; devide the diftance $C D$, inte two equall parts which fuppofe at $E$. draw the line $E \& F$, which is the Meridian line, or line of North \& South : now if the Arke of the Circle CD. beedevided into degrees: place a Keedle GH, upon a plaine fet up in the Center, 2 marke how many degrees
 the point of the Needie $G$, is from $E$. fo much doth the Nerdie vary from the Narth in thát place.
PROBLEM, CI.

How to finde at any time which way the wind is in ones Chamber, witlsout going abroad.

vVon the Planching or floore of a Chamber, Parlor, or Hall, that you intend to have this devife, let there come downe from the top of the boufe a hollow poit, in which place an Iron rod shat it afceid above the boufe 10, or 6 . foote with a vane or a foumben at it to flew the minds with. out : and atthe lower end of this rod of Iron, place a Dart which may by the mooving of the vane with the winde without, turse this Dart which is within : aabout which upon the plaitter muft be defcribed a Circle divided into the 32 .points of the cMariners Compafe pointed and diftinguifhed to that end? then may it be marked by placing a Compaffe by it; for having noted the North poist, the Eaft, orc. it is eafieto note all the reft of the points: and foat any time comming into this Reome, you have nothing to doe but to looke up to the Dart, which will point you out what way the winde bloweth at that inftant.

Pro.

## Mathematicall Recreation.

PROBLEM. CII:

How to draw a parallell phericall line with great eafe.

FIrtt draw an obfcureline $G F$. in the middle of it make two points $A B$, (which ferves for Centers) then place one foore of the $\mathrm{C}_{\text {om- }}$ pafes in $B$, and extend the other foote to $A$, and defcribe the femicircle $A C$ : then place one foot of the Compalfes in $A$, and extend the other foote to $C$, and defribe the femicircle $C D$. Now place the Compaffes in $B$, and extend the other foote unto $\mathcal{D}$, and defcribe the Semicircle D $E$, and fo ad info. nitum, which being done neatly, that there bee no right line feene nor where the Compafes were placed, will feeme very irange
 how poffibly it could bee drawne with fuch exaetnes, to fuch which are ignorant of that Way:

Probiem. CIII.

To mealur an inacce fible diftumce: at the bredib of a River with the helps of oneshat onely.

THe way of this is cafie, for having ones hat upon his head, come neare to the banke of the River, and heulding your head upright (which may bee by puttting a fmall fticke to Come one of your buttons to prop up the chin) plucke downe the brim or edge of your hat untill you may but fee the other fide of the water; then turne about the body in the fame pofture that it was before, towards fome plaine, and marke where the fight by the brimane of the bat glaunceth on the ground; for the difance from that place to your flanding, is the bredrh of the River required.

## Probiek. CIIII.

How to measure a beight with two frawesor troo fmall fickes.

TAke two firawes or two fickes which are one as long as another, and place them at sight Angles one to the ather, as $\boldsymbol{A 2}$, and $A C$. then houlding $A B$. parallel to the ground, place the end $A$. to the eye at $A$, and looking to the other top $B$ Cat C.by going backwatd or forward

## Mathematicall Recreation?

ward untill you may fee the top of the Tower or Tree, which appose at $\varepsilon$. So the diftance from your fading to the Tow or or Tree, is equal to the height thereof above the level of the eye : to which if you add your one. height you have the whole height.

## Othermifa.

TAle an ordinary fquare wi Carpenters or other workmen ufo, as $H$ $K L$ and placing $H$. to the eye fo that $H$ K. be levelly, goo back or come nearer untill
 that by it you may fee the top M. for then the diftance from you to the height is squall to the height.

## Mathematicall Recreation.

## 

How to make fatues, letters, bowles, or other things which are placed in the fide of a bigh building, to be feene below of an equall bigne fle.

LEt B C. be a Pillar 27. yards high, andlet it be required that three yards above the levell of the ege $A$, vizat $B$. bee placed a Globe and 9 yards above B.be placed another, and 32. yards above that be placed another Globe: how much thall the Diamiter of there Globes be, that at the eye, at ©A, they may all appeare to be of one and the fame Magmude: It is thus done, firft draw a line as $A K$.\& upon $K$. erect a prependicular
 $K X$.divide this line into 27 . parts, and according to $A$ K. defcribe an Arke $K$ r.then from $K$. in the perpendicular $K X$,account 3 -parts.viz. at $L$, which fhall reprefent the former three yardes, and draw the line $L A:$ from $L$, in the fayd perpendicular reckon the diamiter of the leffer Globe of what Magnitude it is intended to be: fuppofe $S L$. and draw the line $S$. cutcing the Arke $V$ $K$.in $2 \mathbb{V}$. then from $K$. in the perpendicularaccount 9.9 ards, which admitat T. draw $T$ A.cutting $T \mathcal{K}_{\text {.in }}$ O.transferre the Arke $M 2 \mathcal{L}_{2}$ from

A to P.and draw $A P$. which will cut the perpendicular in $V$ : fo a line drawne from the middie of $V F$. unto the vifuall lines $A T$, and $A V$, thall be the diamiter of the next Globe : Laftly, account from $K$. in the perpendicular $X K, 22$ parts, and draw the line $W$ A.cutting $Y K$, in 2, then take the Arke $M N$, and transferre it from 2,to R.and draw $A$. .which will cut the perpendicular in $X$. fo the line which paffeth by the middle of $X W$. perpendicular to the vifuall line $A W$, and $A X$. be the Diamiter of the third Globe, to wit 5,6 . which meafures transferred in the pillar $B C$. which theweth the true CMag. situde of the Globes 1,2, 2. fro $n$ this an Architecter doth proportion his Images, and the foulding of the Robes which are molt deformed at the ey below in the making, yet mont perfect when it is fetin his true height above the eye.

Problem. CVI.
How to difguife or disfigure an Insage, as a head, anarme, a whole body, đre. So that it bath no proportion, the eares rabecome long:the nofe as that of a froan, the mouth as a coaches entrance, c.yet the
eye placed at certaine
point will be feene in
a direEt and exall
proportion.

TWill not ftrive to fet a Geometricall fgure lhere for feare it may feeme too difficultto unR 2 derftand,

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 Mathematicall Recreation.derftand, but I will indeavour by difcourfe how Mechanically with a Casdle you may perceive it fencible : firft there muft be made a figure upon Paper luch as you pleafe, according to his juft proportion, and paint it as 2 Pitture (which painters know well enough to doe) afterwards put a Candle upon the Table, and interpofe this figure obliquely, betweene the faid Caxdle and the Bookes of Paper, where you defireto have the figure difguifed in fuch fort that the height paffe athwart the hole of the Pitture : then will it carry all the forme of the $P_{i t}$ thre upon the Paper, but with deformity ; follow thefe trats and marke out the light with a Coles blacke boad or Inke: and you have your defire.

To finde now the point where the eye mult fee it in his naturall forme : it is accuftomed according to the order of Perpective, to place this point in the line drawne in height. equall to the largenefleof the narroweft fide of the deformed fquare, and it is by this way that it is performed.

> Рковцем. CVII.

How d Canon after that it bath Sot ; ; may be covered froms the battery of the enemy.

LEt the mouth of a Canon be I. the Caxon $M$.his charge $N O$. the whecle L. the axletree P $B$. upon which the Canon is placed, at which

## Mashematricall Recreation:

whichend towards $B$, is placed a pillar $A E$. fupported with props $D C . E_{2} F_{2} G_{0}$ about which the Axeltreef turneth: now the Cannon being to fhoot, it retires to $H$. which cannot be directly becaule of the efreltree. but it make a fegmé: of a Circle, \& hides him-
 relfe behind the rall $2 R$, and fo preterves it celfe from the $E$ mjmies battery, by which meanes one may avoyd many inconveniences which might arife : and moreover one man may more eafily replace it againe for another thot by helpe of poles tyed to the wall, or other helpes which may multiply the ftrength.

## problem. CVIII.

How to make a Lever by which one man may. alone place a Cannon upombiscarriage, or kaife what other meight be roould.

FIrft place two thicke boards upright, as the figure fheweth, pierced with holes, alike oppofite one umto another as $C \mathcal{D}$, and $E F$ :and let $L$, and $M$, be the two barrs of Iron which palfeth through the holes $G H$, and $F, K$; the

$$
\mathrm{R}_{3} \quad \text { TwO }
$$ props, AB.the Cannon, $O \mathcal{P}$, the Lever $R S$, the two notches in the Lever, and $Q$, the booke where the burthen or Cannon is tyed to. The reltiof the operation is facill, that

 the young eff fchollers or learners cannot faile to performe it : toteach Minerva were in vaine, and it were teraw Clathematicians injury in the fucceedin! ine Ages.

PROBдEM.CIX.

How to make Clocke with one onely wheele.

MAke the body of an ordinary Dyall, and divide the houre in the Circle into 12. parts: make a great whecle in height above the $A x-$ eleree, to the which you thall place the cord of your counterpoife, fo that it may defcend, that in $\mathrm{I}_{2}$


## Mashemasicall Recreation.

boures of time your Index or Needle may make one revolution, which may bee knowne by a watch which you may have by you: then put a balence which may ftop the courfe of the wheelf, and give it a regular motion, and you Thall fee an effect as juft from this as froma Clocke with many wheeies.

## Problem, CX.

How by belpe of two wheeles to make a Cbild todraw up alone a bogshead of water at a time: and being dratuse up foall raffout it felfe into another
veffell as one would bave it.

1Et $R$ beche $P$ it from whence water is to be drawne; $P$, the booke to throw out the water whin it is brought up (this booke mult be moveable) let $\mathcal{A} B$, beethe $\mathscr{A} x$ xis of the wheelf S $F$, which wheele hath divers forkes of Iron made at $G$, equally fattened at the wheele; let $I$, bea Card, which is drawne by $K$, to make the wheele $S$, to turne, which whoele $S$, beares proportion to the wheele T, as 8 to 2: let N be a Chaine of Iron to which is tyed the veffell 0 : and the other which is in the Pit: E F is a peece of mood which hath a mortes in 1 , and 2 , by which the Cord I, pafleth, tyed at the wall, as K H, and the other peece of Timber of the litsle wheele as $M$, mortiled in likewife for the
$R_{4}$
chaine to paffe through draw the Cord I, by $\mathcal{K}$, and the mbeele will turne, and fo confequently the mbeele $T$, which will caufe the veffell $O$, to raife: which being empty, draw the Cord againe by $r$, and the other vefell which is in the pit will come out by the fame reafon. This is aninvention which wil ilill by fave labour if practifed; but here is to be noted that the pit mult be large enough, to the end ${ }^{\text {m }}$ that it containe two great veffels to paffe up and downe one by another.

## Probigm, CXI.

To make a Ladder of Cords which may be carryed in ones pocket: by which one may eafly moust up a Wall, or Trecalone.

TAke two Pullies $A$, and $D$, unto that of $A$, let there be faftned a Crampe of Iros as B; and at $\mathcal{D}$, letthere be faftned a faffe of a foote $3 x$ a halfe long as $F$, then the Pully $A$ :place a hand of Iron,as $\varepsilon$, to which tie a Cord of an halfe inch thich e (which may be of filkebecaufe it is for the pocket:) shen arive to make faft the

## Mathematicall Recreation.

Rully $\mathcal{C}$, by the helpe of the Crampe of Iron $\mathcal{B}$, to the place that you intend to fcale; and the Aaffe $F$, beiog tyed at the Pully D, put it betweene your legges as though you would fit upon it : then houlding the Cord $C$, in your hand, you may guide your felfe tothe
 place required : which may be made more facill by the multiplying of Pullies. This fecret is inof excellent in $W$ arre, and for lover $S_{9}$ its fupportablenefle avoyds fufpition.

## Problem. CXII.

How to make a Pumpe mbofe frength is warued lous by reaf on of the great weight of water that it is able to bring ap at once, and So by conm
t172HARTCO.
IEt $\alpha \beta \gamma \delta$, be the height of the $C a f e$ about two or three foote high, and broader according to difcretion : the reft of the Cafe or concavity let be $O$ : let the fucker of the Pumpe which is made, be juft for the Cafe or Pumpes head $\alpha \beta \gamma^{\circ}$, \& may be made of wood or brafe of 4 inches thick ${ }_{2}$ having a hole at $E$, which dee \{cending

## Marhematicalldecreation.

fending raifeth up the cover $P$, by which iffueth forth the water and ascending or rajring up it flouts it or makes it close : $R S$, is the handle of the fucker eyed to the han-
 die TX, which works in the port $V Z$. Let $A, B, C, \mathcal{D}$, be a prese of Braffeg thepeece which enters into the hole to $F$, to keepe out the Agree. $H_{3}, I, K, L$, the peace tyed at the funnell or pipe: in which plays the Iron rod or axis $G$, fo that it pale through the other peace $M N$, which is eyed with the end of the pipe of Braffe.
Note, that the lower end of the Cifterne ought to bee refted upon a Grediron or Iron Grate, which may be tyed in the pit; by which meane lifting up and putting downe the handle, you may draw sen times more water than otherwife you could.

## Problem, CXIII.

Mow by meakes of a Cifferne, to make water of a Pit continually to ascend without firength, or the affifance of any other Pxmpe.

LEt IL , be the Pit where one would caufe water to ascend continually to each office

## Mathematicall Recreation.

of a boufs or the places which are feparated fromit: let there be madeareceiver as $A$, well clofed up with lead or other matter that ayre enter not in, to which faften a pipe of lead as at $\varepsilon$, which may have vent at pleafure: then let there bee made a $C_{1}$ fterne as $B$, which may bee communicative to $A$, by helpe of the pipe $G$, from which ${ }^{C i}$ fterne $\mathcal{B}$, may iffue the water of pipe $D$, which may defcend to $H$, which is a little below the levell of the
 water of the pit as much as is $G H$ : ro the end of which thall be foudred clofe a Cocke which fhall calt out the water by KH. Now to make ufe of it, let $B$ befilled ful of water, \& whé you would have it run turne the Cocke, for then the water in $B$, will defcend by $K$ :and for feare that there fhould be vacuity, nature which abhors it, will labour to furninh and fupply that emprineffe out of the fpring $F$, and that the Pit dry not, the Pipe ought to bee fmall of an indifferent capacitie acenrding to the greatneffe or fmalneffe of the fpring.

Pros:

## Problem. CXIIII.

## How out of a fountaine to caft the water very high: different froms a Probleme formerly <br> delivered.

LEt the fountaine be $B \mathcal{D}$, of a round forme (feeing it is the moft capable and molt perfect figure) place into it two pipes conjoyned as $E A_{\text {s }}$ and $H C$, fo that no Ayre may enter in at the place of joyning : let each of the Pipes have a Cocke $G$, and $L$ : the Cocke at $G$, being clofed, open that at $I$, and fo with a fquirt force the water through the hole at $H$, then clofe the Cocke at $A$, and draw out the fquirt, and o. pen the Cocke at $G$ : the efirs being before rarified will extend his dimenfions and force the water with fuch violeace, that is will amount above the height of one ortwo Pikes: and fo much the more by how much the CMachine is great : this violence will laft but a lietle while if the Pipe have too great an opening, for as the Ayre approachath to his naturailplace, fo the force will diminifh.


## Mathematicall Recreafion. <br> probleme CxV.

How to empty the water of a Cifferne by a Piph which Ball have a motion of it ciffe.

LEt $A \mathcal{B}$, be the veffell; $C D$ E, the Pipe:HG; a little veffell under the greater, in which one end of the Fipe is, viz. $C$, and let the other end of the Pipe E, paffe through the bettome of the veffllat $F$, then as the veffoll filleth fo will the Pipe, \& when the veffell thall be full as farre as $P O$, the Pipe will begin to runne at $E$, of his owne accord,and never ceafe uatill the veffell bee wholly empty.

## PROXEM. CXVI.

How to Squirt or fpout out a great beight $\int_{0}$ that one pot of water flall laffa a long time.

LEt there be prepared two vefols of Braff, Lutead, or of other matter of equall fubitance, as are the two zeffels $A B$, and $B D$, \& lec them be joyned together by the two Pillars $M N$, and $E F$ : then let there be a pipe $H G$. which may pafle through the cover of the veffell $C D$, and paffe throughe $A$, into $G$, making a little bunch or rifing in the cover of the vefelles $B$, fo that the pipetouch it not as the bottome:
then

## Mathematicall Recreation.

then let there be fodered faft another Pipe IL, which may be feparated from the bottome of the veffell, and may have his bunchie fwelling as the former without touching the bottome:as is reprefented in $L$, and paffing through the bottome of $\mathcal{A} \mathcal{B}$, may be continued unto $I$, that is to fay, to make anopening to the cover of the veffell $A B, \&$ let it have a little mouth as a Trumpet: to that end to receive the water. Then there muft further be added a very fmall Pipe which may paffe through the bottome of the veffell $A$ $\mathcal{B}$, as let it be $O R$, and
let there be a bunch, or fwelling over it as at $P$, fo that it touch not alfo the bottome: let there be further made to this leffer veffell an edge in forme of a Bafen to receive the water, which being done powre water into the Pipe $1 L$, untill the veffell $C \mathcal{D}$, be full: then turne the whole machine upfide downe that the veffell $C \mathcal{D}$, may be uppermoft, and $A B$, undermoft: fo by helpe of the pipe $G H$, the water of the veffell $\epsilon D$, will sunne into the veffoll $A \mathcal{B}$, to have paffage by the $P_{2 p e} P 0$. This motion is pleafant at a feaft in filling the faid veffell with wine, which will fpout it out as though it were from a boyling fosmtaine, in the forme of a thred very plealant to behould.

Pros:

## Mathematicall Recreation.

## Problem, CXVII.

How to praltife excellently the reanimation of fimplesinincafo the plants may not be traxported to be replasted by reafon of dijfence of places.

TAke what fimple youpleare, burne it and take the afhes of it, and Iet it bee calcinated two houres betweene two Creufets well luted, and extract the falt: that is, to put mater into it in moving of it ; then let if fettle, and doe it twoor three times, afterwards evaporate it, that is, let the water be boyled in forme vefeth, untill it bee all confumed: then there will remaine a falt at the bottome, which you thall afterwards fowe in good Ground well prepared: fuch as the Theater of husbandry fheweth, and you thall have your defire.

## Prozenm, CXVIII.

## How so make an infalliable perpetuall motion.

MIxe 5 . or 6. ounces of $\overline{8}$ with his equall weight of $\psi$, grinde it together with 10 . or 12 . ounces of fublimate diffolved in cellerupon a Marble the fpace of 4 - dayes, and it will become like Ojle Olive, which deatll with fire of chaffe or driving fire, and it will fublime
fublime dry fubftance, then put water upon the earth (in forme of Lye) which will be at the bottome of the Limbecke, and diffolve that which you can;-fiter it, then diftill it, and there will bee produced very fubtill Antomes, which put into a bottle clofe fopped, and hee peit dry, and you fhall have your delire, with aftonifhment to all the world, and efpecially to thefe which have travelled herein without fruit.

## PáOBLEM. CXIX.

Of the admirable invention of making the Philofophers Tree, which one may fee with his eyeto grow by little and little.

TAketwo ounces of Aquafortis and diffolve in it halfe an oufce of fine filver refined in a Cappell: then take an ounce of Aqwafortis and todrams of 2 xicke filver: which put in it, and mixe thefe two diffolved things together; then caft it into a Viole of halfe a pound of water, which may be well ftopped; for then every day you may fee it grow both in the Tree and in the branch. This ligurid ferves to blacke haire which is red, or white, without fading untill they fall: buthere is to be noted that great care ought to bee had in annointing the haire, for feare of touching the flefb: for this compofition is very Corrofive or fearching, that as foone as it toucheth the flefs it raifech blifters,and bladders very painefull.

PROB:

## [Mathematicall Recreations]

PRoElem, CXX.

## How to make the reprefensation of the great world.

DRaw falt niter out of falt $\varepsilon$ arth which is found along the Rivers fide, and at the foote of Mountaines, where efpecially are Minerals of Gonld and Flver: mixe that Niter well clenfed with 4 , then calcinate it hermetically; then put it in a Limbecke and let the receiver be of Glafe, well luted, and alwayes, in which let there be placed leaves of Gould at the bottome, then put fre under the Limm becke untill vapours arife whichwill cleve unto the Gould; augment your fire untill there afcend no more, then take away your
 receiver and clofe it hermeticaily, \& make a Lampe fire under it wrill you may fee prefented in it that which nature affords us: is Flowers, Trees, Fruits, Fonntaines, Sunne, Eloone, Starres, $\sigma$. Behould here the forme of the Limbecke, and the receiver: $A$ reprefents the Limbecke, $B$ Itands for the receiver. S Proze

## Mathematicall Racreation.

## Probxem CXXI.

How to makea Cone, or a Pyramidall body neave upon a Table without Prings or other Artio ficiall meanes : So that it grati
nsove by the edge of the
Tablewithout
falling.

THis propofition is not fo thornie and fubtile as it feemes to be, for putting under a Cone of paper a Beesle or fuch like creature, yous Thall have pleafure with aftonifhment 3 c admiration to thefe which are ignorant in the caule:for this animall will ftrive alwayes to free herfelfe from the captivity in which fhee is in by the imprifonment of the Cone: for comming neere the edge of the
Table fhee will returne to the other fide for feare of falling.

## Prozem. CXXII.

Tocleave an Anvill with the blow of a Pifoll.
T His is proper to a warrier, and to performe it, let the exnvill be heated red hot as one

## Mashematicall Recreation?

can polfible, in fuch fort that all the folidity of the body bee foftned by the fire : then charge the Piftol with a bullet of filver, and fo have you infallibly the experiment.

## probдem. CXXIII.

How toroft a Capon carried in a Budget at a Saddle bow, in the Space of riding 5 or 6. miles.

HAving made it ready and larded it,ftufe it with Butter; then heate a peece of feele which may be formed round according to the length of the Capor, and big enough to fill the Belly of it, and then flop it with Butter; then wrap it up well and inclore it in a Box in the Brdget, and you thall have your defire :it is faid that Count Mansfeld ferved himfelfe with no others, but fuch as were made ready in this kind, for that it lofeth none of its fubtance, and it is dreffed very equally.

## Problem, CXXIIII.

How to make a Candle burme and continne three times as long as otherwise it would.

- 7 Nto the end of a Candle helfe burned ficke a farthing leffe or more, to make it hang St


## Nathematicall Recreazion.

perpendicular in a veffell of water, to that it bpec fwamme above the reater; then light it, and it will fuftaine it felfe \&u floate in this manner; and being placed into a fonntaine, pond, or lake that runs flowly; where many people affemble, it will caufe an extreame feare to thefe which come therein in the night, knowing not what it is.


PRoblem. CXXV.
How out of a quantitic of wine to extraft that which is msoft windy, and evill, that it burt not a ficke Perfon.

TAke two viols in fuch fort that they bee of like greatneffe both in the belly and the necke; fill one of them of wise, and the other of water: let the mouth of that which hath thewater be placed into the mouth of that which hath the wine, fo the water thallt.

## Mathematicall Recreation.'

be uppermont:now becaufe the water is heavies than the wine, it' will defcend into the other violl, and the wine which is higheft will afcend above to fupply the place of the water, and to there will be a mutuall interchange of lignids: and by this penitration the wine will lofe her vapors.

## Proz LEM.CXXVI.

How to make two Marmonzets one of which foall light a Candle, and the otber put it out.

vVonthe fide of a wall make the figure of a Marmonzet or other animall or forme, and right azaint it on the other wall make another; in the mouth of each put a pipe or quill fo Artifcially that it be not perceived:in one of which place falt peeter very fine, and dry and pulueriled: and at the end fet a little match of Paper: in the other place fulphwr beaten fmall: then houlding a Candle lighted in your hand, fay to one of thefe Images by way, of commaund, blow out the Candle:then lighting tbe Paper with the Candle, the falt peeter will blow out the Candle immediatly: and going to the other Imsage (before the match of the Candle be our) touch the falphur with it and fay, light the Candle, and it will inmediatly belighted, which will caufe an admiration to thefe which fee the action : it it be done with decret dexterity:

## Pxosilk, CXXVII.

How to keepewime fref as if it were in a celler shough it were in the heate of 5 rmmer, and without Ice or fnow, yea though it were carried at a faddles bow, and expoled to the Swnne all the day.

SEt your wine in a violl of Glafe; and place it in a Box made of wood, leather, or fuch like : about which violl place falt peeter, and it will preferve it and keepe it very frefh: this experiment is not a little commodious for thefe which are not neare fref waters, and whofe dwellings are much expofed to the Sunne.

## PROEEEM, CXXVIII.

To make a Cement which indureth or lafteth as marble, which reffeteth ayre and waser without ever difjoyning or uncomiting

TAke a quantitic of frong and gluing CMorter well beaten, mixe with this as much new feaked Lime, and upon it caft Oyle of Olive, or Limfeede Oyle, and it will become hard as Mar $6 l e$ being applyed in time.

Pros:

## Mashematicall Recreation. <br> FIOBLIM, CXXIX.

How so welt mottle very quicke, yea in a fuclluponlittle fire.

MAkea bed upon a bed of mettle with powder of Sulphur, of Salt peeter, and Jawduff alike;then put fire to the fayd powder with a burning Charcole, and you fhall fee that the mettle will diffolve incontinent and bee in a Maff. This fecret is moft excellent and hath beene practifed by the reverend father CMerconne of the order of the Mimins.

## Probinm. CXXX.

How to make Iron or Steele exceeding hard.

QVench your Blade or other Infirument feven times in the blood of a male Hog, mixt with Goofe greafo, and at each time dry it at the fire before you wet it: and it will become exceeding hard, and not brittle, which is not ordinary accerding to other temperings and quenchings of Iren:an experiment of fmall coft, often proved, and of great conleguence for $A r$ morie in warlike negotiations.

## Thasbematicall Recreationa

PROELEM. CXXXI.

Topreferve fire as long as you will, imaitating the inextinguable fire of $V$ eftales.

AFter that you have extracted the burning fpirit of the falt of 24 , by the degrees of fire, as is required according to the Art of Chimiftrie, the fre being kinelled of it felfe, breake the Limbecke, and the Irons whichare found at the botome will flame and appeare as burning Coles as foone as they feele the ayre; $w^{\text {ch }}$ if you promtly inclofe in a violl of Glaffe, and that you ftop it exactly with fome good lute:or to be more aflured it may be clofed up with Hermes 2pax for feare that the Ayre get not in. Then will it keepe more than a thoufand yeares (as a man may fay) yea at the bottome of the Sea; and apening it at the end of the time, as foone as it feeles the Ayre it takes fire with which you may light a Match. This fecret merits to be travailed ofter and put in practife, for that it is not common, and full of aftonifoment, feeing that all kind of fire latteth but as, long as his matter lafteth, and that there is no matter to be found that will fo long indure.

## FINIS.

## (AN

 Artificiall fire-W orkes: Or the manner of making of Rockets and Balss of fire, as weil for th: Water, as for the Ayre; with the compofition of Stars, Golden-raike, Serpents,Lances, WW beteles of fre, and fich lise, pleafant and Recreative.

Of the compofition for Rockers.


N the making f Rockets, the cheefeft thingto beregarded is the compofition that they ought to befilled with, for as much as that which is proper to Rockets which are of a leffe fort is very improper tothofe which are of a more greater forme; for the fire being lighted in a great concave, which is filled with a quick compofition,burnes with great violence;contrarily, a weake conpofition being placed into a fmall concave, makes no effeet: therefore we thall here deliver in the firft place rules and directions, which may ferve fur the true compofition, or matter with which you may charge any Rocket, from Rockets which are charged but with one ounce of

## Of Fire-Workes.

Powder unto great Rockets which requireth for their chargero. pound of Powder, as followeth

## For Rockets of one onice.

Vinto each pound of good musket Powder forall beaten, put two ounces of fimall Cole duft, and with this compofition charge the Rocket.

$$
\text { For Rockers of } 2 \text {, or } 3 \text {.ounces. }
$$

Vnto every fouse oances and a balfe of powder duft, adde an ounce of Sale-pecter, or to evesy 4 . ounces of powder dwfe, adde an ounce of Colednft.

$$
\text { For Rockets of } 4 \text {.osnces: }
$$

Vnto cvery pound of Powder duft adde 4. ounces of S. Peeter \& one ounce of Coleduf: but to have it more flow, unto every 10 . ounces of gond duft powder adde 3 . eunces of Saltpeeter, and 3 . ounces of Coleduft.

For Rockets of 5 oor 6 ounces.
Vnto every pound of powder $d x f t$, adde 3 . ounces and a halfe of Salt peeter, and 2. ounces and a halfe of Cole duft, as alfo an ounce of Sulpher and an ounce of fyle duff.

For Rockets of 7, or 8.onnces.
Vnto every pound of $P$ owder duff adde 4. ounces of Salt peeter and 3 . ouncts of Swlpher. Of Rockers of 10 , or 12 ,ownces.
Vato the precedent compofition adde halfe an ounce of Sulpher, and it will be fufficient. For Rockers of 14 , or 15 ,ounces.
Vnto every pound of Powder $\dot{d x f}$ \& adde 4 .ouncss of Salt peeter, of Cole duff $\frac{3}{4}$ ounces. of

## of Fire-Workes.

Sulpher and filedrift of each $1 \frac{3}{4}$ ounces. For Rockets of 1 ,ponad.
Vnto every pound of Porider duft adde 3 ounces of Coleduft, and one ounce ot Sulpher. Of Rockets of 2, pound.
Vritoevery pound of Powder duff adde $9 \frac{2}{2}$ ounces of Salt peeter, of Coledaft $2 \frac{3}{2}$ ounces, fileduf $1 \frac{1}{2}$ ounces, and of Sulpher $\frac{3}{9}$ ot ounces. For Reckers of 3 , poind.
Vnto every pound of Sats peeter adde 6 ounces of Cole duft, and of Sulpher 4 ,ounces.

For Rockers of $4,5,6$ or 7, pound.
Vnto every pound of Saltpecter add 5 . oun. ces of Cole duft and $2 \frac{7}{3}$ ounces ot Sulphyr.

$$
\text { For Rockets of } 8 \text {, or } 10 \text {, pound. }
$$

Vnto every pound of Salt peetere, adde $5 \frac{1}{2}$ ounces of Cole duff and of Sulphur $2 \frac{1}{2}$ ounces.
Here note that in all great Rockets, there is no Powder put, becaufe of the greatnefle of the fire which is lighted ar once, which caufeth too great a violence, therefere ought to bee filled with a more weaker compofition.

Of the making of Rockets and other Firewsples.

FOr the making of Rockets of fundry kinds; divers molds are to be made, with their Rowling pirs, Breathes, Chargers, ofc. as may be feene here in the figure. And having rowIeda Cafe of paper upon the Rowling pin for your mould, fill it with the compolition belonging to that mould as before is delivered:
now may you loade it on the top, with Serpents, Reports, Stars, or Golden Raine: the Serpents are made about the bigneffe of ones litsle finger, by rowling a little paper upon a fmall fticke, and then tying one end of it and filling it with the mixtconnpofition fomewhat clofe, and then tying the other end. The reportsare made in their paper Cafes as the Serpents, but the Paper fomewhat thickerto

graixe Powder or halfe Powder and halfe compofition, and tying bothends clore, they are finifhed. The beft kind of farres are made with this mixture following; unto every 4. ounces of Salit perter, adde 2.ounces of Sulphwr

## Of Firs-workes.

phur, and to it put 1 .ounce of Powder duft, and of this compofition make your ftarres, by putting a little of it within a fmall quantity of

## Of recreative fires.

PHiloftrates faith, that if wine in a Platiter bee placed upon a receiver of burning Coles, to exhale the fpirit of it, and be inclofed withina Coploard or fuch like place, fo that the Ayre may not goe in, nor out, and fo being Inut up for 30. yeares : he that thall open it, having a wax Candle lighted, and thall put it into the Cwpboard; there will appeare unto him the figure of many cleare fonrres.
If Aquevite have Camphere diffolved in its and be eyaporated in a clofe Chamber, where there is but a Charcolefire, the firt that enters into the Chamber with a Candle lighted, will be extreamely aftonifhed, for all the Chamber will feeme to be full of fre very fubtile, but it will be of little continuance.

Casdles which are deceitfull are made of halfe Pomder, covered over with $T$ alow; and the other halfe is made of cleane Tallom, or Waxe, with an ordinary meeke; this Candle being lighted and the upper halfe confuned, the Powder will take fire, not without great noyfe and atonimment to thofe which arcig. norant of the caufe.

A dozen or twenty frmall Serpents placed fe cretly under a Candlefficke that is indifferent big. which may have a hole paffe through the Cocket of it to the Candle, throwgh which a peece of primer may be placed, and fetting a fonali Candle in the facket to burne according

## Of Fite-Workes.

to a time limited: which Candlefficke may bce fet onafide Table without fufpition to any; then when the Candle is burned, that it fires the primer, that inmediatly will fire all the Sorpents, which overthrowing ite Cmolleflick will flye here and there, intermixung themfelves, fometimes in the Ayre, fometimes in the Planching, one amongf another, like the crawling of Serpents, continuing for a pretty while in this pofture, and in extinguithing every one will give his report tike a p:foll; This will not a litele aftonifh fome, thinking the houfe will bee fired, though the whole powder together makes not an ounce, aed hath no Atrength to doe fuch an effect.

## How to make fire runne up and downe, formard and backuard.

TAke faall Rockets, and place the tajle of one to the hed of the other, upon a Cord according to your fancie, as admit the Cord to be A B CD E F G. give fire to the Rocket at A, which will fly to $B$, which will come backe againe to $A$, and fire another at $C$, that will fly at $\mathcal{D}$, which will fire another there, and fy to $\varepsilon$, and that to $F$ : and fo from $F$, to $G$ : and at $G$, may be placed a pot of fire, viz. $G H_{\text {: }}$ which fired will make good fport, becaule the Serpents whichare in it will varioufly intermix thenafelves in the Ayre, and upon the ground, and every one will extinguinh with a report : and here may you'note that upon the

Rockers

Rockets may be piaced fierie Dragons Comba. tants, or fuch like to mecte one another, having
lights placed in the Concavity of their bodies, which will give great grace to the action.

## How to make wheeles of fire.

TAke a Heope, and place two laths acroffe one the other; upon the croffing of which make a hole, fo that it may be placed upoma pin to turne eafily, as the figure 2. The weth: upon the fides of which hoope or round Cirele place your Rockers, to which you may place Lances of fire betweene each

## Of Fire-Workes.

Rockett'et this wheelebe placed upon a fandard as here is reprefented, and place a peece of Primer from one Lanceso another, then give fire at $G$, which willfire $F$, that $E$, that will fire $\mathcal{D}$,

that $\mathcal{C}$, and that will fire the Rockerate © ${ }^{2}$ : then immediatly the wheele will begin to moveand reprefent unto the fpectators 2 Circle of changeable fire, and if pors of fire be tied to ir, you will have fine fort in the turning of the whecle and cafting out of the Serpents.

CLubbes, Targuets, Faulchons, and CMabs charged with feverall fires, doe make your nights Combatants, or are ifed to malke place amongt a throng of people. The Clubber at the ends are made like a round Panier with fmall
fmall fticks, filled with little Rookets in a fpirall forme, glued and fo placed that they fire but one arter another; the craffes are of diversfahions, fone made oblong at the end, fome made of a fpirall forme, but all made hollow to put in feverall compogition, and are boared in divers places, which are for fundry Rockos, and Lances of weake coaspofition to be firedat pleafure: The Fanlchoss are made of wood in a bowing forme tike the figure $\ldots$, having their backes large to receive many Roce kets, the head of one aeare the neeke of another,glued and fartned well together, fo that one being (pene another may be fired : The Tar =

## Of Fire-Workes.

ta fire the Rockets one after another, which is all covered with chinne covering of mood, or Pafboard, boared with holes fpirally alfo; which Rockets muft be glued and made faft to the place of the Chanells : Now if twomen the one having a Targuet in his hand, and the other a Falchan, or CNaffe of fire Thall begin to fight, it will appeare very pleafant to the Speeritaxs: for by the motion of fighting, the place will feeme to be full of ftreames of five: and there may be adjoyned to each Targuer a Sunxe or a burning Comet with Lanses of fire, which will make them more beautifull and refplendent in that action.

SVch as are ufed for recreation, are (oHofirw, Statmes, Arches, Fyramedies, Chargots,

## Of Fire Works.

Chaires of triumph \& fuch like, which may be accommodated with Rackets of fire, \& beautiGed with foundry other artificiall fires, as pots of fire for the Ayre w ${ }^{\text {ch }}$ may caff forth Several figures, Scutcheons, Rockets of divers forts, Starves, Crownes, Leaters, and fuck like; the borders of which may be armed with fundry Lances of fire, of finall Allying Rockets with reports, Games, of foal birds of Cypres, Lase ternes of fire, Candles of divers ufes, and colours in burning: and whatfoevr the fancie of an ingenious head may allude unto.

Of Pots of fire for the Are, which are thrown out of one Cafe one after another of a long continuance.

MAkea long Trunke as $A G$, and by the fide $\mathcal{A} H$, let there be a Charnel which nay be fiered with flow primer or compofition; then having charged the Trunke $A G$, with the Pots of fire for the e Ayreizt IGEC, and made the Truske e $1 G$, very fat unto a $\mathcal{P}$ off as $I K$, give fire at the top as at $A$, which burning downewards will give fire to $C$, and fo throughout that $P$ ot in the tyre, which being fpeut, in the mane time the fire will burse from $B$, to $D$, and fo fire $E$, and throw it out alto into the Aye, and fo all the reft one after another will be throwne out: and if the Pots of fire for the fAyre which are catt out, bee filled with diverse Fireworks, they

## Wh Of Fire-Workes.

they will bee fo much the more pleafant to the behoulders. Thefe Trunkes of fire doe greatly adorne a Firewerke, and may conveniently bee placed ad each angle of the whole worke.


> of Pors of fire for the ground.

M any Pots of fire beiog fired together doe
 caufe a wonderfull fhout amongt the common people which are ftanders by; for thofe Poos being filled with Balles of


Eigure $H$.
 fire and flying Serpents for the Ayre, they will fo intermix one within another, in flying here and therea little above the ground, and giving fuch a volley of reports that the Ayre will rebound with their noife, and the whole place bee filled with fundry ftreames

## Of Fire-Workes.

Iftreames of pleafant fire ; which ferpents will much occupic thefe about the place to defend themfelves in their upper parts, when they will nolefle be bufied by the bailes of fire, which feemes to annoy their feete.
of Balles of fire.

THere are very various according to 2 mans fancie fo we of which are made with very fmall Rockets, the head of one tyed to the neck of another: the ball being made may be covered over with pitch except the hole to give fire to it;this Ball will make fine fport amongt the Atanders by, which will take all a fire, and rowle fometimes this way, fometimes that way, betweene the legs of thofe that are ftanders by, if they takenot heede, for the motion will be very irregular, and in the motion will caft forth feverall fires with reports. In the fecond kind there may be a chanell of Iron placed in divers places in fpirall manner, a- $^{-}$ gaint which may be placed as many fmall pezards of paper aspoffible may be, the Channell muft be full of flow compofition and may be covered as the former, and made fit with his Rockers in the middle: this 3 all may bee fhor


## Of Fireworkes.

out of a morter Peece or charged on the rop of a Rocket : for in itsmotion it will fly here and there, and give many reports in the Ayre : bscaufe of the difcharge of the petards.

## of fire exponthewater.

PLaces which are fituated upon Rivers or great Ponds, are proper to make Recreative fires on : and if it be required to make fome of cenfequeace, fuch may conveniently bee made upon two Boats, uppon which may be builttwo Beafts, $T$ wrrets, Pagents, Caftles, or fuch like, to

reeeive日 Fod dibediverfitity of Fire warkes that may \& made within it, in which may play divers fires, Petards, efc. and caft out many fimple Grenades, Balls of fire to burne in the

## Of Eirc-Workes.

 water ferpents and other things, and often slimes these bates in their incounters may fang one in another, that fo the Combatants with the Targets, and Males may fight; which will give great content to the eyes of thole which are lookers on, and in the conclufion fire one another, (for which end they were made:) $5 y$ which the dexterity of the one may be known in refpect of the other, and the riumph and victory of the fight gotten.Of Battles of fire which moves upon the water.

THere may be made in forme of a Ball futfed with other little Balls, glued round about and filled with compofition for the maer, which fired will produce merveilous and admirable effects, for which there mutt be had little Canons of white Iron, as the ends of mall runnels; thee Iron Cannons may be weircedi in fundry places, to which holes, may be fell Anal Belles full of compofition for the water, which finall Balls malt be peireed deepe and large, and covered with Pitch, except the hole : in which hole mat bee frit placed a little quantities of graine $P$ owner; and the reft of the hole filled up with comvolition ; and note further that there Iron Cannons, mull


## Of Fire-Workes.

be filled with a flow compoivion; but fuch which is proper to burne in the mater: then mut thefe Cannons with their fmall Balls bee put fotogether that it may mike a Globe, and the holes in the Cannons beanfwerable to the hollow Talls, and all covered over with Pitchs and Tallow; afterwards pierfe this Ball againt the greateft Cannon (to which all tine leffer fhould anfwer) unto the cempofition, then fire it, and when it begins co blow, throw it into the water, fo the fire comming to the holes will fire the graine Powder, the which will caufe the Balls to feparate and fly bere and there, fometimes two at a time, fometimes three, fometimes more, which will burne wi:h in the water with great aftonifhment and content to thote wnich fee it.

## Of Lances of fire.

TTanding Lances of fire, are made commonly Swith hollow wood, to containe fundry Petards, or Rockets, as the figure here fieweth, by which is eafie to ineent others accordinty to ones fancy. Thefe Lances have woodden handies, that fothey may be faftued as forue Poft, fo that they be nor overthrowne in the flying out of the Rockets, or Petards: there are lefler forts of Lances whofe cafes are of threc or foure fouldings of $E$ aper of a foote long, and about the bigneffe of ones finger, whichare filled with a compofition for Lances. But if thefe Lances be filled with a compofiti- 2.ounces of Sali pecter, and unto that adde I. ounce of Suiphur) it will make a brick fire red before it be halfe fpent, if the Lance be fiered and heid to it : and if 20. fuch Lances were placed about
 a great Rocket and fhot to a bouse or fip, it would produce a mifchievous effect.

> How to Boote a Rocket Horizontall, or Otberwife.

VNto the end of the Rocket place an Arrow which may not be too heavy, but in ftead of the fearhers let that bee of thinne white tinne plate, and place it upon a reft, as here you may fee by the Figures then give fire unto it, and you may fee how ferviceable it may bee. To the
 head of fuch Rockets may be placed Petards, Balls of firc,Grenardes, orc, and fo may be applyed to warlike uffaires.

## Of Eire-workes.

How a Rocket burning in the rater for acertaine time, at laff Ball fly up in the Ayre zoith an excceding quickne $\iint$ e.

TO doe this take two Rockets the one equall to the other, and joyne them one untoanother in the middle at $\mathcal{C}$. in fuch fort that the fire may eafily paffe from one to another:it bes ing thas done, tye the two Rockers at a llicke in $\mathcal{D}$, and let it be fo long and great that it may make the Rockets in the water hang, or lye upright; then take a packe thread and tye it at $G$. and let it come double about the fticke D M. at $H_{0}$ and at that point hanga Bullet of fome weight as K. for then giving fire at $A$. it will burne to B. by 2 fraall ferpent filled there and tyed at
 the end, and covered fo that the water injure it no:, which wilk fire the Rorket $B \mathcal{D}$, and fo mounting quicke out of the water by the loofe tying at $C$, and the Bullet at the packe thread, will leave the other Pocket in the water: and fo afcend like a Rocket in the Ayre, to the admiration of fuch as know not the fecrecie.

## Of the framing of the parts of a Fire.Worke together that the feverall woikes. may fre one after anotber.

CAufe a frame to be made as $A B C D$. of stwo foot fquare every way, or thereabouts (according to the quantity of your feverall workes) then may you at each angle have a great Lance of fire to ffand, which may caft out Pots of fire as they confume: upon the ledges, $A B . B C$, and $C$ D. may bee placed fmall Lances of fire about the number of 30 . or 60. fome fidewife, \& o ohers upright, betweene thefe Lances may be placed Pots of fire floping outwards, but made very faft, and covered very clofe, that they chance not to fire before they fhould; then upon the ledges RE.F G.H . and $A D$.may be placed your foucifons, and behind al the work may be fet your Boxes of RocKets in each of which y ou may place $6,9,12$.or 20. fmall Rockets : Now give fire at $A$. (by helpe of a peece of primer going from one Lance to another) all the Lances will inftantly at once be lighted, and as foone as the Lance at $e f$ is confumed, it will fire the Chamell which is made in the ledge of the frame which runnes under the Pots of fire, and as the fire goes along burning, the Fots will be calt forth, and fo the ranke of Pots upon the fides of the frame $A \mathcal{B} . B C$ and $C D$. being fpent, the foucifons will begin to play being fiered alfo by a Chamell which runnes under them, upon the
 the Soucifors are fpent, upon the laftedge $R E$. there may bea fecret Chanrell in the ledge $C \mathcal{D}$, which may fire the Box of Rockets at K. \& may fireall the reft one after another, which Boxes may be all charged with feverail Fre-Workes: for the Rockets of the firlt Box may be loaden with ferpents, the fecond with ftarres, the third with reports, he fourth with Goulden raine, and the fift with fmall fying Serpents; thefe mounting one after another and flying too and frowill much inligbren the Ayre in their af cending, but when thefe Rockets difcharge themfelves above, then will there be a moft pleafant reprefentation, for thefe fires will dilate themfelves in divers beautifull formes, fome likethe branching of Trees, others like fountaines of water gliding in the ayre, others like flafnes of lightning, otherslike the glitte ring of ftarres, giving great contentment, and delighe to thole phich behold them; But if the worke be furnihned alfo with Silons (which is the chicfeft in recreative Fire-workes) then Thall youfee afcending in the ayre but as it wereonely a quill of firc, bus once the Balon raking fire, the Ayre, will fecme more than 100. foot fquare full of crawling, and flying ferpents, whichwill cxinguinh with avolles of more than 5 ooreposeng sud fo fill the esfre and Firmawsen withutuerc iqbounding clamour.

The making of which with many other rare and cxcellenc Fircworkes, and other practiles
of Fire-workes.
practifes, not onely for recreation, but alfo for fervice: you may finde in a booke intituled Artificiall Fire morkes, made by Mr. eMalthas (a mafter of his knowledge) and are to be fold by Rich. Fiaw kins at his fhop in (bancery lawe, neare Sarjants Inme.

## Conclufion.

## In this Booke we have nothing

 omitted what was materiall in the originall, but have abundanto ly augmented it in fundry experiments : And though the examinations are not fo full, and manifold, yet (by way of brevitie) we have expreffed fully their fubftance, to avoyd prolixitie, and fo paft by things reiterated.
## FINIS.



## Ad Authorem D. D. Henricum

 Van Etenium, Alumnum Academix Ponta Mouffon.A RduaWalkeri fileant fecreta profundi, Definat occultam carpere Porta viam: Itala Cardanimirata eft Lampada docti Terra, Syrachfium Gracia tota fenem: Orbiterrarum, Ptolemai Clepyydratoti, Raradioptra Procli, mira fuere duo. Anglia te foveat doctus Pont- Mouffon alumsй:
Qxidquid nature,quilegis, bortus habet.
Docta cqûbinet opus doctum, te fit tua docto
Digna, Syracufij, arca, corona, viri, Arca Syracufis utinam fit plambea forvis, Aureafed dominis, aurea totafuis:

## A Table of the particurall heads of this Booke, contrazted according to the feverall Arts fpecified in the Title page.

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## Experiments in Fireworkeso

Frompage,265,to the end.

$$
\mathcal{F} I N I S .
$$

Fecenfrib bunc librum cuititulus efts Mathamaticall Recreations, qui quidem liber continet centum, ov vigin= ti folia, in quibis ommibus nibil reperio, quad non cum utilitate Publica impris matur, modo intra feptem menees proximé é equentes typis mandetur.

Exxdibus Londinen- Guil.Bray, GBus.Inl.23.1632. Epenfi Capellanus Domefticus.

Ris apoore c fourk at ontc $2 \operatorname{Lin}_{2}$ Roseo $I I$ forming at Gok omis Goses mist bo owivs, nozithe akes howhe < ofes a movy 7 bunn - Dours fos $\sim 2$ armer os of 8 mula flow no prot fot 2 Hho miso onfor o no fimpon 2 nowke ino or fothon sorket Ins -6 N hill $a=$ sorket gns $-6 \sim$ ariel 7 go mugt por上f frike Eivis a bonto yo norket


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\begin{aligned}
& \text { Q164 } \\
& \text { R4313 } \\
& 1633 \\
& \text { Rare BK } \\
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