## THE

## Gentleman's Diary, <br> ORTHE

Mathematical Repository; An ALMANACK For the Year of our LORD if6g. BEING
The First after Bissextile, or Leap-Year。 Containing many ufeful and entertaining Particulars peculiarly adapted to the ingenious Gentlemen engaged in the moft delightful Study and Practice of the MATHEMATICKS.

The Twenty-ninth Almanack publifhed of this Kind; and the Seventeenth of the NEwStyle in Exglasd:

## With wife Intent

The Hand of Nature on peculiar Minds Imprints a diff'rent Byafs, and to each Decrees its Province in the common Toil. To fome the taught the Fabric of the Sphere, The changeful Moon, the Circuit of the Stars, The golden Zones of Heav'n: to fome fhe gave To weigh the Moment of eternal Things, Of 'Time, and Space, and Fate's unbroken Chain, And Will's quick Impulfe.

Akenside.

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\mathrm{L}_{\mathrm{L}} \bigcirc \mathrm{~N} D O \mathrm{~N}_{\mathrm{N}}
$$

Printed for the Company of Stationers. M.DCC.LXIX.
[Price Nine-pence ftitch'd.]

$\mathrm{A}^{\prime}$If L Perfons who pleafe to be Contributors to this Diary, by anfwering the शuefions, Enigmas, \&c. or by fending new ones, or any other ufeful, entertaining and improving Subjects proper for this Work; are earneflly defired to fend them, and their Solutions at large along with kem (otherwine they need not expect their Publication) before ihe firt Day of May 1769: DireEted, for the Author of the Gentleman's Diary; and to be left with Mr. Heitry Cropfer, Attorney at Lare; in hougbborough, who will forward them to the Author.

## P R O P O S A L S

Formaking, and publishing by Subscription, A new and accurate Map of the Gounty of Leicesterp. From an actual Survey of the fame.
By Thomas Peat, of Thringfon, Surveyor, and Affiftants. In this Map will be particularly noted and planned all the Market Towns, with their true Diffances, and all notable Villages thro which any principal Roads do pafs. The Place and Diftance of every Village will be truly ajcertained, and expreffed. All the great Roads, and Turnpikes, will be taken and laid down from Chain Meafure, as alfo the finaller from one Village to another, and a proper Diftinction preferved. The County will be truly bounded, and properly divided according to its feveral Hundreds. The Foreft Boundaries, and thofe of the large C mmens, will be pointed out. The Courfe of all the Rivers and Rivulers, will be exactly defribed. The feveral Seats of the Nubility and Gentry will be truly fixed in this Map. All Places noted for Curiofities in Nature, as Minerals, \&c. or for Antiquities, or any remarkable Occurrences, will be taken Notice of in fuch Manner as to render it alfo a general View of the Natural Hiftory of the County. Alfo the Latitude of every Market Town will be accurately determined, together with its Longitude from the Meridian of London, \&c.
C O N D I T I O N S.

This Work will be Engraved by the beit Hands; and decorated with the Arms of fuch of the Nobility and Gentry, as choofe to have them emblazon'd ; and other proper Embellifhments, fo as to tender the Whole as compleat as any Thing of the Kind.

The Scale is propofed to be one Statute Mile in an Inch.
The Pree tu Subcribers will be Half a Guin a; Five Shillings to be $\mathrm{pa}^{3}$ id in the Courfe of the Survey, and the Remainder on D livery of the Map; except thoie who have thear Arms in the Margin ; who are to pay Hali a Guinea at Subfcribing, and Half a Guined more on the Delivery.
'the Wurk will be carricd on with all convenient Expedition, provided the Irr jectors me $t$ with a proper Enc uragement, adequate to fo large an Widertaking; and whever will be fo kind, are defired inly to find Heir Names to Mir. Juinn Gregory, Printer, in Leic Aer, as no Subfitintinn Phinty will ber requird, beforea proper Jud mes, can be formed.
N.R. Lanc's furvey'd, oivided, and inclifed; and Maps of the fame correcily dimeated; alf. Timber valued, Houfes, and other Buildir.gs, defigrid, drawn, furveyed, and eftimated, by the faid Thomas Peat, late of Nottingham, now of Thringfon, in the County of Leicefter.

All Letters are defired to be fent Poft paid.








| e | If at Night. | $117^{\circ} 57$ |
| :---: | :---: | :---: |
| Firft Quarter the gin | 54 m . Paft $10 \mathrm{M} \cdot \mathrm{rn}$. | $6{ }^{6} 1638$ |
| Iull Moon the Ijth | a Qirarter paf 11 Foren. | $11 \begin{array}{lll}15 \\ 11\end{array}$ |
| Laft Quarier the 24th | 20 m . Afierno n . | $16 / 133^{8}$ |
| New Moon the 319. | ( 34 m . paft 9 Morn. | $\left.\right\|_{2 \lim _{2}} ^{21_{1}}$ |



## S EPTE MBER hath $x x x$ Days. $\left|\begin{array}{l}\text { M } \\ \mid\end{array}\right| \begin{aligned} & \text { O } \\ & \text { North. }\end{aligned}$






## DECEMBER hath xxxi Days. <br> MIO Deci.




ATABLE of all the Kings and Queens of England, fince the Conqueft.


Names. William Conq. Williain Rufus
Henry 1.
Stenhen
Henry II.
Richard I.
John
Henry III.
Edward I.
Edward II.
Edward III. Richard II. Aenry lV. Henry V. Henry VI. Enward IV. Edward V. Richard III. Denry VII. Aenry VIII. Edward VI. Mary I. Elizabeth !ames I. Chames I. Charles II. lomes II.
\{Willian ILI.
[Mary II.
Anne
Geurge I.
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A Compendious Table of Interest, Shewing the Intereft of any Sum of Money, from a Million to a Pound; for any Number of Days, at any Rate o Intereft.

| No 1. s. | 1. s. d. $q$ |
| :---: | :---: |
| 1000000-2739 14 60,99 | 1000-2 $14.92,14$ |
| 900000-2405 15 0 3,29 | 900-2 933,12 |
| 800000-219115 71,59 | 800-2 3100,11 |
| 700000-191716 1 3 ,89 | 700-1 18 4 18 ,10 |
| 600000-1643 16 82,19 | 600-1 12102 ,80 |
| 500000-1369 17 300,49 | 500-1 7 7 433 , c |
| 400000-1095 17 92,79 | 400-1 111100,50 |
| 300000-821 18 4 4 , 09 | $300-016 \quad 5 \quad 1.40$ |
| $200000-54718103,40$ | 200-0 10 11 2 ,30 |
| 100000-27319 5 1, 70 | 100-0 $5 \quad 53,10$ |
| 90000-246 11 60,32 | 90-0 41130,71 |
| $8=000-219360,96$ | $80-04422,41$ |
| 700e0-19115 71,59 | $70-03100,11$ |
| 60000-164 7 8 0, 22 | 31,81 |
| 50000-136 19 8 2,85 | 83,51 |
| 40000-109 11919,4 | 40-0 221,21 |
| 30000-84 3100,11 | $30-1170,90$ |
| 20000- 5415102,74 | 20-0 1 10,60 |
| 10000- 27 7 111,37 | 10-0 0-6 2,30 |
| 9000- 241313,23 | $6-00503.67$ |
| 8000- 211641,10 | 8-0 0511,04 |
| $7000-19362,96$ | 42,41 |
| $60=0-16$ \% 90,82 | 6-0 0 - 3 3,78 |
| 5000-1313112,58 | 5-0 0 0 311,15 |
| 4000-1019 20,15 | 4-0 0-2 2,52 |
| $3000-84420,41$ | $3-00013,89$ |
| 200)- 5970,27 | 2-0 0 0 111,26 |
| 1000- $\quad 1192,14$ | $1-0002,63$ |

## R U L E.

Multiply the Sum by the Number of Days; ans that Product by the Rate per Cent.'Then cut (ff the two lait Figures to the Right Hand, and the refl you muft find in the Table.
Example, What is che Intereft of $100!$ tor 365 Days at 5 per Cent.


# The Gent. Diary; or, Math. Repofitory. 17 

## Continuation of the Rev. Mr. Smith's Letter to the Author.

Reflex. g. Moreover the Time of the Earth's paffing over D A B' in our Summer, was $81 \mathrm{~d} .10 \mathrm{~h} .40 \mathrm{~m} .35^{\prime \prime}$; but in Winter it defcribed an equal Angle from H toI in $76 \mathrm{~d} .12 \mathrm{~h} .53 \mathrm{~m} .2 \mathrm{I}^{\prime \prime}$; confequentlv, even granting the Orbit to be a Cirele, and her Motion uniform, the Diftances cannot remain the fance; or, if they do, the Motion then cannot be uniform, but accelerated in defcribing HPI; wherefore, fince the Orbit has been proved an Ellipfe, this Phenomenon arifes both from a nearer Diffance and an Acceleration, amounting together nearly to a fifteenth Part of the whole; of which Reality our Antipodes muft inevitably be as fenfible in December, or their Summer, as we in our Winter.

Reflex. 10. The obferved angular Velocities are not in inverfe Ratio of the different Diameters of the Sun, fo that the Inequalities of the Earth's Motion are not barely apoarent, and caufed only by a Change in the Diftance from the Sun; for if they were, then it would be as $3^{1}{ }^{\prime} 3^{\prime \prime}, 89$, the obferved Diameter at $A: 7^{\prime} 9^{\prime \prime}, 076$, the Velocity there, :: $32^{\prime} 42^{\prime \prime}, 18$, obf. Diam. at P, : $7^{\prime} 23^{\prime \prime}, 845$, the Velocity there; but it was obferved $7^{\prime} 33^{\prime \prime}, 621$; whereby it clearly follows, that the Motion of the Farth is really accelerated as fhe approaches the Sun, again thewing the Truth of the Retardation in the firft Reflex: on.
§4. Here is an Affirmation without any Manner of Proof, and aga:n too haftily concluded from the Mean of Effects: Indeed their Seafons are always at oppofite Times with ours; yet as they are nearer the Sun, from what has alrcady appeared, in their Summer at $\sigma$, and farther off in their Winter at $v_{f}$, than we are in ours at bf $^{5}$ ard $\sigma_{c}$, and both of us, at tije fame Seafon, receiving the Rays of the Sun at the farre Angle, the'r Summer muft be hotter, and W nter colder, than ours; fo that a Mediuri of Heat and Culd, between us and them at any Time, either in the fame or oppofite Seafons, cannot be at the Equator, except in the Equinoxes; for as they enjoy the Extrem:s of both in a greater Degree than we do. this Mean will at all cther Tenes incline towards them, and be on the South Side of the Equator; the Heat on the South Side while the Cold is on the North, and vice verfâ: Now then, if thefe two Means of Heat and Culd thius alternately paits the Equator to a confiderable D.ffance on eitlier Side, defcribing, as it were, a Zone, the Eq!:atorians do undcubtedly undergo different Degrees of Heat and Cold; infomuch that the Effects of a Thermometcr expofed to the Beams of a clear Sun, abfratting from fubterraneous Heats, or rather, in fome Meafure to prevent this Impediment, a double Convex Lens, applied with like Circumftarces, to the Tbermometer, would not only be very different in different Seafons there; but always much greater (from the Point of Temperate) with our Antipodes than with us, in like Seafons: This, however, I have great Reafon tobelieve frim the Accounts given by Naturalifts, Hiftorians, and Travellere, that I have met with in the Courfe of my Reading: Be this as it will, the Anfwer to the next Paragraph will :fford ancther ftrong In fecence in Procf of it.

## 18 The Rev. Mr. Smith's Letter continued.

§ 5. I have frequently taken the habouring Oar out of his Hands, to prove feveral Negatives, an.I now I anfwer in the Affirmative to his two Quiftions here put in the Negative; it is more immediately incumbent upon me to prove it; which I fhall endeaviour by returning back and continuing cur Reflections: But why he afks tivo Qugftions is not within my Comprelienfion, becaufe the one includes the other; however, I thall addeefs my felf to botis.

Reflex. 11. The two Points $\gamma \bumpeq$ are agreed and fixed upon by Antonomers for the Limits or Boundaries of Summer and Winter; thus, when the Earh is at $\bumpeq$, Summer begins, and continues till it has paffed by is to $r$, where and when. Winter commences, ard continues cill it his paffed by co and arrived again at $\bumpeq$; and becaufe the Sun is then vertical at the Equator, and the Days and Nights every where equal, they have ebtained the Name of the two Equinoctial Ponts. Now the Day begins at the North Pole, and an Equatorian to have the Sun on the North Side of his Zenith, when the Earth is at $\Omega$, and both continue during the Time of defcribing $\bumpeq v$, when the Day at the South Pole, and the Sun on the South of the faid Zenith commence, and continue till it has ar: ived again at $=\ldots$ : But I have manifefly fhewn that, it de frribes thegreateft Half $\sim$ iv $\gamma$ with a retarded, and the leffer $\gamma \sigma \bumpeq$ with an accelsrated Motion; fo that, for thefe two joint Reafons, the Affirmative of his Queftions is, not only reafonable, hut really true in Effect : And the Quantity is had from the Time of the Obfervations at $\gamma$ and $\sim$, between which are $17^{8} \mathrm{~d} .18 \mathrm{~h} .8^{\prime} 35^{\prime \prime}$; this doubled and fubitracted trom $3^{6 / 5} 5^{\mathrm{d}} 5^{\mathrm{h}} \cdot 4^{8^{\prime} \cdot} \cdot 5^{6^{\prime \prime}}$, a tropical Year, there will remain $7 \mathrm{~d} .17^{\mathrm{h}}$ $31^{\prime} 4^{\prime \prime}$, for the Time an Inhabitant at the North Pole has his Diy longer than one at the South Pole; or a Refident at the Equator has the Sun more on the North than on the South Side of his Zenith, or our Summers exceed our Winterc. Which likewife is a Manifeftation of what is in Anfwer to the laft Paragraph.
§6. The whole Diameter of the Earth's Orbit, about 162 Millions of Milee, fubtended an Angle at the fixed Stars of about $47^{\prime \prime}$, called the annual Parallax, in the iaft Age; but in the prefent, by more accurate Obfervations, it is found not to exceed 3 or $4^{\prime \prime}$; nay, fome make it only are Stcond, i, that 64 Millions of Miles at the Stars, the Diftance of his *wo parallel Lines, can fubtend an Angle of no more than about one fingle Second at the Earth; and a little Practice would foon fhew what great and infuperable Difficulties attend the Certainty of meafuring fo small an Angle, even with the beft Inftrumente, efpecially in taking Amplitudes, where fo many Impediments interpofe: From whence we may conclude, that if what he fays is true. as 1 believe it is, yet the Effect cannot be macte to appear; and the whole amounts to no more than di--iding a Hair into a thoufand Parts.
\$7. Let the Orbit tarn upon the two Points $\gamma \bumpeq$ as an Axis $\boldsymbol{y}^{\circ}$ $\approx$ vs $\gamma$ below and $\gamma 5 \bumpeq$ above, making an Angle of $23^{\circ} 29^{\prime}$ with the Planc of the Paper being in the Plane of the Equinoctial, the Orbit will be in that of the Ecliptic, and $\gamma S \bumpeq$ their common Interfection: let us alfo imagine, for the better conveying our Ideas, a Plane always petpendicular to the Planc of the Payer fafing through $S$ the Sun and the

# The Gent. Diary ; or Math. Repofitory. I9 

Earth, which is therefore the Plane of the Solar Meridian ; this moving uniformly in the Equinoctial from lf with the mean Motion of the Erth, will deferibe the Bate of a right angled rpherical Triangle on the Paper, and the Hypothenufe in the Orbit: which is lefs than the Bafe all the Way to $\gamma$, becaufe the remaining part from $\boldsymbol{r}$ is, by the Rules of 'rigonome:ry, greater than that of the Bafe : at $a$, the Middle between W' $^{\prime} \Upsilon$, it fuftains a Lofs or Defeet of no lefs than $2^{\circ} 28^{\prime} 25^{\prime \prime}$, almoit $9^{4} 54^{\prime \prime}$ of Time; from whence it increafes, and both become $90^{\circ}$ at $\gamma^{\circ}$; thence the Augmentation continues to $\beta$, the Middle between $\uparrow \sigma$, and there acquires an Excefs of the fame $9^{\prime} 54^{\prime \prime}$ which it again lofes in going to $\sigma$, and both there become $180^{\circ}$. So in the other half $\sigma \bumpeq 10^{\circ}$ Now equal or mean Time is always meafured by this equable Motion upon Paper or Equinoctial, and the apparent by that in the Orbit or Ecliptic, whish, in other Terms, is, the right Afcention in the Equincctial, and Longitude in the Ecliptic; both thefe cvidently agree in $\nabla^{\circ}, \gamma$, छठ $\bumpeq$; but fince the Plane paffies over any certain Portion of the Equinoctial before a like in the Ecliptic from $V \rho$ to $\gamma$, and from OD to $\bumpeq$, the apparent Time is there ton Now; and, on the contrary, it arrives at any given Point of the Elliptic from $\boldsymbol{\gamma}$ to $\sigma_{0}$ and from $\sim$ to $V)^{\prime}$, fooner than at ore in the Equinoctial, equally diffant from the fame l'oints $\gamma, \bumpeq$; the apparent is then too faff. This Equation, arifing from the Inclination of the Ecliptic to the Equinnctial, was firts brought into Calculation by Tycho Brabe, and thence called the Tychonic Equation: which the fagacious Kepler found not always to correfpond with his Obfervations; and, after he had difcovered the planetary Orbits to be elliptical, added therefore another Equation, arifing from the Inequality of the Earth's Motion in her Orbit, which Inequaliy has manifelly appeared from our Obfervations; we now will confider :his apart with refpect to the Cafe before us, by comparing the true Motion of the Earth in her Orbit with the mean. Suppofe both to commence at $A$, where the true begins to decreafe from the mean, it will have loit in $r 1^{\circ} 55^{\prime} 29^{\prime \prime}$, or $7^{\prime} 42^{\prime \prime}$ of Time (fee Reflex. 6) where it begins to increafe upon the mean, gains the former Defeet of $7^{\prime} 4^{\prime \prime \prime}$ at K , where it again begins to decreafe from the mean, and lofing this Excefs, again becomes equal to the mean at A : whereby it is evidenf, the Plane will, in its Revolution, firft arrive at the true Motion in the Orbit, in going from A $0 r$ and from R to.A; therefore the apparent is there toofaft. Ori the contrary, in going from $r$ by P to R , it will firft pafs the mean Motion ; the apparent therefore is here too Now; fo that if this Equation of the Orbit, called the Profthapberefis, alone obtained, apparent Time would agree with the mean only twice in the Year, viz. when the Earth was at $\Lambda$ and $P$, as this Gentleman afferts from his peculiar. Notiens and Reafunings for a Mean between the Extremes: But fince thefe two Equations are the Productions or Effects of only one fingle $M$ Motion of the Earth in her Orbit, neither of them can take Place without the other ; and muft, therefore, be iointly contidered as acting together, and the Equation thence, arifing will fhey the true Diference.berween apparent and miean Time; wherefore; once more fending the Plane round from A. attended with both thefe Irregularities, it will, irum a littie Confidearion, appesr, that

20 'The Rev. Mr. Smith's Letter continued.



Hence four Times a Year, according to our Syffem, doth the Suo and Clock fhew the fame Time, without the Earth being twice in Ayhelion and Perichelion, to which Abfurcity he has laboured to redace it, but without Succefs, and his wonderful Reafoning for a Mean again fails: Indeed the Admiffion of fuppofing both the true and mean Motions to commence from $A$, as above, rather than from any other Part of the Orbit, may affiord fome Objections; but I fhall deffif from giving their Anfwers till preffed with more Difficulty than at prefent, prefuming it fufficient to remind him ; that, as any Quantity or Mution in paling from a Negative to Affirmative, and the contrary, is fomewhere equal to nothing, the Difference between apparent and mean Time, in our former Obfervation, muft be nothing fomewheie between D, B, Gr, Q and is, $\gamma, \mathrm{P}, \mathrm{D}$ refpactively, which is very confonant to the Times juft now affigned: Befide I have always found this Difference to be juft what it Thould be from an Horizontal Dial, divided into Qurters of Minutes, compared with the Time-piece regulated to mean Time; fo that we have the Facts of Nature, and the univerfal Confent of Aftronomers, to fupport this Suppofition.

His reafoning from the abfolute Motion of the Earth being fafter at P, and flower at A, than mean Time, is not true; for, of two Clocks both going at the fame Inflant trom 12, the one equably, and the other unformly accelerated, or too faft, from 3 to 9 , but as much uniformly rerarded or too flow from 9 to 3 , will he affirm that this, after one or more Revolutions, is flower at 12 , or fafter at 6 , than the reguiar one, becaufe the abfolute Motion at thofe Times is $\mathrm{f}_{0}$ ?

If he is for eftablining circular Orbits, as appears to me, his Memory muft certainly fail him; not only to grant, but fay, that the Earth is nearer the Sun and moves fwifter at one Time than another is not very. confiftent with circular Orbits.
§ 8. Notwithfanding this Queftion is put in the Negative, yet the Affirmative muft fufficiently appear from what has juft been faid, where it was Mewn, that Aftronomers have confidered thefe very 5 wo Circum-
fances he is fo mighty anxious to pur them in Mind of, and in the enly Manner wherein they can agree with the Phznomena of the Heavenly M tions.
§ 9. As I have not fufficient Penetration to difeern wherein the Times of M. De La Caille differ from thofe of other Aftronomers (fet forth in Anfiwer ti) the 7 th Paragraph), I am, with great Reluelance, drawn into a Neceffity of fufpecting either this'Gentleman's Abilities, or my own, in underfanding this Author; who, indeed, no where particulariy treats $0^{\circ}$, or even mention, the Equation caused by the Inclination of the Ecliptic to the Equator, yet refers the other, caufed by the irreguiar Motion of the Earth in lier Orbit, to the Motion in the Equinoctial, comparing it with the right Afcenfion, which at once includes and produces :he Effect of both Equations, perfectly agreeing with other Afronomers; for it amounts to the very fime, whether we confider the irregular Motion of the Eath in her Orbit with Reference to the mean, ant then the Irregularity of this mean again tu that in the Equator, as I have done; or, at unc, to confider and compare the irregular Motion in her Orbit to that of the right Afcenfion in the Equinoctial, as this Author has done; in demonftrating of which, Mr. Bamfeld will certainly deftroy his own Syftem; and eatablifa the very one he labours to rejeet: for the Truth of this, and which of us beft underfands our Author, 1 do, with great Submifion, appeal to every ingenious Artift, of whom I here, once for all, fincerely beg to fet me right whenfoever I fiall be in the wrong.

It really gives me fome Uncafinefs to fee the Motion of the Earth, affigned by the prefent Aftronomers, bearing the hard Epithets of "forced, "compounded, and unnatural ;" where.s it is the moft eafy, regular, fimple, and natural, that can flow from the fpheroidical Figure of the Earth, perfectly confentaneous to his Notions, "Nature performs all her "Operations the fhorteft and eafieft Way"_ "There are not many "particular Intricacies in the regular Courfe of Nature;" and the compleatly keeps up to Horace's - Simplex duntaxat et unum; as will appear Fio ctery one that fhall have the Happinels of removing the prefent Partiality, fo zealoufly attached to the moft fictitious and inadequate Caufer, but, unforiunately Effects of Projection and Attraction in the Heavens, for the Adoption of the real Agents, which God has created to put, preferve, and continue his Machine in Motıon.

I heartily wifh he would make my Eye-fight as good as his, and fee as much; but till he has brought the Earth into a perfect Spbere, he muif expect no fmall Trouble in accomplifhing the Bufinefs; nay, even then I fhould defpair of the phyfical Caufes for fuch a Motion; becaufe 1 firmly believe no fuch are in Nature, and thercupon confidently affirm he cannot fippo:t this extraordinary Affertion, without introducing fome hypothetical Data that fhall deftroy, or, at leaft, enervate the whole Bafis of his Principles.
§ 10. His feventh Paragraph, if I underfand his Meaping, is a full and adequate Reply to this. "For, fays he, when the Earth is neareft "s the Sun, She moves fafter than equal Time; and when fartheft, flower "thin mean Time;" from which different Diftances and Degrees of Motion, muft inevitably follow the two refpective Confequences of the Sun liding different apparent Diameters; and our Summer !onger than

## 22 The Rev. Mr. Smith's Letter continued:

our Winter, even if the Sun be in the Center of the Earth's Orbit: To affirm thefe $\mathbf{P}$ emifes, and deny the r abfolutely confequent Effects, with the Evidence of Demon ${ }^{6}$ ration, is fomeching wonderful; amounting to rothing lefs than demonfrating that the apparent Diameter of any given Object is the fame at all Difiances. viz. Reflex. 8. Will he, in Contradietion to the eftablifned Rules of Perfpective in one Cafe, a plain Axiom in $N^{\prime}$ echanics in the other, and common Senfe in both, fay, that the vifual Angle from a Soire is the fare at the Diftance of one Furlong as a hundred? and that a Body will pais over an equal, if not a greater Space, with a flow Velocity, in the fame Time as another with a greater Velocity?

His refting all Afronomy, and the Objections againft his Hypothefis, upon the different apparent Diameters of the Sun, and our Summer exceeding our Winter by $\&$ Days, certainly proceeds from a Want of due Confderation; for in the firt fix Reflexions, is determined from Obfervations, not only the Form but the very Dimenfions of the Orbit, with every other Requifite, abfolutely and incepently of thofe; $\quad$ riz. Reflex. $7 \cdot$ which only follow as concomitant Proofs in Reflexion 8, 9 and 11. Yet, fuppofe his Denial of thefe two Phrenomena to be true, his Demonfration of it, if it can be fo called, is very, deficient, and comes now to be examined.

## * * To be concluded in the next Year's Diary.

The Rev. Mr. Smith's. Errata of that Part of his Letter publified left Year.
Page 38 , Line $1_{3}$, after witnefs afd $i^{\prime}$; Page 19 , Line 47 , for 10 read to ; Line 49, for but the, read brit this; Page 23, Line 1 and 2, for that Cbjet, and plice anofice of the fume Magnitude at, read it to $\mathbf{j}$ Line 2, for this, read the fame Olyifo.

In the Table of Obfervations.
Jine A, Col. 2, for $29^{\prime} 38^{\prime \prime} r .21^{\prime} 28^{\prime \prime}$; next, for. $24^{\prime}$ r. $25^{\prime}$ iff 9 ; Col. 5 , for $28^{\prime \prime}$ r. $33^{\prime \prime}=6$; Col. 2 , for $28^{\prime} r \cdot 3^{8^{\prime}}$.

Conclufion of Mr. William Chapman's Tables of the Solar Eclipfes, which will be vifible in England till the Year of our Lorn 2000.
rg19. Nov. 22, After. 1920, Nov. 10 , After. 1927, April 8, Morn. yg22, March 28. After 1925, Jan. 24, After. 9227. Tune 29, Morn. : 928 , Nov. 12, Niorn. 3929, Nov. x. Morn. 3936, June i9, Morn. 1939, April 19, After. 1942, Seft. 1c, After. 3945 , July 9 , After. 1949, April 2S, Morn.

| Begin. | Midd. | End. | Durat. | D |  |
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| 3203 | 41732 | 51032 | I 50 c | 30 | 0. |
| 353.1 | $\bigcirc 36$ | $\begin{array}{llll}6 & 3 & 3\end{array}$ | 21030 | 73 | 0 |
| 7391 | 85251 | IO 931. | $2333^{\circ}$ | 048 | 0 |
| I 152 | 2.855 | 25925 | 144 c | 216 | 0 |
| 24721 | 35249 | $454 \quad 9$ | 264 c | 100 | 0 |
| 42911 | -244I | 62541 | 15630 | 116 | 0 |
| 7476 | 8354 | 927 4 | 1400 | 242 | 0 |
| :0 59 if | 11366 | $12: 036$ | 1112 C | 059 | 0 |
| $3554{ }^{\circ}$ | 44210 | $53^{2} 10$ | 1363 C | 642 | 0 |
| 5324 | 62422 | 71252 | 140 c | 442 | 0 |
| 326 f | $4143^{6}$ | 5 - 61 | 137 | 354 | 0 |
| 12475 | $2 \quad 2: 7$ | $3135 \%$ | 226 | 749 | 0 |
| $644 \div 4$ | 74044 | 8413 1́l | 156 501 | 427 | 0 |

## The Gent. Diary; or, Math. Repofitory. 23

19 द2, Feb. 25, Morn. 1954; June 30. Morn. 1259, Oet. 2, Mom.
ICfis Feb. 15, Morn. ig66. May 20, Morn. 19'S, Sept. 22, Mom: 1971, Feb. 25, Mern 1972, july 10, After. 1973, Dec. 24, After. 1975, May'11, Morn. $1_{3}-6$, April 2, Morn. 1082. Dec. 15, Morn. 1!84, May 30, After. 1994, May 10, After. 1996, Oct. 12, After. ig99, Aug. 11, Morn.

| $83^{8}$ \& | 9 II 38 | $94^{68}$ | 18 c | 1 |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | $12383^{2}$ | 2 II 2 | 251 | 939 |  |
| II 26 | 12243 | 12131 | $1553^{\text {c }}$ | 45 |  |
| 639 IC | 74040 | $\mathrm{S}_{4} 64{ }^{\text {c }}$ | 2730 | I125 |  |
| 833 | 936 | 1043 | 2100 | $5^{17}$ |  |
| 93018 | 102718 | 112748 | 15730 | 47 |  |
| S 3738 | 941 : 8 | $10433^{8}$ | 211 c | 754 |  |
| 737 5: | 2122 | 9322 | 12530 | 6 |  |
| 31 | 41936 | 52236 | 21230 | 556 |  |
| $53^{82}$ ( | $6345^{6}$ | 73426 | 1 $5^{6}$ o | 648 | - |
| 942 | 10190 | 1051 c | 190 | 12 |  |
| 72328 | 82928 | 94128 | 218 | 5 |  |
| $5^{2} 45^{\prime}$ | 62329 | 71759 | I 53 |  |  |
| $55^{2} 311$ | 65031 | 74531 | 153 |  |  |
| 19 If | 22818 | 34218 | 233 |  |  |
| $9105:$ | 1027 | 114 | 23640 | 1124 |  |

Of the Eclipses which will happen this Year, 1769. By Mr. Robert Langley, of Hitckin.
Whilf Sol, this Year, through th' 'cliptic ftrays,
Palc Luna near the fame will come,
And three Times intercept the Rays
Diffufed by the radiant Sun :
And Luna likewife will appear
And Oppofition fall)
Two Times in Darknefs, I declare,
To this terraqueous Ball.
The firft is of the Sun, Fanuary 8, at about half an Hour paft 2 in the Morning, confequently invifible

The fecond will be a vifible Eclipfe of the Sun, $\mathcal{F} u n$ e 4, in the Morning ; apparent Time, at the Royal Obfervatory at Grecinwicb, by the Durkem Tables.


$$
\mathrm{R}_{\mathrm{FM}} \cap \mathrm{P}, \mathrm{~K} .
$$

The Center of the Penumbra firft of all, enters the Globe in Neru Britain, where the Sun rifes centrally and totally eclipfed; and purfuing a North Eafterly Direction, leaves that Place near Button's Iflard, at the Entrance of Hudfon's 'Straights, pafling over Davis's Straights, Grecmland, and the unknown Parts about the Nortb Pole: It then takes 2 South Eafterly Courfe over the Icy-Oican, and the North Eait Part 0: Gredi Tartary? leaving it near Saint Larerence': Ifland, and enters the

## 24 Of the Eclipses this Year. ${ }^{1} 769$.

Pacific Ocean, where the Center of the Penumbra leases the Globe, and the Sun is centrally and totally eclipied at feting.

The third is of the Mon, June 19, pat 8 in the Morning, invifible.

The fourth is of the Sun. November 28, about a Quarter pat 8 in the Morning, invifible; by Reason of the Moon's South Latitude.

The fifth and last, is a vifible Eclipse of the Moon, on the $13^{\text {th }}$ of December, as follows:

## h $1 / 1$

$\left.\begin{array}{llll}\text { Beginning } & 4^{\prime} & 57 & 1 \\ \text { Middle } & 6 & 21 & 3^{\circ} \\ \text { Ecliptic } 8 & 6 & 27 & 57\end{array}\right\}$ In the Morning at London.
$\left.\begin{array}{llll}\text { Ecliptic } 8 & 6 & 27 & 57 \\ \text { End } & 7 & 45 & 59 \\ \hline\end{array}\right\}$ Apparent Time, by the Durban Tables.
Duration
$248 \quad 58$
D. gits eclipfed $8^{\circ} 57^{\prime} 9^{\prime \prime}$

Mr. William Chapman rent Calculations of all the Eclipfes at large, together with their geographical general Appearances: That of the Sin on the $4^{\text {th }}$ of $\tilde{J}^{\prime \prime a}$, in the Morning, at Foxton in Lcicellerfire, from the Duríam Tables, is as follows:
$\left.\begin{array}{llll} & \begin{array}{l}\text { h }\end{array} 111 \\ \text { Beginning } & 6 & 35 & 27 \\ \text { Vifible } & 7 & 26 & 54 \\ \text { Middle } & \begin{array}{ll}7 & 27 \\ 1\end{array} \\ \text { End } & 8 & 22 & 47\end{array}\right\}$ Apparent Time.

He alpo lent that of the Moon, on the $1 \mathrm{~g}^{t}$ th of December, in the Morning, for Foxton, from the Durbam Tables, as under :
$\left.\begin{array}{llll} & h & 1 & \prime \prime \\ \text { Beginning } & 4 & 53 & 50 \\ \text { Middle } & 6 & 14 & 50 \\ \text { End } & 7 & 3^{2} & 50 \\ \text { Digits }\end{array}\right\}$ Apparent Time.

Mr. John Edruards also favoured the Author with Computations and Types of the Eclipfe of the Sun, on the 4 th of $\mathcal{F}$ une, as len from Cambridge.

H M
$\left.\begin{array}{lll}\text { Beginning } & 6 & 40 \frac{7}{2} \\ \text { Middle } & 7 & 36 \frac{1}{2} \\ \text { Ends } & 8 & 23 \\ \frac{7}{4}\end{array}\right\} \begin{gathered}\text { Apparent Time } \\ \text { at } \\ \text { Cambridge. }\end{gathered}$ Digits $5 \frac{3}{4}$
Aid alpo that of the Moon, December I 3, in the Morning.
H M


## The Gent. Diary; or, Math. Repofitory. 25

Mr. William Terril, of Relruth in Cornvall, fent alfo the following Calculation of the Lunar Eclipfe, for Clisvance, the Seat of Sir $\mathcal{F} o k n$ Saint Aubin, Barr, and at Redruth.


Mr. Thomas Atkinfon, of Ingbam in the A/bes, Linsolnfbire, fent the following Calculation of the Solar Eclipfe, on the $4^{\text {th }}$ of Yine, by FerEufon's Tables, as it will appeal at Linco'r.
1769. F̛une 4. Morn. Beginning $\begin{array}{llll}h & \prime \prime \prime & \prime \prime \\ 6 & 39 & 20\end{array}$ Apparent Time
\(\left.\begin{array}{llll}Midale \& 7 \& 34 \& 15 <br>

End \& 8 \& 25 \& 19\end{array}\right\} \quad\)| at |
| :---: |
| Lincoin. |

Duration
I 4.559
Digits $50 \frac{1}{2}$
Together with the Lunar Eclipfe, on Dec. I3, in the Morning,

| Beginning | $\begin{array}{llll}5 & 4 & 20\end{array}$ | Apparent Time |
| :---: | :---: | :---: |
| Middle | 62330 |  |
| End | $74340$ | Lincoln. |

Mr. Ricbard Rowvly, of Kirkby M.llory, in Leiceffer/Bire, gives the following Account of the Moon's Eclipfe, from Mr. Abrabam Lord's MSS. Tables, for Kirkby Mallory.


And Mr. William Pbillips, of Silfden, near Skiston in Craven, Yorkfire, fent the following Calculation of the Sun's Eclipfe.

|  |
| :---: |
|  |  |
|  |  |
|  |  |
|  |  |
|  |  |
|  |  |
|  |  |

## Ænigmas in 1768 , anfwered.

Mr. William Cbapman (with Parallaxes from Halley's Tables) has been at the Pains to calculate the Trinfit of Venus (with Types) for Lordon, Petcifburgh, Manilla, and Bofion in Nezv England: That for London is, as under:

App. Time in the Aftern.. Yune 3. $7275_{2}$ Central Ingrefs Middle 103444
Central Egrefs 134428 Sun fet $8 \mathrm{~h} 5^{\prime} \cdot 28^{\prime \prime}$.
Mr. Robert Langley obferves, that this Iranfit will be vifible at Greenzicich, till afier the total Immerfion; that at the Middle the Sun will be vertical in Lat. $22^{\circ} 27^{\prime}$ N. Long. $1 ; 9^{\circ} 10^{\prime}$ W. from Grecnsuich, where the Duration will be the fhorteft. In Lat. $55^{\circ} 44^{\prime} \mathrm{S}$. and the fame Long. its Duration will be the preateft poffible.

Answers to the Jenigmas, sic. in lalt Year’s Diary.
y. A Rainbow.
2. Darkness.
3. Languacie.

4 Birmingham HalfPENCE.
5. A Bird"s Nest.
6. FASHION.
7. An Arrow.
8. A Wind-mill Sails.
9. News.
:o. Prize, a Pair of Breeches.
3. Rebus, A Rake. 2.Tarratt. 3. A Beacon.4.Exeter.) Aniwer to all the Anigmas by Mr. W. Swift ; Addreffed to Mirs Políy Stow. Beauty and Fashion.
Says Beauty to Fashion, as they fot at the Toilette, If I give a Charm, you will certainly fpoil it; 'Tis fo metamorphos'd by your fiddling and fangling, Juft like the Bad Hatfpence we often are handling: 1 farce know my old Breeches when 1 fee them again, (Such Changelings you make, beth of Women and Men!) For, like Windmill-SAils your Head does turn round, 8 And with a fair Speech you the World do confound! 3 Now, What have you done? you'll fay full enough, For you daub 'em with Gold, fine Lace, and fuch Stuff: Your Head, like the Rainbow, all Colours will beat, With Ribbons and Trappings to fly in the Air Or, like a Bird's Ns.st, clofe; or ruffled in Hair!.
Without Handkerchicf now; then Darkness with Ruff,
Now plain as a Quaker; foon all of a Puff:
Juft like Cock on the Steeple that fhews you the Weather, foys are hardly the fame for two Days together:
Jou fly fvift as an Arrow when fent from the Bow; 7 And changc like the News.-What think you, Polly Stow? 9
Anfwer to all the $\not$ Enicmas by Mifs Poliy Stow ; Addrefled to Mr. W. Szuiff. Fashion and Beauty.

Mifs Fasmion to Beauty; the fmiling reply'd,
Who does mofl for the $S e x$ ? Let it fairly be try'd:

## The Gent. Diary; or Mith. Repofitory. 27

And they that look round 'em will prefently fee
No Birwingham HALEPENCE will buy aught for me. ..... 4
I grant it indeed; mighty Favors you boaft.
But how fanty are they !-How fcarce is a Toaf !
A Shape, a Complexion, you confer now and then,
But, to one you give either, you refufe it to ten;
For, if once you fucceed, you much oft'ner do fail
For, if once you fucceed, you much oft'ner do fail
Here jour Rofe is too Red; there your Lily's too Pale ..... $\} s$
Your Head's full of Conceit, and turns like Wind-Mili Sail.
For fome Feature or other is always amifs,
And pray let me know, when you've finifh'd a Piece,
But what I was oblig'd to correct, or touch over,
Or you never would have either Hußband or Lover : ..... $I$
Tho' your Face (as the Rainbow) may beauteous appear, ..... 7
And your Eyes like an Arrow dart all the whole Year;
Yet, I hope (my fair Lady) you do not forget,
Tho' you find the Thread, that its I make the Net :
Don't famble in Speech, Mifs.-It muft be allow'd
That Woman is nothing-unlefs A-la mode;3
Neglected fhe lives, and no Beauty avails;
(For what is a Ship, without Rigging and Sails ?)
rou'ré buried'in Darkness (my beautiful Miis)2
Unlefs I afiift you, you can't deny this:
Your Nympls, with their Shapes, Complexions, and Features,
What are they without me? -but poor aukward Creatures!
Juft likea Bikn's Nest which unfin:hid lies,
5.
Or an old Pair of Breeches all torn in the Thighs. ..... Prize
The Rout-the Aliembly-the News-will jou tell ..... 9
'Tis I form the Beau, and I finifh the Belle:
So I think with your Beauty you'd maike but bad Shift,
Unlefs FaßBion attend it-'eant it fo, Billy Swift.
Friend Rachell Bell, of York, fent the following general Anfwer to all the AEnigmas, in a Defeription of a rural Scene.When Sol's bleft Radiance paints the orient Skies,And gloomy Darkness to the Weftward flies;2
When ev'ry Leaf and Flower's bepearl'd with DewAnd blooming Verdure decks the Fields anew:
The feather'd Songfter quits his downy Nest, ..... 5
And with fweet Language trills his Brood to Relt; .....
3 .....
3
The Rain bow's vivid Hues his Plumes adorn. ..... 1
The beauteous Fashiun of the fragrant Morn: ..... 6
No News nor Noife difturb the placid Scene,
9
8
9
8
Nir Storms annoy the Mile-Sails on the Green:
The Miller thus being difengag'd from Cares;
To Neighbor Collin chearfully repairs,
With Bow and Arrow, at a Mark they froot, ..... 7
And for the Prize moft eagerly difpute:
A Pair of Breeches, with fome Halfpence bad ..... $\boldsymbol{P} ; \dot{z}<0$ The fure Reward is, for the Vigfor Lad.
Mr. Gcrvas Alams, of Alviaficn near Derby, fent the Anfwers to all the Kinigmas, as follows.
The Rainbow Friend $I$ angloy endeavors to hide ..... 1
But like Turner in Darkness f'll never be tied; ..... 2
Then $V^{\prime \prime}$ lld's is good Language (which butfew underfand) ..... 3
And Hubbaid's Bad Halfpence, made ready to's Hand: ..... 4
Next Vaughan's a Bird's Nest; I plainly do fee ..... 5
6
That Swift with the Fashion will always agree.
7
The next is an Arrow (if I hit the Mark ftill) ..... 8
Then Sevift with his fccond, as fwift as News flies; ..... 9
And Weft (with his Breeches) difguifes the Prize. ..... 10
2 Mr. Fobn Ramey fent the following Anfwer to the REnigmas.
When the Rainsow appears, nu Darknesscan be; ..... 1.2
Expunge your bad Halffence:-good Language forme! ..... 4. 3
Vaugban builds a Bred's Nest upon an old Wall; ..... 5
And then makes an Arrow to kill the Birds all. ..... 7
The Coqucties in the FAshron, much News they muft tell, ..... 6.9 With Wind-Mile head Sails, and 'rongues mighty fell, ..... 8They 'll tell you long Stories of Fairies and Witches;
And fometimes who fought the good Man for his BREECHES. ..... Prize.
All the 在nignaas anfwered by Mr. Fames Brown Afiton, of Lincoln.The Storm.Mild was the Ere, and ev'ry Scene was gay,But lo! as Pkobus funi into the Weft,The gaudy Rain bow his high Throne aflum'd,A certain Sign that Storms would foon enfue :Ev'n fo it hap'd, the Skies all cloudy turn'd,And fable Darkness fpread its Mantle round,$\approx$
And all was dread; - The Winds began to roar,And teeming Show'rs of Rain impetuous feilWith rattling Hail-The forked Light'ning thone,And dreadful Thurders roll'd with awful Speech.3The heavy Threat'nings of an angry GodMade all afraid; the * base degen'rate Man,4
Or Atheift wild, now own'd the Lord fupreme!The Fashionable Beau, in gaudy $+\mathrm{D}_{\mathrm{ress}}$,Who jut before was boafting of his Pow'r,Now tremb'ling ran for Shelter to his Head;Nor Man alone was frail: the Feather'd RaceFlew to their Nests for Shelter from the Storm,$\xi$
find round the Plain the Beafts all lowing ran.
it now a while fubfided, then again As tho' by Strength renew'd began afrefh; Red fiery Thunderbolts like Arkows fell ..... 7
And fpread with Horror Defolation round.The Winds as tho' enrag'd vehement warr'd

- Biraingk and Halfpercs.+ Aliuding to Brecrbes.6. Prize3




## The Gent. Diary; or, Math. Repofitory. 29.

And by the Roots tore up fome lofty Trees
And Houfes overtuin'd, with Steeples high;
And from each Mrie tore off the lab'ring Sail. 8
At length its Pow'r declin'd ; th' impetuous Rain,
And rattling Hail, with Thunder's dreadful Sound,
Fntirely ceas'd, and all again was hufh'd.
But here the Terror did not quite decline,
For, by the weekly News, it was refum'd;
To read the dire Defolation done,
1 iight fill each mortal Breaft with Dread and Fear, And from their Hearts draw unaffected Pray'rs That fuch a Storm may ne'er be felt no more.
All the 价nigmas anfwer'd by Mr. Jobn Colledge, of Weft Haddon.
Langley has well difguis'd the Rainbow's Charms, I
Tuiner on Darkness ev'ry Bofom warms; 2
Wild's Speech is void of Fiction and Deceit, 3
But Hubbard's Coin is bafe and counterfeit: $\quad 4$
$V$ Gugban's Bran's Nest originally fhines, 5
Squift's is the FASHION, in old fafhion'd Lines. * 6
Vauglan again comes arm'd with Cupid's DAR T, $\quad 7$
Polly on Windmil's Saits is fweet and fmart: $\quad 8$
The Nintb's ambigious, and compar'd may be
To Ligbt or Ligbt'ning; News, or Letter T;
9 Now fay, ye Bards of 'h' Enigmatic Trade. Are not the Breeches (think you) neatly made? Prize

A हeneral Anfwer to all the Rebufcs, by Mifs. Polly Ajbton, of Swinethorpe.
Not all the Wits that Exeter can boaff. Can vie with Tarrat; He remains the Toalt Can vie with TARrat; He remains the
Of all Diaria's Sons, both gay and fage, Which Rakes acknowledge, tho' they're fir'd with Rage; 1 His Works confpicuous thine, like Beacon's Blaze;
Of all Diaria's Sons, he merits Praife.
Mr. James Mille, of Brixzortb, anfwers all the Rebufes in a Father's advice to his Daughter.
Be fure, my Ckild, to fhun a R a a E, I
Or you'll repent it when too late;
A Man of Senfe will give you Peace
(May Tarrat's Friendihip never ceafe.)
If e'er abroad you chance to ride,
May Truth, like Bracon, be your Guide :
And always Virtue's Ways perfer
Before the Beaus in Exeter.

* See the Lniver fol Magazire for March 74 S.


## The Paradoxes answered.

I. Paradox anfivered by .1. D. Wi;bana.

Divide a Circle into Seven equal Parts, and draw the chord Lines $\mathrm{AB}, \mathrm{BD}, \mathrm{DC}, \mathrm{CE}, \& \mathrm{c}$. Then by drawing Chords in the fame Manner to the two inward concentric Circoles, together with the Lines AI, CK, sic. and it is done.

Mr. Sreijf, of Stozv, alpo Sent a Fig. to Solve it.

Mr . Fol :n College gives the Scheme annexed, in Answer to the fecond Paradox.

Behold the Scheme, once known to none but you, Stands here exhibited to pubbic View.

No Anfwers came to the third Paradox.


Answers to the Queries.

1. Quere, anfwered by Mr. George Lodge.

Both Parties, it is certain, diftrefs the Poor greatly; and it is hard to Kay subich does it the mort. - Now the Monopolizers oft make a Scarcity in the Midft of Plenty, 'lis true ; yet they help the Poor to Corn, tho' at an extravagant Price : whereas, when it is exported, it can yield no Relief to the Poor at any Rate, being quite gone: Wherefore I think the fe left diftrefs the Poor the mort; for certainly it is better to have Corn at an advanced Price, than to have none at any Rate.
2. Quere, anfwered by Mr. William Swift the Propofer.

This Cuftom, in my Opinion, proceeded at firft from observing that Inftinet in thefe fagacious Infects to return to their Hives, when they are out at Labor, at the Approach of a Storm : the Air at that Time undergoing a very fenfible Change in its Denfenefs, they are undoubtedly apprehenfive of the approaching Danger, and immediately repair to thin Cattle of Security.

## The Gent. Diary ; or Math. Repofitory. 3 r

The tinkling of a Mortar has fomewhat a fimilar Effect on them, as it in fome Meature condenfes the circumambient Air, fo far as the Sound extends : but the Fugitives then having no Plare of Retreat, being driven from their Hive by the old Swarms, are obliged to feek Security on whatever they find any Way convenient for them.
3. 日ever, anfwered by Mr. Gco. Langley, of Wiangle, Lincolnhire.

The firit Difcovery of the hot Wells appears to be of a very ancient Date. In the King's Latb at Bath, is a Statue of King Bladud (whom Mr. Cumbden calls the Soothrayer) with an Infcription under it, importing that He difcovered the Ufe of thefe Baths 300 Years before Christ. Sce Boaiutics of Englaiad, publifhed by Mefl. Davis and Reymers.

> New 在nicmas to be nnfwered in the next Year's Diary.
> 1. Ainigma $2 ; 0$, by Mr. 70 fipb Roultbee, of Tbringston. When Sol in fouthern Seas his Glory hides, And dark'ning Fogs furround the Mountain's Sides : When cold bieak Winds fiweep thro' the lowr'ing Skies, And dead the vegetable Kingdom lies, Out of my Cell I creep, and with my Train In hoftile Form affert my wide Domain ; But think not (tho' the naked Truth I tell) Six Summer Months confine me to my Cell: Am I an Hermit? If fuch charge you bring, I foon fhall make you know that I'm a King ! In fplendid Robes of Majefly I fhine: The Crown, the Scepter, and the Clube are mine. Yot chiefly amongit Fools my Empire lies, 12 m not much regarded by the $W$ ife. The Foes are many that difpute my Reign, With mighty Wars we fhake th' embattled Plain: Greatly I conquer; tho' fometimes I yield, And Crimfon Dyes befpread the well-fought Field. My Followers (obedient at Command)
> Are firty $\{e v ' n$, and arm'd with Clubs they ftand; Tho' (Truth I tell) there's one among my Train Who dares ippofe me; furly, proud and vain And turbulent; regardlefs of my Frown He lifts his Club, and often knocks me down! But (when Time ferves) I vindicate my Throne, And the black Varlet hath my Fury known : For foon I rife, in Majeity array'd, Again grow terrible-and am again obey'd.
II. Ænigma 231, by Mr. Matberw Flinders, of Donnirgeina A queer Kind of a Thing you'll think that I am When you have heard my Tale; tho' as meek as a Lamb: I am odd, yet of a very great USe I declase Humble Servant to yo:l Cents, as well as the Fair Sev'ral Eyes I poffefs, and they're all in a Row, And into one of them my No?e ofrendoes go i

## 32 New IEnigmas, to be anfwered next Year.

Such an odd Prank as this you'll think on with Surprize,
That one's Nofe fhould be thruft into one of his Eyes!
Some wide gaping Mouths too to me do belong
'Tho' for numerous Mouths I've got never a Tongue:
Yet they certainly filling require (that agreed on)
I am fed with fuch odd Food as Men never feed on;
From Places far off, alfo threfe that are near
From this Place and that Place, from here and from there,
My Food is collected.-Sometimes I am lean,
And quite thin and meagre-Anon I am feen
Fed with choicen of Food; but as frequent am fat
With bad ftuffing as good, what think you of that?
I'm moft commonly Beaui/h, and wear a lac'd Coat
But fomstimes quite Sbabby, and fcarce worth a Groat:
Much belov'd by my Mafter and Miftrefs am I,
For by Chance if I'm loft-they're ready to cry !
Nay, fo much I am priz'd by the buftling Throng
That I've often been ftolen, as pafling along: So Adiell, my dear Gents-for I don't ith' Ica!t fear But my Name will be fhewn in this Di'ry next Year.
III. IEnigma 232. by Tbomas Vauglan, M. A.

I am at a Lofs the Reafon to explain,
Why I'm left out by all the Riddïng Train:
I'm Captain of fome hundreds, you mutt know,
My Brethren all; they follow in a Row:
Yet ne'er o'ertake me: Is it not a Wonder
None of us meet, tho' never far afunder ?
I do precede then all; yet can't deny
Many of them are longer far than $I$.
Me fev'ral of my Brethren often do
Outhine in Beaty, and in Sweetnefs too ;
When Sol does frew himfelf to mortal Sight
And gilas the Heav'ns with his refulgent Light,
One of my Brethren always does appear
Yet I, their Chief, but once or twice a Year:
Take this one Hint the Myftry to unfold,
I'd but one Name, but now I've two, you're told:
If yet I'm not found out-Gents, don't difpair,
Look in your $D i^{\prime} r y$, and you'll find me there.
IV. Enigma 233. by Mr. W. Wyd, Author of an Effay on the Character of Manilius in an Epittle to 7 uvenis, in which is attempted a Defcription of the Diftreffed, the Mifcr, and the Liberal; with!other Epiftles on feveral Subjects in blank Verfe, lately publifhed-Printed for the Author; Sold by Meff. Ricbardfon and Urqubart under the Royal Exchange, Mr. Nicoll in St. Paul's Church-Yard; and Mr. Bladon in Pater Nofter Row. Price 1s. 6d.

To trace my Lineage and defcribes my Birth, Relate my Rife, or boalt inherent Worth,

## The Gent. Diary; or Math. Repofitory. 33

I choofe to wave- Ye Wits, let this fuffice,
I ne'er was yet detected of a Vice:
Tho' grave Divines to me fometimes compare
Earth's gay Enjoyments, and their pompous Glare:
'Tis true, like it, J'm of a globous Form
But ufe no Guile my Lovers Eyes to charm :
J much depend on human Pow'r and Skill,
The Slave of Shew, obedient to your Will :
Whillt I exift, I need no borrow'd Grace,
Since native Beawties beam around my Face;
There, fweetly blended, various Colours glow,
'Tho' far exceeded by the Heav'nly Bow;
But foon, ah foon, my fhining Glories fade
And in a loathfome wat'ry Tomb are laid.
V. Ænigma 234, by Mifs Polly Storv, of Stow. Leaft of all Numbers, yet do get (Believe me, Sirs, you may) Vict'ry o'er Kings, and them defeat : So tell my Name, I pray,
VI. Ænigma 235, by Mr. William Swift, of Stozv.

All Ladies court my Beauty bright, And like my Face to fee :
Tho' I am blind and have no Sight, Moft pleafing yet I be.
I'm ferviceable to the Queen (In Silver I appear), And in her Chamber may be feen All Months throughout the Year ${ }^{\text {d }}$ So, what I am, kind Sirs, pray fay, And clear up ev'ry Doubt: I'm Flattery'sFriend--by this you may Soon find th' Ænigma out.
VII, Enigma 236, by Mr. Fohn Poto, of Hawick, Roxburgh-Shire ${ }_{3}$ Scotland.
I can neither eat nor drink; I often fpeak, but never think: I fcarcely ever tell a Lie; yet teach you how to live and die.
VIII. Enigma 237, by Tbomas Vaugban, M. A. At firft I from my Mother's Womb with Violence was torn; Then fentenc'd to fo hard a Doom I'd rather ne'er been born : I'm beat, and bruis'd, and knock'd about, with Inftruments of Steels And into Pieces often broke, fo hard with me Men deal:
Then, after they have us'd me fo, I fill have more to bear ! 1 Martyrdom muft undergo (they burn me I declare!)
Not wearied with tormenting me, they ftill purfue their Game; I after this muft drowned be, then I lofe half my Name. But, for this defp'rae Ufage then, I oft with them quit Score, And fometimes burn thofe very Men, that martyr'd me before. Wou'd you believe it, many Ways, I Frendfhip fhew again, And Monuments oft help to raife to celebrate great Men.

## 34 New Ænigmas to be anfwered next Year.

I can difpel Sterility, by my prolific Art;
And caufe a vaft Fertility almort in ev'ry Part.
What I've endeavour'd to conceal ; now, Gents, with all my Pow'r;
I do not doubt but you'll reveal, in lefs than half an Hour.
IX. Anigma 238, by Ignotus of Hull.

When I to you (ye Bards) my Tale relate,
You'll find I'm old, and of an ancient Date;
Before the glitt'ring Stars their Light difplay'd
Or Earth from Cbaos into Form was made;
Ere Sol had ting'd the Clouds with burnifh'd Gold
Or murm'r'ng Streams in fweet Meandres roll'd;
I had a Being-Angels by me fell,
Eternal Vengeance funk them down to Hell.
Stirr'd up by me, rebellious Powers arofe
In haughty Pride the King of Kings t' oppofe:
On Heav'n's wide Champaign the Battalia lay
Angelic Legions rank'd in dread Array:
Thus, firft to Sin I drew the Sons of Light,
But foon defeated took myfelf to Flight ;
And while I fled, with all the Hoft fubdu'd;
Victorious Angels triumphant purfu'd :
No Place was found to harbor my Retreat,
Their mighty Arms deftroy'd my lofty Seat ;
Drove to the Verge:-with hidecus Shrieks of Woe
Hurl'd headlong, flaming, to the Realms below.
When conqu'ring Rome made mighty Nations yield,
And Kings in Vaffalage their Scepters held;
Fir'd with heroic Deeds, two Rivals burn
To grafp the Globe, and call it all their own ;
The Warriors frown'd, and each exalted ftood,
By Me, each waded e'en thro' Seas of Blood!
I charm'd their Eyes, and their whole Souls infpir'd,
While Thoufands fell, and flaughter'd Heaps expir'd:
Stirr'd up by me, they wag'd decifive War,
To ride triumphant in my gilded Car .
But Pompey fell-I prov'd his Overthrow,
And made the Romans to great $\mathcal{F}$ ulius bow;
Then rais'd the Hero to immortal Fame,
And made the Globe refound with Cafar's Name.
But, when I led him to th' imperial Crown
He from meridian Glory tumbled down :
Then, Man, beware! my Pageantry deride;
For all my Show is empty Pomp and Pride.
X. Enigma 239, by Mr. FobnColledge, of Weft Haddon, near Northamp. ton, being the Prize AEnigmator this Year if6g (to be anfweed before ad February.)

Ye Britijh Bards! I as a Stranger come, Whofe chier Concern in Bufinefs-is at Home;

## The Gent. Diary; or, Math. Repofitory. 35

Tho' many Times compell'd ahaoad to ftroll
O'er fundry beaten Tracks-exempt from Toll :
The verdant Mead and flow'r-befpangled Plain
Render my Efforts frivolous and vain:
For, when I travel (let it not furprife)
Thick Clouds of Duft and noxious Vapors rife.
I vifit oft where wealthy Crouds refort, And am (in Fact) a fav'rite Friend at Court ! Where I, by ftricteft Rules of decent Pride, Have gain'd Admittance at the Qu Een's Bed-fide. In Oxford too (believe me) I am known At all the public Offices in Town; The College and the Study I attend, And to the Church of England am a Friend. But, how precarious is the Will of Fate? Relating to th' Affairs of Cburch and State ! Decay'd by Labor-and decrepid Age, From all thefe Honors I muft difengage: And then, fome Youngster of my kindreds Race Will (Pboenix like) ftart up, and take my Place. That graceful Beard which once adorn'd my Cbin, By flow Decline, looks ghaftly, weak, and thin. My waving Locks, by Length of Time decay'd (Which my ftern Agent fails not to upbraid). When thus 'tis with me (Gents) you need not wonder To fee my Head and Body ftruck afunder !

Now, if you hope to merit true Renown, "Declare my Name"-and wear Apollo's Crown.

New Rebuses, Paradoxes, Queries, Flowers; \&c* to be anfwered in the next Year's Diar y.
I Rebus, by Mr. F. Gleed, of Donington, Lincolnfhire.
The Man for Aritbmetick formerly fam'd; A Sorcerer blind, who in Scripture is nam'd; The Fifh that in fre?h and falt Water refides; A Part of a Nut you muft then add befides: To th' above pleafe to join what always is feen In the Heavens above when the Day is ferene:
Th' Initials of thefe when you rightly have join'd Will name a fweet Fair one, endu'd you will find With many Perfections of Body and Mind.
II. Rebus, by Mr. Fobn Bayley, of Middleton, Yorkifire.

What rapidly runs round each Day, What (tho' defir'd) for none will fay; A Fowl, which larger few there be, A. Fifh the greateft in the Sea:

Th' Initial join, and you'll forn tell
A Diarian's Name, whofew excel.
III. Ie bus, by Mifs Polly Agon. A brutal Race, which Sacred Writ record; An Idol by the Saxons much ador'd: To there, two thirds of a known Pulse unite, And you'll the Place find where 1 breathe and write.
I. Paradox, by Mr. A. D. Witbam. As thro' the Neighb'ring Woods I mulling rove, I oft retire unto a Shady Grove; Where only thirteen lofty Trees are feer Which form, in Order plac'd, juft Rows nineteen: 'Three Trees (I think) in every Row appear; Artists, explain this Problem the next Year.
II. Paradox, by Mr. William Swift of Stow.

A Man that was young at threefcore and ten, He gave it me in and wrote it down then, His Friend was more old at twenty and two (You may think it falfe; but "tic certainly true); Ye Diarian Wits, this Secret unfold:
For old died young, and young he died old.

## I. Query by Mifs Polly Store of Stow.

What Paffion is the mort that can Prevailing be o'er mortal Man?
II. Query by Mr. Tho. Walker, a Writing Mafter \&c. at Knarefkere.

If a Man fhould throw himfelf from the Top of a high Tower; doth he fall to the Ground by Attraction, Compreffion, or Gravitation?
III. Query, by Mr. James Mills, of Brixworth, near Northampton.

Were there any Heathen Temples before the Tabernacle? And whe, the the Tabernacle was built in Imitation of them, or they of that?

A Nofegay of Flowers, prefented by Corinne, to Miff Polly Stow.
To lull Matter afleep what the Nurfe often does Add Latin for and, it's as feet as a Rofl. Place next your Man's Name with one Letter left out And a Feather that's oft us'd by Lovers no doubt, What now-a-days forme call a good Country Dame, What Gents wearinthe Morning and Clowns when they'relame;
Two fifths of what Students are left to the Care of ; And a Feature I now rob the Face of the Fair of; What Courtiers are always well known to profess But feldom, if ever are found to poffers; Pick next (dear Miff Stow v) what forme wish to recall And with the fe drefs the Flow'r Pots that ftand in your Hall.

## The Gent. Diary; or Math. Repofitory. 37

Answers to the Questions in laft Year's Diary.
(1.) Queft. 305, anfwered by Mr. William Forrefer, 2 Serjeant in the firt Regiment of Dragoon Guards.
From firf Equation $z=37-x-y$; put $v=37-x$, then $z=v-y, z^{2}=v^{2}-2 v y+y^{2}$, and $z^{3}=v^{3}-3 v^{2} y+3 v y^{2}-y^{3}:$ $x=37-v, x^{2}=136 q-74 v+v^{2}$, and $x^{3}=50653-4107 v$ $+111 v^{2}-\tau^{3}$; fubflitute the Value of $z$ found above in the 2 d and 3 d Equations, and we fhall have $2 y^{2}-2 v y+v^{2}+x^{2}$ $-509=0$; and $3 v y^{2}-3 \cdot v^{2} y+v^{3}+x^{3}-7675=0$; and by the Method of Extermination (fee p. 120. Emerfon's Algebra) from laft two Equations $a=2, b=-2 v, c=v^{2}+$ $x^{2}-509, f=3 v, g=-3 v^{2}, b=v^{3}+x^{3}-7675$, therefore $b f-a g=0$, confequently $b b-c g=0 ; \quad c=3 v^{2}+3 \tau x^{2}-$ $1527 v, a b=2 v^{3}+2 x^{3}-15350 \because c f-a b=v^{3}+3 v x^{2}-2 x^{3}$ $-15270+15350=0$. An Equation clear of $y$; and by fubflituting the Values of $x$ before found into this laft Equation, and proper Reduction, we fhall have $v^{3}-74 v^{2}+$ $1799 v=14326$; whence $v=19$, and $x=18, y=11$, $z=8$; and the Age required is found to be 18 Years, ${ }_{11}$ Months, and 8 Days.
The fame anfwered by Mr. William Stepbens, of Redruth.
Let $s=37, m=509$, and $n=7675$.
per Tranfp.
$\left\{\begin{array}{l|l}1 & x+z=s-y \\ 2 & x^{2}+z^{2}=m-y^{2} \\ 3 & x^{3}+z^{3}=n-y^{3}\end{array}\right.$

| 1 (0) | 4 | $x^{x^{3}+3 x^{2} z+3 x z^{2}+z^{3}=s^{3}+3 s^{2} y+3 s y^{2}}$ |
| :---: | :---: | :---: |
| - 3 | 5 | $3 x^{2} z+3 x z^{2}=i^{3}-35^{2} y+35 y^{2}$ |
| $\times 2$ | 6 | $x^{3}+x z^{2}+\frac{1}{2} x^{2}+z^{3}=m s-m y-s y^{2}+y^{3}$ |
| - 3 | 7 | $x z^{2}+z x^{2}=m s-m y-s y^{2}+2 y^{3}$ |
| $7 \times 3$ | 8 | $3 x z^{2}+3 z x^{2}=3 m s-3 m j-3 s y^{2}+6 y^{3}$ |
| 5 | 9 | $6 y^{3}-3 s y^{2}-3 m y+3 m i-3 n=s^{3}+3 s y^{2}$ |
| $\pm 6$ | 10 | ${ }^{3}-37 y^{2}+430 y=-1584$. Solved $y=$ |

Whence the Age $=18$ Years, 11 Months, and 8 Days. C 3
(2.) Queft.
(2.) Quef. 306, anfwered by Mr. Gervafe Cliff of Rud. dington; addreffed to Mr. Atkinfon of Ingham, in Lincolnfire.

Your Charmer's Fortune (by Algebra) is found
To be juft five and twenty Hundred Pound ;
Her Age likewife $i t$ maketh to appear
To me to be, exactly eighteen Year :
Her Height in Inches (if my Anfwer's right)
Wants only one to make it Fify-eight :
Therefore, kind Sir, if you intend to wed,
l'd have you take that Lady to your Bed.
The fame anfwered by Mr. Henry Flock, of Bladon, near Nerwcafle.

$$
\left\{\begin{array} { l } 
{ 1 }
\end{array} \left\{\begin{array}{l}
x^{2}+x^{2} y^{2} z^{2}=6579225000324=a \\
2 \\
x^{2} y^{2}+y^{2} z=6=20307302676 \text { (and not, as print- } \\
\text { ed in Diary) per Queft. } \\
3
\end{array}\right.\right.
$$

$=\div y^{2}|+| \begin{aligned} & x^{2}+z^{2}=\frac{b}{y^{2}} \\ & z^{2}-1\end{aligned}$
3-
$4+5 \quad 6 \quad 2 z^{2}=\frac{b}{y^{2}}+c-a$; and $z^{2}=\frac{b+c y^{2}-a y^{2}}{2 y^{2}}$
$4-5|7| 2 x^{2}=\frac{b}{y^{2}}+a-6$; and $x^{2}=\frac{b+a y^{2}-c y^{2}}{2 y^{2}}$, by fub-
flituting thefe Values of $x^{2}$, and $z^{2}$, in the firt Step, and reducing, we have ${ }^{y^{4}+\frac{2 a-2 c y^{2}}{c-\left.a\right|^{2}}}=\frac{b^{2}+2 b}{c-\left.a\right|^{2}}$, and folved by the Method for Quadratics, $f=57$; and from thence $x$, and $z$, are readily found $=18$, and 2500 refpectively: confequently the Lady's Age is 18 Years, her Height 57 Inches; and her Fortune 2500 Pounds.
(3.) Queft. 307, aniwered by Mr. George Lodse, at NeruMarket School.
As $z$, by Infpection, appears larger than $v$, and $y$ larger than $x$; put $m+n=z, m-n=v$; alfo s+r=y; $s-r=x$, and the given Equations will ftand as follows:

The Gent. Diary; or Math. Repofitory. 39

| Viz. |  | $\sqrt{m-n}+25+m+n=36,732$ |
| :---: | :---: | :---: |
|  | 2 | $\sqrt{-r+s}+2 m+r+s=27,7416$ |
|  | 3 | $\sqrt{r+s}+2 m-r+s=25,1231$ |
|  | 4 | $\sqrt{m+n}+2 s+m-n=36$. |
| 1-4 | 5 | $\sqrt{m-n}-\sqrt{m+n}+2 n=0,732$ |
| 2.3 | 6 | $\sqrt{-r+s}-\sqrt{r+s+2 r}=2,6185$ |
| Whence | 7 | $m=3,5 ; n=, 5 ; s=15,5, r=1,5$ |
| And | 8 | $v=3 ; x=14 ; y=17 ; z=4$. |
| $\because$ | 9 | A Cord is the fatal Remedy. |

Mr.William Reynolds fent the following Anfwer to the fame.
It appears from Algebra, that $v=3 ; x=14 ; y=17$, and $z=4$ : Whence I find Cord.

It feems poor Sudlorw has a Cord in View,
To cure his Grief-He'll bid the World adieu:
Oh foolifh Man!-Pray be advis'd by me, Rather than hang thyjelf; go - hang up She.
(4.) Queft. 308, anfwered by Mr. Robert Langley, of Hitckin.
Let $p=$ the given Periphery, $x=$ the tranfverfe, and $y=$ conjugate Diameter. Then (per Conics) $x: y:: y:$ $\frac{y^{2}}{x}=$ Latus Rectum ; and $\sqrt{\frac{x^{2}-y^{2}}{4}}=$ Diftance of the Focus from the Center of the Ellipfis. $\because \frac{y^{2}}{x} \times \sqrt{\frac{x^{2}-y^{2}}{4}}=$ $\sqrt{\frac{x^{2} y 4-y^{0}}{4 x^{2}}}$ is a Minimum (per Queft.) But $2 \sqrt{x^{2}+y^{2}}$ $+\frac{y}{3}=p$; whence $x^{2}=\frac{9 p^{2}-6 p y-35 y^{2}}{36}$; writing this in the Minimum above, gives $y^{4}-\frac{3^{5} y^{6}}{c p^{2}-6 p y-35 y^{2}}$ a Minimum which fluxed and reduced, gives $81 p^{2}-108 p^{3} y-1080 p^{2} y^{2}$ $+690 p y^{3}+34^{3} 5 y^{4}=0$. Whence $y$ may be determined.
(5.) Queft. 302, anfwered by Mr. Ed. Smith, of Baldock.

By the Queft. the arifing Points of the Ecliptic were the $26^{\circ} 4^{\prime}$ of Cancer, and $17^{\circ} 23^{\prime}$ of Leo; whence the Declina-

$$
{ }^{C} 4
$$

tions

40 Queftions in r768, anfwered.
tions are $20^{\circ} 59^{\prime}$; and $15^{\circ} 40^{\prime}$, whofe Tangents let be $a$, and $b$; and $n$ the Sine of $30^{\circ}$, the Afcenfional Differences; and $x$ the Cotangent of the Complement of the Latitude ; then, as Radius $1: x:: a: a x$, the Sine of the Afcenfional Difference of the $26^{\circ} 4^{\prime}$ of Cancer ; again $1: x:: b: b x$ the Sine of the Afcenfional Difference of the $17^{\circ} 23^{\prime}$ of Leo. 'Then by Emerfon's Trigon. Prop. 6. $a x \times \sqrt{1-b^{2} x^{2}-b x}$ $\times \sqrt{1-a^{2} x}=1 \times n$; reduced, \&c. we have $\overline{a^{4}-2 a^{2} b^{2}+64}$ $+4 n^{2} a^{2} b^{2} \times x^{4}-\overline{2 n^{2} a^{2}-2 n^{2} b^{2}} \times x^{2}=-n^{4}$; in Numbers compleating the Square, \&c. $x=.7791 ;$ true to the laft Figure, the Cotangent of $37^{\circ} 55^{\prime}$. Whence the Latitude of the Place is $52^{\circ} 5^{\prime}$; and the arifing Point of the $26^{\circ} 4^{\prime}$ of Cancer in the Ecliptic, is 50 minutes and 28 feconds pait $40^{\prime}$ Clock in the Evening.
(6.) Queft. 310, anfwered by Mr. Fames Young, of Newton, Nortbumberland.


Let $2 a$, and $2 b=$ the tranfverfe and conjugate Axes of the Spheroid; alfo let $x=\mathrm{AG}$, and $y=\mathrm{FG}$; then will $2 a-x=G B$; furthermore, let $p=, 7854$. Then $4 p y=\frac{x}{2}$ the D Circhmference at the Bafe; and $\sqrt{a^{4}+y^{2}}=A F$; then $4 p y \sqrt{x^{2}+y^{2}}$ $=$ the curve Surface, and $4 p y^{2}=$ the Area of the Circle EF; then (per Data) $4 \not p v \sqrt{x^{2}+y^{2}}+4 f y^{2}=\mathrm{a} \operatorname{Max}$. or (becaufe $4 p$ is confiant) $y \sqrt{x^{2}+y^{2}}+y^{2}=a$ Max. but, by the Nature of the Spheroid, it will be as $a^{2}: b^{2}:: 2 a x$ $-x^{2}: y^{2} \because a^{2} y^{2}=2 a b^{2} x-b^{2} x^{2}$; and by Divifion $y^{2}=$
$\frac{2 a b^{2} x-b^{2} x^{2}}{a^{2}}=13 \frac{1}{3} x-{ }_{y}^{4} x^{2} ;$ and $y=\sqrt{13 \frac{1}{3} x-x^{2}}$; the fe tho Values of $y^{2}$ and $y$ taiken in the Maximum will be $\left.\sqrt{179} \frac{7}{3} x^{2}+1 \frac{1}{2} \frac{1}{7} x^{3}-\frac{20}{x 1} x^{4}\right)+13{ }^{\frac{1}{2}} x-\frac{4}{3} x^{2}=$ a Maximum. In Fluxions $\frac{355^{\frac{5}{9}} x \dot{x}+4 \frac{4}{3} x^{2} \dot{x}-\frac{8}{8} \frac{0}{1} x 3 \dot{x}}{2 \sqrt{1-7 \frac{7}{3} x^{2}+1^{1} \frac{3}{3}-\frac{8}{4}} \frac{8}{1} x^{4}}+13{ }_{3}^{x} \dot{x}-8 x \dot{x}=0$. Out of Fluxions, \&c. and rightly ordered, will at laft become $i 8=x^{3}-3780 x^{2}-95175 x+1944000=0$. Solved $x=19$,

The Gent. Diary ; or Math. Repofitory. 41 $732375=A G=$ the Cone's Height, and confequently all that is required may be eafily found.
(7.) Queft. 311, anfwered by Mr. Alex. Rowe, near Penzance.


In the fpherical Triangle ABC, are given $A B=10^{\circ}, B C=20^{\circ}$ and $A C=26^{\circ}$. To find (by Spherics) the $\angle A C B=20^{\circ} 44^{\prime} 17^{\prime \prime}$. Then (af er the perpendicular BE is let fall on $A C$ ) in the right angled fpherical $\triangle B C E$ are given $\angle E$ $=90^{\circ} . \angle B C E=20^{\circ} 44^{\prime} 17^{\prime \prime}$, and $B C=20^{\circ}$, to find $\mathrm{BE}=6^{\circ} 57^{\prime} 22^{\prime \prime}$.
Then (by Simpfon's Geom.) $D A=D B=D C$ (the Radii of the Circle $A B C$, being taken as Chords of their refpective Arcs, becaufe thefe are but $($ mall $)=\frac{A B \times B C}{2 \mathrm{D}^{\circ}}=14^{\circ} 22^{\prime} 23^{\prime \prime}$ the Diffance required.
The fame, anfwered by Mr. Edward Parnell, of Nuneaton.
In thi: Problem, there is no more required, if we take the plane Triangle formed by the Chords of the given Dillances of the three Stars A, B, and C, than to find the Radius of its circumfribing Circle ; which is the right Sine of their required Ditance from the fourth Star D (for it is evident, by the nature of the Queftion, the Places of the three Stars $\mathrm{A}, \mathrm{B}$, and C , mutt be on a parallei Circle of the Sphere, whofe Pole is in the Place of the fuarth Star D; and it is well known, the Radius of that Circle is the right Sine of its Dillance from the Pole) which, by plane Trigonometry, will be found $=$ the Sire of $14^{\circ} 23^{\prime}$ the Dittance equired.
(8.) Quet. 312, anfivered by Mr. Robert Snowball, near Hedicy, Noribumberland.
Put $x=$ the Perpendicular BD; and $a=\mathrm{AD}=2$ ) (fee Fig. in laft Year's D(ARY) ; then $\sqrt{a^{a}-x}=A B$; and $5: 3:: \sqrt{a^{2}-x^{2}}: \frac{3 \sqrt{a^{2}-x^{2}}}{5}=\mathrm{BC}$; alfo $\frac{3 \sqrt{a^{2}-x}}{5} \times \frac{x}{2}$
$=$ the Area of the $\triangle B D C$; and $\frac{x \sqrt{a^{2}-x}}{}=$ Area of
$\triangle \mathrm{ABD} ;$ but $\frac{3 x \sqrt{a^{2}-x}}{10} \times \frac{x_{\sqrt{\prime}} a^{2}-x}{2}=$ a Maximum. In Fluxions $6 a^{2} x \dot{x}-12 x^{3} \dot{x}=0$. Reduced, $a^{2}=2 x^{2}$, and $x=\frac{a}{\sqrt{2}}=$ Ch. 14, 14213; whence it is evident $A B=B D$, and from thence the Area of the Triangle $A B D=100$, and the Triangle $B D C=60$ Square Chains, refpectively $=10$, and 6 Acres.
(9.) Quef. 313, aniwered by Mr. Fobn Garton, Jun. of Chilweell.
The Diameter of the Earth (allowing it to be 7970 Miles) I find (by 47. Eu. 1.) the Height of the Mount to be 1,104539 Miles; the double of which added to the Diameter of the Earth gives 7972,209078 Miles, the Diameter of the Earth and Water; which cubed and the Product $\times, 5236$, it will give $265299039498,616692=$ folid Miles in the Earth and Water: from which fubtract the folid Miles contained in the Earth, and the Remainder will be $220+79875$ = the folid Miles of Water, which multiply by the Tuns in one Mile gives $78804175258823337+3946=$ the Tuns of Water then brought upon the Earth.
(10) Quef. $3^{14}$, anfwered by Mr. G. Glofop, at Pool-grecn School.
Let $a=\mathrm{OD}=30, b=\mathrm{AO}=20 ; a=, 7854, x=\mathrm{OE}$; and $y=\mathrm{OH}$ (fee laft Year's Fig.) then, by the Property of the Ellipfis, as $a^{2}: b:: a^{2}-x: b^{2}-\frac{b^{2} x^{2}}{a^{2}}=\left.\overline{\mathrm{GE}}\right|^{2}$; whence $2 \sqrt{b^{2}-\frac{b^{2} x^{2}}{a^{2}}}=G F$, this fquared, and $x$ by a, we have $4 a \times \frac{\overline{b^{2}-b^{2} x^{2}}}{a^{2}}=$ the Area of the Circle GF; which $x$ by $\dot{x}$ makes $4 \mathrm{a} \dot{x} \times \frac{\overline{b^{2}}-\frac{b^{2} x^{2}}{a^{2}}}{}$; the Fluent $4 a b^{2} x-\frac{4 a b^{2} x^{3}}{3 a^{2}}$ $=$ the folid Part ABGF, Again, by the Property of the Ellipfis,

The Gent. Diary; or Math. Repofitory. $43^{\prime}$ Ellipfis, as $b^{2}: a^{2}:: b^{2}-y^{2}: \frac{a^{2} b^{2}-a^{2} y^{2}}{b^{2}}=\left.\overline{H F}\right|^{2}$; whence $2 \sqrt{\frac{a^{4} b^{2}-a^{2} y^{2}}{b^{2}}}=$ FL. And by the Property of the Circle $\overline{b+y} \times \overline{b-y}=b^{2}-y^{2}=\overline{\mathrm{H}_{1}}{ }^{2} ;$ whence ${ }^{2} \sqrt{b^{2}-y^{2}}=\mathrm{K}[$ now $2 \sqrt{b^{2}-y^{2}} \times 2 \sqrt{\frac{a^{2} b^{2}-a^{2} y^{2}}{b^{2}}} \times a=4 a \times \frac{\overline{a b^{2}-a y^{2}}}{b}=$ the Area of the Ellipfis whole Diameters are FL, and IK; which $\times$ by $\dot{y}$ we have $\frac{4 a a b^{2} \dot{y}-4 a a y^{3} \dot{y}}{b}$; the Fluent is $\frac{4 a a b^{2} y-4 a a y^{3}}{b^{3}}=$ the folid Part LFCD. And (per Quef.) $\frac{4 a a b^{2} y-\frac{4}{3} a a y^{3}}{b}=4 a b^{2} x-\frac{4 a b^{2} x^{3}}{3 a^{2}}$; this divided by $4 a$, we have $\frac{a b^{2} y-\frac{1}{3} a y^{3}}{b}=b^{2} x-\frac{b^{2} x^{3}}{3 a^{2}}$; now fubstituting $\sqrt{\frac{b^{2} a^{2}-b^{2} x^{2}}{a^{2}}}$ for $y$ its equal, and clearing the Fraction, we have $3 a^{2} b \sqrt{b^{2} a^{2}-b^{2} x^{2}}-\sqrt{b^{2} a^{2}-b^{2} x^{2}} \times \overline{b a^{2}-b x^{2}}$ $=3 a^{2} b^{2} x-b^{2} x^{3}$. And by Reduction we have $x^{6}-$ $\frac{3 a^{2} x 4}{2}+\frac{9 a^{4} x^{2}}{2}=2 a^{6}$. In Numbers $x^{6}=-1350 x^{4}+$ $3645000 x^{2}=1458000000$ : whence is found $x=21,21$ nearly, and $y=\sqrt{b^{2}-\frac{b^{2} x^{2}}{a^{2}}}=14,14$.
(iI.) Queft. 315, anfiwered by Mr. William e Kingston, of Bath.
Let $a=P G ; b=P F$ (fee Fig. in lat Year's Diary) $s$, and $c=$ Sine and Cofine of $60^{\circ}=\angle \mathrm{ABC} ; x$ and $y$. $=$ Sine and Cofine PBG, $s y-c x$ and $c y+x s=$ Sine and Confine of $\angle \mathrm{PBF}$; then $x: a:: 1: \frac{a}{x}=\mathrm{BP}$; and $s y-c x: b$ $:: 1: \frac{b}{s y-c x}=\mathrm{BP}=\frac{a}{x}$ as above $: \because b x=a s y-a c x \because a c x$ $+b x$

44 Queftions in 1768, anfwered.
$+l x=$ asy $: \frac{x}{y}=\frac{a s}{b+a c}=$ the Tangent of the Angle PRG, from whence BP, PG, and PF are known. But how this can admit of a Minimum I cannot comprehend, as the nearcs $A C$ approaches $P$, the lfffer will the Triangle $A B C$ be; and the leoft when $A C$ coincides with $P$; but then P cannot be faid to be within the Triangle, as it will be then in one of its Sides.

The fame, aniwered by Mr. Henry Taylor, of BißhopWilton.


It is plain by Infpection, that the leaft Triangle will be formed, when the Side AC pafles through the given Point P ; for all Lines farallel thereto, as $a c$, will it is plain increafe the Area more and more, as $P_{p}$ perpendicular to ac, increafes (per Queft.) the Area PGBF is always conftant. Therefore through $\mathrm{P}, \mathrm{d}$ aw PH parallel to AB , and bifect PH in I, and let IC be perpendicular to PH , and take IC $=P G$; through ${ }^{\prime}$ draw CPA, and the Triangle $A B C$ will be the leaft poffible.

Demonstration. It is a known Property of the equilateral Triangle, that the Sum of the two Perpendiculars PF and PG is always=CK the Perpendicular of the whole Triangle; $\mathrm{PF}=\mathrm{IK}$, and $\mathrm{PG}=\mathrm{IC}$; therefore CK $=P F+P G$; and confequently the Triangle $A B C$ is the leaft poffible, by what is proved above.

Calculation. Since $P F+P G=C K$, and (per Eu. 47. 1.) $\overline{\mathrm{CK}}{ }^{2}=\overline{\mathrm{CA}}^{2}-\frac{\overline{\mathrm{CA}}}{}{ }^{2} ;=\frac{3}{4} \times \overline{A C}^{2}, \quad \mathrm{CK}=\frac{\pi}{2}$
$A C \times \sqrt{3}$, therefore $A C=\frac{2}{\sqrt{3}} \times P F+P G . Q . E . D$.

The Gent. Diary; or Math. Repofitory. 45 (i2.) Queft. 316, anfiwered by Mr. Alexander Rowe, the Propofer.
Taking the fquare Root of the firf given Equation, we have $2 a^{3} \dot{x}-3 y^{3} \dot{x}=5 m^{2} \ddot{x} \because 2 a^{3}-3 y^{3}=5 m^{2} \dot{x} \because \dot{x}=$ $\frac{2 a^{3}-i y^{3}}{5 m^{2}}$. Now take the Fluent of the fecond Equation, and we get $\dot{x}=\frac{x 4}{4} \because \frac{x^{4}}{4}=\frac{2 a^{3}-3 y^{3}}{5 m m} \because x^{2}=\frac{8 a^{3}-12 y^{3}}{5 m^{2}}$ $\because x=\sqrt{\frac{\sqrt{2 a^{2}-12 y^{3}}}{5 m^{2}}}$.
(13.) Quef. 3 17, anfwered by Mr. Thomas Walker.

Put $u=150, \mathrm{R}=1,04$, and $\mathrm{P}=$ the prefent Worth of 150 1. per Annum. Then by the Nature of Annuities $\frac{u}{\mathrm{k}-4}=37501$.

Then put $A=3750 ; \mathrm{P}=100, \mathrm{R}=1,04$; and $t=$ the Time in which 1001 . put out at Compound Intereft, will amount to 3750 . Then will $\frac{\mathrm{A}}{\mathrm{P}}=\mathrm{R} t$; whence $\log$. A - Log. $\mathrm{P}=\log . \mathrm{R}+\log , t ; \quad$ Ergo $\frac{\log \cdot \frac{\mathrm{P}}{\mathrm{Log} \cdot}=t=92,409}{\mathrm{R}}=9$ Years required.
** At Knaregoro, in Yorkhire, Youth are boarded, and carefully and expeditioufly taught Writing, Arithmetic, Merchants Accompts, and all the Branches of the Mathematics, by Thomas Walker.
N. B. Knareforo' is fituate in the moft pleafant and healthful Part of the County of $Y_{0}, k$.
0f Particular Regard to Morals and Behaviour.
** The worthy and ingenious Contributors to this Diary are again defired to accept of the Author's fincereft Thanks for their kind Affifance and Encouragement; and is in great Hopes that he may (as it gives him no fmall Concern) be generoully excufed the not publifhing any Solution to the Prize Queftion, not one coming to Hand worthy Publication: However, the next Year (God willing) purpofes to oblige the Gentlemen Contributors with a proper Anfiver to the fame; but, in the mean Time, is in Expectation that fome of
46. Queftions in 1768, anfwered.
them will be carefully confidering the Nature of the Curve, together with its Equation, \&c.

He further moft earnefly defires, that the Contribustors hereto will be pleafed, at all Times hereafter, to fend fuch Things as fhall either be entirely New, or (if otherwife) much improved, fo as to be ufeful and more entertaining; and alfo that the Schemes or Figures, may be drawn as perfect as poffible, and of a proper Size for the Diary ; likewife, that all Equations may be brought out in Numbers, \&c.

And whereas a great many Letters of ten come too late to Hand to be taken Notice of (as the ingenious Mr. Metcalfe's, with his Calculations of the Eclipfes, and many others did this Year), the Dates whereof prove it to be no Fault in the Poftage; the Editor therefore defires that for the Future the Letters may all come to Hand within the Time limited for that Purpofe, in Order to their having a due Perufal, and being carefully compared one with another, \&c. The Author ufing his beft Endeavour, and being determined (fo far as poffible) that nothing fhall be wanting in him (fo far as in his Power) to promote ufeful Knowledge, and give due Encouragement to whoever fhall appear deferving of it, \&c.
N. B. No Questions, or other Things, fhall ever for the future be publined in this Diary, except their Solutions at large be fent along with them.

New Mathematical Questions to be anfiwered in the next Year's Diary. (1.) Queft. 319 , by Mafter Hutton Wood.

Let there be two Perpendiculars $A D, B C ; A D=18, B C=24$. Feet; and the Bafe $D C=36$ : The Hypothenure $\mathrm{AF}=\mathrm{FB}$, is to be placed in the Bafe (fuppofe at F), fo as to reach
 the Top of both Perpendiculars; Quere the Point F in the Bafe; and the Length of the Hypothenule?
(2.) Queft. 320, by Mr. Thomas Walker of Knareßro'.

Given $y^{4}-z^{4}=y+\approx$; require $y$ and $\approx$ ?
(3.) Quent.

The Gent. Diary, or Math. Repofitory. 47
63.) Queft. 321, by Mr. T. Atkinfon, of Ingham, Lincolnfiire.

Once formerly 1 did with Freedom flow,
But now, alas! I bid that time adieu;
Faft bound with Chains, I now confin'd muft lie,
Lamenting much in fore Captivity!
Ingenious Algebraifts, hafte to my Relief,
Shew in a Word * the Caufe of all my Grief!
*Viz. $w+x+y+z=50 . w y-x z=150 \cdot \frac{x y}{w x}=5,2727$. $w+x=y+z$. Where $w, x, y$, and $z$, fhew the Places in the: Alphabet of the Letters compofing the required Word.
(4.) Queft. 322, by Mr. Robert Langly of Hitchin.

A Lady's Age and Fortune are defin'd,
In the Equations $\dagger$ hereunto fubjoin'd;
Diarian Artifts, make the fame appear
In your Diary the enfuing Year.
$t$ Viz. $\left\{\begin{array}{l}y^{2} x-x^{2}=42343959 \\ y^{2}-x^{2} y=\text { I } 390180\end{array}\right\} \begin{aligned} & \text { Where } x \text { reprefents the } \\ & \text { Lady's Age, and } y \text { her: } \\ & \text { Fortune in Pounds. }\end{aligned}$
(5.) Qieft. 323, by Mr. Thomas Barker, of Wiffett, Sufflk.

A Gentleman has a Garden in the Form of a Quadrant, whofe Radius is 40 Poles; in which he has ordered his Gardener to make a Canal at one of its Vertices, in fuch. Sort, that the Rectangle of the Secant and Cofine fhall exceed the Produet of the Cotangent and Verfed Sine by a Maximum; required the Garden's Area ?
(6.) Queft. 324, by the fame Gentleman.

Let $z^{8} \pm a x^{4}=y$, and $a z^{4}-z^{8}=y$; Quere the Value of $x$, in Terms of $a$, and $y$; by the Inveltigation of Fluxions, $\& \sim$,
(7.) Queft. 325 , by Mr. Tbomas Robinfor, of Biddick.

In a right angled Triangle, whofe Bafe and Perpendicular are 48 and 35 ; required the Dimenfions of the greateft infcribed Parabola; whofe Abfciffa is parallel to the Perpendicular of the Triangle?
(5) Queft. 326, by Mr. Kienry Tilnsy, of Harlefor.

To determine the Dimenfions of the Greateft Parabola that can te infribed in the Sector of a Circle whofe Radius. is 20 ; and the Angle at the Genter Go Degress?
(9.) Queat.

4 S New Quest. to be anfwered next Year.
( 9. ) Quefl. 327, by Mr. Alexander Rowe, of Penzance.
In what North Latitude is the finorten Day equal to $\frac{2}{5}$ of ${ }_{3}^{4}$ of the longelt at London?
(10.) Qielt. 328, by Mr. Robert Langley of Hitchin.

I have a cylindrical Ciftern in my Garden, ftanding truely Horizontal (whofe Ufe is to water the fame). On Novimber the, 21 ft in the Morning, being in Latitude $52^{\circ}$ North; I obferved the Shadow of the Top of the Ciftern, falling on its oppofite Side, whofe loweft Diftance from the Top was 6 Inches: inftantly I ordered the Ciftern to be filled with Water, and then found the Shadow's loweft Diffance from the Top to be 20 Inches, which is the Depth of the Ciftern : Required the Diameser, and Content of the fame in Ale Gallons; and alfo the Hour of the Day, when this cur:ous aftronomical Obfervation was made?
(11.) Queft. 329, by Mr. Alexander Rorve.

Given the Fluxionary Equation $\hat{3} \cdot 375 a^{3} \dot{x}^{3} \dot{y}^{3}-6.75 \boldsymbol{a}^{2}$ $y^{3} \dot{x}^{3}+4 \cdot 5 a y^{2} \dot{x}^{3} \dot{y}^{3}-y^{3} \dot{x}^{3} \dot{y}^{3}={ }^{2} 7 m^{6} \dot{x}^{3}$. Required the relation of $x$ and $y$, when $x^{2} \dot{x}$ is to $\dot{y}$ as 3 to 2 .
(12.) Quen. 330, Prize Question, by Mr. Rob. Langly.

Whocver flall fend the beft Solution to $i t$, and the beft Poetical general Solution to all the Anigmas, before Candlemas Day 1759 , fhall be entitled to the ufual Yearly Prize of Diaries.

Ingenious Artifts, whofe unbounded Skill,
The deepeft Problems can refolve at Will ;
In ev'ry ufeful Science, you may find,
Curious Theorems timprove the Mind.
Know then, kind Artifts, in a Gauger's Round, A Cafk upon the Tilt was lately found;
A Spindle * Parabolic feemed to be * Midd. Frufum Whofe Axis makes an Angle fixty three $t$, Its Head Diameter is fixty-feven, Inches Bung eighty-two; Length a hundred and 'lev'n:
What Liquor in the Cafe does now remain, Next Year, kind Philomaths, declare the fame.
$\dagger$ Degrees with the Horizon; and the Beer juft touches the Bulge.

$$
\begin{array}{lllll}
\mathrm{F} & \mathrm{I} & \mathrm{~N} & \mathrm{I} & \mathrm{~S} .
\end{array}
$$

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THE new improv'd Englifh Slates, now brought to great Perfection; they are light, and not liable to be broken; very proper for Schools, Baxs of Taverns, \&cc. - The new invented Music.円 , oks, particularly ufeful for learning and compofirg Mufick. - Alfo new invented Memorandum Books, very neat and bandy. -Likewife Pocket Fooks, greatly improv'd, more commodious and urable than any others now in Ufe, with Slate Paper Memorandum-Books of all Sizes Alfo Ink clarified from the Cakes, being free from Sediment, and thin as Water, in two Days after it is us'd will be the fineft and deepelt Black, and will continue fo while she Paper or Parchment will endure.
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THE true Original Daffy's Elixir, from the old Warehoufe in Salisbury Court, Fleet-Streer, where it was firft made and fold, rs. 3 d pe Bottle.-Peter's Pills 1s. a Box, and his Cordial Tinc ture at is. 3 d. per Bottle. - Dr. Lobb's Tinaure foFämily Ufe, 2s: 6d. each Bottle.-Dr. James's Feven Powder, 2s. 6d. each Packet. - Hoopers Female Pills 1s. per Box. - Anderfon's Scotch Pills is a Bax. Hadfield's Tineture for frefh Wounds 1s. per Bottlo. - Jackfon's Tincture for Burns, Scalds, \&c. 1s. each Bortie. - Greenhough's Tineture for preferving the Teeth and curing the Tooth Ach rs. each Bottle. Dr. Radeliff's Purging Elixir 1s-The genuine Britifh OiI which cures all Scorbatic and Rheumatic Diforders Price is.-Ditto refin'd Price is, 6d. - Alfo the Baume de Vie, a moft efficacious Medicine againft many Diforders, firf difcover'd by the Apochecary to the King of France, Price 3 s. ${ }^{3}$ eact Bottle. - Blagrave's goldeni and plain Spirits of Scurvy Grafs 1s. each. - The Stomachic Lozenges ys. 6d. a Box. - Britilh Powder for Teeth is.-Godfrey's general Cordial, :Price 6d.Chymical Dropss for the Cure of Coughs, Colds, Aftbohas, \&c:uStoughton's Elizir Price Is.

