## THE

Geintleman's Diary,
ORTHE
Mathematien ${ }^{\text {De }}$ Repository; An ALMANACK For the Year of our LORD 1779:

BEING

The Third after Bissextile, or Leap-YEar. Containing many ufeful and entertaining Particulars, peculiarly adapted to the ingenious Gentlemen engaged in the delightful Study and Practice of the M A T H E M A T I CK.

The I hirty-ninth Almanack publifhed of this Kind, and the Twenty-fiventh of the New-Styie in England.

With wife Intent The Hand of Nature on peculiar Minds Imprints a different Byafs, and to each Decrees its Province in the common Toil. To fome fhe taught the Fabric of the Sphere, The changeful Moon, the Circuit of the Stars, The golden Zones of Heaven : to fome the gave To weigh the Moment of eternal Things, Of Time, and Space, and Fate's unbroken Chain, And Will's quick Impulfe. Arenside.

## L O N D O N,

Printed for the Company of STATIONERS And Sold by George Hawkins, at their Hall in Ludgate-Street. 1779.
[ Price Eight Pence ftitched.]

THE Author again returns moft fincere Thanks to all his kind Contributors; and intreats the Continuance of their Favours; and, as he is now removed to his old Town of fair Nottingbam, humbly requefts, that fuch Contributors who live convenient for that Post-Office, will order Letters for bim to be left tibere Pof-paid: And the others with Mr. Hawkins, at Stationers-Hall, London, Poft-paid alfo, before Easter Day, 1779.

FEBRUARY hath xxviii Days.

| M |
| :---: |
|  |  |


| Full <br> Lalt <br> Firf | Moon <br> Quarter <br> Moon | the 1 the 8 t the 16 t in $23_{1}$ | $\left.\begin{array}{l} \mathrm{ft} \\ \text { th } \\ \text { th } \end{array}\right\} \text { Day }$ | $\begin{aligned} & \text { at }\left\{\begin{array}{l} 3 \mathrm{in} \\ \mathrm{Hal} \\ \mathrm{Hal} \\ 9 \mathrm{at} \end{array}\right. \\ & 5 \mathrm{~m} \cdot \mathrm{pait} \end{aligned}$ |  | ouning. in the M ${ }_{11}$ Foreno <br> noon. |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\begin{array}{l\|l} W \\ 0 & 0 \\ \hline \end{array}$ | Sund <br> Leng | nc. | and | Term | ys; | $5$ | $\begin{aligned} & \mathrm{N} \\ & \mathrm{So} \\ & \hline \end{aligned}$ | Moon Sourh. |
|  | M 21 | Days in | reafed | hour | 28 mi | Faft. | D R | les | 6 |
|  | Tul2 | Purif. B | V. | Mary. |  |  | 6A 26 | 26 | 0 |
|  | W 23 | Blafius | B. Onth | heMor. | of P | 3 Ret. |  |  | $4^{8}$ |
|  | Th 24 | Axtridg | ge. Bat | th, Som |  |  | - |  | 28 |
|  | F 25 | Agatha | , Old S | S. Paul. |  |  |  |  | $4 \begin{array}{ll}4 & 13\end{array}$ |
|  | S 26 | Nampt | wich, C | Chefh. |  |  |  |  | 57 |
|  | C 27 | Sexage | fima Su | unday. |  |  | Mo |  | 2 |
|  | M 28 | Days in | cr. 2 h | hours. |  |  |  | 50 | 6 |
| 9 | Tu 29 | $\ln 8 \mathrm{D}$ | ays of P | Purif. | 4 Retur |  |  |  | $7 \quad 14$ |
| 10 | W 30 | Lland3 | Jel, Mon | nm. |  |  |  |  | 0 |
| 11 | Th 31 | Day 9 | h. 46 m | m. long |  |  |  | 13 | $8 \quad 52$ |
|  | F Fe | Hilary | Terme | ends. |  |  |  |  | $94^{2}$ |
| 13 | 5 | Old Ca | dlema |  |  |  |  | - 10 | $10 \quad 32$ |
|  | C 3 | Quinq. | Sunday | y. Val | ntine |  | 63 | 3911 | 1120 |
|  | M | Blaije, | Coinw. | . Boxgr | ve, Sh | pfh. |  | 10 A | Aftern. |
|  | Tu | Shrove | Tuefda |  |  |  | ${ }^{\text {d }}$ Set | ts | - 8 |
|  | W | Afh-W | ednefda | ay, ift |  | ent. | 6 A | 30 | - 54 |
|  | Th | Nun-E | ton, W | arw. |  |  |  |  | 39 |
|  | F | Beverly | , York | fh. |  |  |  | 32 | 223 |
| 20 | S | Days i | ncr. 2 h | h. 34 |  |  |  | 47 | $3 \quad 9$ |
|  | C 10 | 1 Sund | day in L |  |  |  |  |  | $3 \quad 56$ |
|  | M 11 | Nortor, | Oxf. |  |  |  | Morn |  | $4 \quad 45$ |
| 23 | $\Gamma_{0}{ }_{12}$ | Godalm | ing, Sur | urrey. |  | , |  | 27 | $\begin{array}{lll}5 & 38\end{array}$ |
|  | W/ 13 | St. M | Tthia | A. Pr. | Adol. |  |  | 476 | 6 |
|  | Th $\cdot 4$ | Feverß | $a m, \mathrm{Ke}$ | ent. [ | Embe | Week |  |  | $7 \quad 36$ |
| 2 t | F 15 | Oundle, | North | amp. |  |  |  |  | $8 \quad 38$ |
| 27 | S It | Day 10 | h. $5^{\circ}$ | min. |  |  |  |  | $9 \quad 41$ |
| 28 | C $\mathrm{I}^{-}$ | 2 Sund | day in |  |  |  |  |  | $10 \quad 41$ |
| $1 \mathrm{M}$ | $\begin{aligned} & \text { Sun } \\ & \text { Rifes } \end{aligned}$ | $\begin{aligned} & \text { sun } \\ & S: \cdot \mathrm{s} \end{aligned}$ | $\begin{gathered} \text { Satuin } \\ \text { Rifes } \end{gathered}$ | $\left\|\begin{array}{c} \text { Jupiter } \\ \text { Rifes } \end{array}\right\|$ |  |  | $\begin{aligned} & \text { Day } \\ & \text { Break } \end{aligned}$ |  | $\begin{aligned} & \text { Clock } \\ & \text { too faft } \end{aligned}$ |
|  |  |  | $2 \mathrm{M}_{20}$ | $\overline{8 \text { A } 39}$ |  |  |  |  |  |
|  | $\begin{array}{ll}7 & 16\end{array}$ |  |  | 8 48 | - 44 |  |  |  | $14 \quad 32$ |
|  |  | $4{ }^{4} 5$ | 144 | 57 | - 37 |  |  |  | $14 \quad 40$ |
|  | 659 | 5 | 26 | 35 | - 30 |  |  | 614 | it 29 |
| 41 | 49 | 5 | 17 | $7{ }^{7} 12$ | - 20 | - | 57 | 7 | 14 |
|  | 39 | $5 \quad 22$ | 1047 | 648 | - 10 | ¢0 | 448 |  | $13 \quad 12$ |



## APRIL hath xxx Days.






## JULY hath xxxi Days,

$|$| $M$ | $\odot$ |
| :--- | :--- |
| $D$ | Decl. |
| North. |  |

Laft Quarter the 6th
Lat Warter Mon the 6 th
Niew $\quad\{6 \mathrm{~min}$. palt 9 at Night.
 Full No.n the 28 th

O in $\Omega{ }_{23}$ Day, 53 min. paft 2 Morning.

| 1 | $23^{\circ}$ | $8!$ |
| :--- | :--- | ---: |
| 6 | $2!$ | 43 |
| 11 | 22 | 8 |
| 16 | 21 | 23 |
| 21 | 20 | 30 |
| 26 | 19 | 27 |








A TABLE of all the Kings and Queens of England fince the Conqueft.
The Year of the Birth of each King The Years and Queen ; alfo the Year, Month, and Day, whereon they began to reign: beginning the Year the firft Day of January, 1779.

Leng:h
of each
Reign. fince each Reign ended


## A Compendious Table of Interegt,

## SHEWING

The Intereft of any Sum of Money, from a Milion to a Pound, for any Number of Days, at any Rate of Intereft.

| 1000000-2739 | 14 | -1000-2 14 |
| :---: | :---: | :---: |
| 900000-246 | 1503,29 | 900-2 9 9 3 3,12 |
| 800000-219 | $1571 ., 59$ | 800-2 3100,11 |
| 700000-1917 | 16 1 3 , 89 | 700-1 18 4 1,10 |
| 600000-164 | 1582,19 | 600-1 12102,80 |
| 500000-136 | $17 \quad 30.49$ | 500-1 7 7 433,70 |
| 400000-109 | $17 \quad 92,79$ | 400-1 11110,50 |
| $300000-82$ | 1841.09 | $300-016 \quad 512,40$ |
| 200000-54 | 18103,40 | 200-0 10 11 2,30 |
| 100000-27 | 1951,70 | $100-05 \quad 53,10$ |
| 90000-24 | 1160,32 | 90-0 41110,71 |
| $80000-21$ | $36 \bigcirc, 96$ | $80-044^{2,41}$ |
| 70000-19 | $15 \quad 71,59$ | 70-0 3100,11 |
| 60000- 16 | 780,22 | 60-0 3 3 1,81 |
| $50000-13$ | 1982,85 | $50-0283,51$ |
| $40000-10$ | 1191,48 | $40-0221,21$ |
| 30000- | 100,11 | 30-0 1 70,90 |
| 20000- | 15102,74 | 10,60 |
| 10000- | 7111 ,37 | $10-0 \quad 0 \quad 6 \quad 2,30$ |
| 9000- | 1313,23 | - $\quad 53,67$ |
| $8000-$ | 1841 ,10 | 51,04 |
| $7000-$ | $\begin{array}{llll}3 & 6 & 2 & , 96\end{array}$ | - 42,41 |
| 6000- | 890,82 | 6-○ $0 \cdot 313,78$ |
| $5 \mathrm{CO}-$ | 13112,58 | 5-0 0 - 3 1,15 |
| 4000- | 1920,55 | 4-0 0022,52 |
| 3000- | $44^{2} 2,41$ | 3-0 013 , 89 |
| 2000- | 970,27 | 2-0 $00.111,26$ |
| 1000- | $14 \quad 92,14$ | $1-0 \quad 0 \quad 0 \quad 2,63$ |

Multiply the Sum by the Numher of Days; and that Product by the
Rate per Cent. Then cut off the two lant Figures to the Right Hand, and the reft you muft find in the Table.
Example, What is the Interef of rool. for $3^{6} 5$ Days at 5 per Cent? $\mathrm{N}^{2}$ of Days $3^{6} 5$


## The Gent. Diary ; or, Math. Repofitory. 17

## Of the Ecripses of the Luminaries happening in 1779.

The Firf; will be an invifible Eclipfe of the Sun, on Sunday the I6th of May, at x in the Morning.

The Sccond, will be a cotal Eclipfe of the Moon ; and part-vifible: on Trinity Sunday, the 3oth of May, in the Morning.


The Third is a vifible Eclipfe of the SuN , on Monday the 14th of - Fune, in the Morning: Beginning of the Eclipfe - $\quad 7 \quad 18$

Middle - - - 759
End - Digits $3^{\circ} 15^{\prime}-84$
The Fourtb, will be a great and vifible Eclipfe of the Moon; on Tue'day the 23 d of Nowember, at Night:
H. M.

Beginning of the Eclipfe - 6
Beginning of total Darknefs - 77
\(\begin{array}{llll}Middle <br>

End of total Darknefs\end{array} \quad-\quad\)| 7 |
| :--- |

End of the Eclipfe - - 947
Digits eclipfed $20^{\circ} 42^{\prime}$
The Fiftb and laf, will be an invifible Eclipfe of the Sus , on Tuef? day the $7^{\text {th }}$ of December, at half paft to at Night.

Mifs Polly Stow's, are as under;
See the Eclipfes, how they run;
Two of the Moon; one of the Sun: By Polly Stozu your female Friend,
As She below the fame has penn'd.
The Moon, on May 30, Morn. The SUn, fure 14, Morning.

The ${ }^{\text {' Moons }}$, on November 23, at Night.


## 18 Sun's Eclipfe; Enigmas anfwered. $\mathrm{N}^{\circ} 39$.

Mr. Richard Todd, of Alnwick, Nortbumberland; fent the following computation of the Sun's Eclipfe, on the $14^{\text {th }}$ of fune.


Mr. John Norman, of Braybrook, Northamptonfhire, computed all the Eclipsesfrom new manuicript Tables of his orwn compofing; with the general appearances, for LONDON, Cork, and Edinburgb.
And Mr. Samuel Oliver, of Popplewick, Nottinghamhire, fent computations of the Echipses, with a Type of that of the Moon on the $3^{\text {oth }}$ of May; which, for want of room cannot be inferted.

Answers to the Ænigmas, \&cc. in the laft Year's Diary.

1. Scandal.
2. Darkness.
3. Magic lanthorn.
4. The Finger Nails.
5. A Cork.
6. Time.
7. A Sexton.
8. Strength.

Prize. Dice.
1 Rebus; Peat. 2 Gough, Colledge, andSimpine. 3 Excise。 The Prize Æinigma anfwered by Mr. William Richardson. Diarian Wrid, your riddle, I think May be the $B_{o x}$ and Dice;
Therefore, my friend, let's have a drink, Then try to get a prize.
The fame anfwered by Mifs Polly Stow, of Stow. Make room - ftand by.-Let me caft the dicz!
Who knows but kind fortune may give me the prize?
Behold-how furprifing !-Pray look down and fee,
The dige, they run fixes- the PRIzE falls to me;

## The Gent. Diary; or, Math. Repofitory. Ig

The fame anfwered by Mr. Robert Marshar, of Hoole, Lancafhire.
From the bints giv'n (which are quite nice)
Your meaning Wyid's, a pair of dice.
Mis. Amelia Stanhope, anfwersthe fame, thus;
Let cards nor dice no more (ye fair)
Your hands employ, nor hearts enfnare,
For more fublime delights prepare.
Finow! facred time the gift of gracious heav'n,
'fo wafte at folly's fhrine-was never given.
Mr. Francis Turner, anfwers it thus;
The prize Ænigma l've guefs'd in a trice,
And nought could I make on't but ivory dice.
Mr. Thomas Barker, anfwers the fame as under;
While fome parade in ufelef's wealth, thro' all the paths of vice,
Wafting their thoufands, time and health, at billiards, cards, or DICE:
To pleafe the contemplative mind, and not offend its God.
May I Eliza's cottage find, a peaceful, blefs'd abode !
All the 甭igmas and Rebusses anfwered by Mr. Wm. Wyid, addreffed to Lufedo, in a diffuafive from DICE.
Will you Lufedo fport your time away
With dic E, at bazard, or back-gammon play?
Will you ; defcended from a lineal race
Of peers illuftrious! Thus yourfelf debafe ?
Suppofe you zvin-what caufe have you to boaft?
When reputation in exchange is loft
Think what a scandal tis: your footlefs fame
Will foon be fully'd with a GAMBIER's name.
By facred friendhip's tye, I now intreat,
You will the cork-tree fhun, where gamefters meet!
You-who may have a tip-faff at command,
Duteous, to walk before you with a wand *;
That undifturb'd by the tumultuous throng.
With fafety you, in fate, may pafs along;
All which is forfeit, if you perfevere
Will refolutely to the box adhere :
If you defign to leave it. Do not throw,
Do not yourfelf another caft allow.
'Tis repetition which a bias lays,
Upon the will, and the affection fways;
Heightens the tafk the conqueft to acquire,
Cuftom incites-gives strength to the defire, At leifure hours, if 1 may you advife,
Repair to Peat's, the office of excife;
1 and 3 Rebs
Enquire there, for Wilixin, Gough, and Coxemdge, 2 Reb. Men of erudition, and fam'd for knowledge:
What darknefs in $L_{u f f d o ~ y e t ~ d o e s ~ d w e l l, ~}^{\text {, }}$
They will by force of argument difpel;

$$
\mathrm{B}_{2}
$$

Will

* Alluding to a sexton.


## 20 Ænigmas in $177^{8}$ anfwered.

Will make that LANTHORN, reafon, brighter thine, 3
Enlarge conceptions; moral and divine:
With fuch affuciate-genious to improve, The leaft degree of ign'rance to remove; Yet, fome remains we may expect to find Of clouded notions in a youthful mind.

If thefe reflections are of no avail,
Then be advis'd to fit and pare your NAII.
All the Einigmas and Rebusses, anfwered by Mr. Wilisam Massom.
Since Coliedee, Gough, and Simkin, are all deem'd 2 Reb.
Three tipling poets, why fhould I be fcreen'd?
I love the bottle, and good company,
As well as any of the jovial three!
One night when DARK, I to the tavern bound,
When there I got, friend Simpkin foon I found;
Tho' time was thort, - his company I join'd,
So we thook hands, -our finger-Nails combin'd:
No fop of pride, no SCANDALizing tongue,
No DICE, nor cards to either did beiong: Prize
No brawling company at all was there,
So, next my friend, I took the corner chair $;$
Both freely drank (as we are apt to do)
Had call'd the reck'ning, ready for to go.
In came the sexton, and Excise man too! 7 压. 3 R. $b_{0}$
Diarians both, of wit and judgment nice
Some friendly welcomes pafs'd, when in a trice,
Another bottle we uncork'd in hafte
Drank bealth to PEAT, and ev'ry fon of tafte!
The liquor fine, foon made us all fo wanton,
We look like figures in a magic-ranthorn ! 3
We fung, laugh'd, jok'd, and drank, until at length,
We fairly found, -we'd try'd each other's strenGTH.
All the 届nigmas anfwered by Mr. Wiliiam WOODhOUSE.
In this night fcene-this DARK retreat
With me, O Lord refide
Myfingers Lord, and eke my feet 4
As with a Lanthorn guide.
Be scandal ne'er by me enjoy'd,
While time I cancall mine.

Then when the sexton tolls my bell
Light as a cork I'll fiee
Above where DICE, nor gamblers dwell Prize
To faints, to beavin, to THEE!

## The Gent. Diary; or, Math. Repofitory. 21

## Mr. Thomas Adcock of $A \beta b-$ de-la-Zouch, anfwers them as follows:

THEHAPPYMAN.
Happy ! the man, who free from noify fports,
And all the pomp and pageantry of courts ; Free from the venal world, can live fecure-
Be moral honeft; - virtuous-tho' poor:
Who walking ftill by equity's juft rules.
Detefting CORKifhknaves, and SCANDALizing fools! 5. I
Regarding neither fortune, pow'r, nor ftate,
Nor ever wifhing to befvainly great;
Door strong with nails he fees old time defy,
8.4. 6

But what is that to him who's learn'd to die?
A foe to DICE, no paffions guilty friend,
Prize
Obeying nature, faithful to the end.
Severe in manners, and in truth fevere, Juft to himfelf, and to his friend fincere;
His temper even, and his fteady mind
Refin'd by friendihip, and by books refin'd;
In fome neat cottage holds the happy fwain,
Unknown to DARKNESS, or the LANTHORN train;
2, 3
He ftudying nature grows ferenely wife,
Like to a sexton lives, or like him dies:
He alks no glory gain'd by hoftile arms,
Nor fighs fur grandeur with her painted charms;
With calm indiff'rence views the fhifring fcene,
Thro' all magnanimous, refign'd, ferene:
On hopes fuftain'd he treads life's devious road,
And knows no fear, except the fear of God !
Would heav'n indulgent, grant my fond defire,
Thus would I live -and thus fhould life expire !
Mr. W. Gough fent the following anfwer to the Finigmas and Rebufes, One evening young Molly I met in the vale, Refolved I was for to tell my fond tale;
Iftep'd to the fair one, and offer'd a kils, Fye Hodge! -She reply'd; what a SCANDAL is this?

I
Pray hafte to your flock, mind your plough and your team,
Your vows and your fighs are no more than a dream;
And DARKNESS comes on-fo I'll bid you adieu,
What fair can be fafe with fuch rakes Hodge as you?
No Magical Lanthorn could e'er more furprife;
I view'd her foft charms, and her black rolling eyes:
My heart was inflam'd with foft raptures of love!
But deaf to my fighs fill the fair one did prove.
Refolv'd then I was for to try her next day,
She happen'd to pafs me when turning my hay;
I laid down my prong to embrace the fweet fair,
And grefs'd her foft Fincers 'twixt love and defpairo

## 22 Enigmas in 1778 anfwered. $N^{\circ} 39$.

Why Hodge cry'd the fair one, you lately did own,
You'd $w_{00}$ 'd all the girls that refide in the town;
Then, how can I truft you ?-So take up your fork,
For your words are as light as a feather or cork.
Pray be not fo harfh, cry'd the fubtle young fwain
I've a farm of my own, and a flock on the plain;
No time then delay, but away let us hie6

To the church on the brow, where the knot we will tie.
She fmil'd in my face, and the SExTon call'd too,
Then blufb'd ber compliance ; and vow'd to be true;
Saying, Hodge if you're conftant (to end all the ftrife)
I'll give you mv hand, and be happy for life!
Mystrencthi renew'd, and without more delay.
8
To the altar of Hymen we hatten'd away;
Where both were united in conjugal blifs.
To love and live happy! What's equal to this ?
The nuptials being crowned, to dinner we went,
At dice, wbift, and cribbage, the evening we fpent: Prize
No mortals fo happy, nor to full of glee,
As th'exciseman and Peat, Simpkin, Colledge and Me. Reb.
The Ænigmas anfwered by Mr. B. Ceeypole; on Scurrility.
To a puppet-ßorv one TIME I did go,
(A mile and half did I wander)
Some young priggs being there to whom I fat near
6
Their click-clacks were all upon SLANDER.
One faid that Mifs Clark was kifs'd in the dark;
That the was both wicked and wanton;
Becaufe the did go for to fee the odd thow
Performed by amagic-lanthorn.
Thus, they run their randans with uplifted HANDS, 4
'Their language, as light as a cork, 5
With one eye they would wink, which made me to think
They'd ne'er feen a SEXTON at work.
'Till their clacks at the length, having fpent all their STRENGTH
And all modefty quite had bereft 'em,
When up they did rife, for play with two dies, Prize
Then I came away, _and there left 'em.
All the Enigmas anfwered by Mr. William Richardson, on Morning.
See! How Aurora, with her gilded fan, Drives darkness off, -and ufhers in the dawn:
Firft of the feather'd tribe, the lark begins,
And poiz'd on high, his early matins fings:
Perch'd on the fpray, the black-bird tunes his throat,
Makes woods reverb'rate with his fwelling note.

## The Gent. Diary; or, Math. Repofitory. 23

## Hear, how the 乃bepberd his bucolics play, To welcome in the roly fingerd day.

Who fpends both tIME, and strencth o'er rattling DICE. 6. 8. Prize

He, sexton difregards -or tolling bell,

$$
\text { Will draw another cor } \mathrm{C} \text {, or filthy tale will tell. } 5
$$

Perhaps, a magic-lanthorn, he will fay, 3
By far excels the fweets of new-born day !
See yonder, how the milk maids trip along,
Cheering each other with a rural fong:
For, in the morn, all nature's blithe and gay,
But then, e'er noon - The droops, and fades away.
Anfwers to all the 不nigmas, by Mr. Wililam Swift of Stow, near Lincoln.
Whát a scantalous virger * I paffed laft night! 1.7.2
With his rod, and his Lanthorn, he much did me fright: 3
I was all for figbting-but my strenger - gentlemen
At that time did fail me-what could I do then ?
Yet, alucky chance after! IFINGER'D the dice; 4. Prize
And as light as a cork was my heart in a trice
When, at one fingle caff, I gained your prize.
A general Anfwer to all the Ænigmas, and Rebusses; by Mr.
Thomas Trusswele of Nun-Eaton, Warwick/hire.
Once more (my dear gents) your foft, rapturous itrains
Invite me to tread the diarian plains;
Where fcience extends her fair branches around,
And bends with her clufters of fruit to the ground !
How happy was I, when permitted to rove,
Where learning now wears the foft emblems of love;
Where truth and fair fcience, united agree,
In meanings abftrufe, tho' good natur'd and free.
When firft, in my youth, I attempted the ftage
Kind peat me excus'd, and confider'd myage;
x Reb.
Thanks, thanks aged mafter, my thanks are your due;
For all the kind favours seceived from you !
Then fortune! O fortune, unto him be kind!
God grast him long life, and accomplifh his mind!
How oft I've perus'd the \&nigmatic lore,
Each Rebus and Query, I've conn'd them all o'er :
Such intricate turnings and zvindings appear,
I fcarkeiy can folve tn' Enigmas this year.
But ftop! my dull mufe - and no longer defpair
For riddles are made a dark garment to wear
But quickly unveil'd -by attention will fhow.
An afpect that feems quite delightful and new ;
24 Ænigmas in 1778 anfwered.

Likemagical lanthorns convey to the mind
Strange comical fincirs-tho' always refin'd
By witty Diarian's - e'en fome of the beft,
As Coleedge, and Simpiin, Gough, Gumiey, and Weff. 2 Reb.
When scandai takes place, how great is the fway, I
(But time will foon bring fuch things to decay.) 6
How bufy their FINGERS, how fcornful their eye 4
Their hearts fo malicous, 'tis hard to defery.
When the sexton he tolls, and the death-bell does call 7
Their stength will have left 'em, and down they muft fall! 8
Then caft the fair DICE, let the number be thrown, Prize
That each may partake a fair chance of his own;
May mine be a chance that will lead me to heav'n
And grant that my fins be hereafter forgiv'n.
P. S. The fifth ENIG. is a Cork, and third Rebus. Excije. $^{\text {R }}$

Mr. Benjamin West anfwers the Enigmas, as follows.
Poily Stow, a Lyric Essay: addrefs'd to Mr. W. Swift. Audentes fortuna juvat. Virg.
Let goffips o'er their dear bohea,
In lies and scandal wafte the day And doat on empty fhow; Be mine the tafk in lyric ftrains, To fing the Clio of the plains, The tuneful Poley Stow.
When night appears, in DARKNESS dreft
"Sleeping" (he fays) the "calls out West !"
But let the charmer know,
He, bleft already with a mate,
Muft wifh fome worthier youth the fate
To wed with—Polly Stow.
Say little patent urcbin, fay
What filent MAGIC waits thy fway
That swaft fhould feem too sxow?
Oh! give the bard a voice to fing, And pow'r to wake the rapt'rous fring

To love-and Polly Stow.
When blufhing o'er the dewy lawn
The dappled rofy finger'd dawn
Díplays her brighteft glow,
More beauteous than Aurora's dies
More lovely far to Billy's eyes
Appears his Poley Stuw.
Courage! fweet bard of Lincolnhire! With heart as light as CORX appear

## The Gent. Diary ; or, Math. Repofitory. 25

Your parts, your merit, rife confeft Then fue-fucceed-belov'd-be bleft By_pretty Polily Stow.
See! beck'ning to the hallow'd dome Propitious Hymen bids you come (His torch flames bright as tow)
Hafte then, fond youth!-no time delay
Prefs on -be happy while you may With-charming Polxy Stow.
With accents difmal as the knell,
Deep-founding from the sexton's bell
Tho' fools paint wedlock's woe,
Empty as air their words you'll prove, And own a little heav'n in love,

When yok'd with Poli.y Stow.
Such fenfe, with fpotlefs virtue join'd, An inexhaufted fource you'll find,

Whence pureft joys will flow;
When age your manly strength thall break
And fteal the role-bluh from the cheek Of-lovely Poliy Stow.
Sing, Heliconian vireins, fing!
And wreaths of choiceft flow'rets bring
That on Parnafjus blow ;
With Io Pcans fill the fkies !
Fates die is caft and Billy's prize
Is - peerlefs Poliy Stow.
General Solutions (in Verfe) were alfo given, by Mefirs. Jobn Jockjon, Jofepb Fames, Benjamin Kemp, Robert Marfh, Samuel Oliver, William Percival, George Simpkin, Antbony Temple, Henry Walcb, and others.

Anfwers to the Regusses in the laf Year's Diary. By Mr. Benjamin Kemp.
Peat, and Excise, Gough, Simpkin and Colledge, Are your Rebufles three; or you've out-done my knowledge. Aniwered alfo by the IMafter of the Red-lyon inn, Barnet. Was my beer, worthy Peat, from excise but once free, 1.3 With friend Weft, and Mifs Stow, I merry would be; Good fare I'd pruvide 'em, with liquor fo fine; Gough, Coleedee and Simpinin fhould oft with me dine; ? For fucb be the gents, that help t' keep up my fign.

Anfuers to the Queries in the laft Year's Drary.

1. Anfwered by Mr. John Jackson.

This reafon proceeds partly from all the three caufes mentioned in the Query. 1. The air within it, not only fupports the ambient air, but alfo the two abutted elliptical domes, 2. Thofe elliptical domes

## 26 Ænigmas in $177^{8}$ anfwered. $\quad \mathrm{N}^{\circ} 39$.

bear a preffure equal to arches (every way) on this conftruction, which cannot be forced logether, fo long as the materials laft; therefore, $3^{\text {dly }}$, The hands being of a fofter texture than thefe materials cannot break it.
2. Query anfwered by Mr. Benjamin Cieypole.

Crowns are defined to be an ornament, \&c. and as fuch, I find they were originally ufed; as may be feen, Exodus xxv. v. 11. where a golden crown was to ornament the ark, \&c. and verfe 25 , the fame ornament for the table, \&c, and (per query) " and who may be faid to have wore the firft gold one!" If we compare the 30 th verfe of the 2gth cbap. of Exodus with the 6th verfe of the 29th cbap. it will appear that AAron was the firf that wore a cold cerown, \&c.

## Mr. William Swift; anfwers the 3d Query, thus:

One Simun Eyre, a fhoemaker, being chofen Lord Mayor of London, made a pancake-feaft on Sbrove Tuefday, for all the apprentices in LONDON ; and from that time it became a cuftom.

He ordered, that upon the ringing of a bell in every parifh, the ape prentices fhould leave work, and fhut up their fhops for that day; which being ever fince yearly obferved, is called the pancake bell. He made them a large feaft of pudding-pies, and pancakes: and what remained when all had dined, was given to the poor. Then after, in that year, he built Leadenball.

In aniwer to the 4 th Query Mr. Joseph James fays; That, coaches were firf introduced into England, in the year 1155 . But Mr. K. F. I. London, fays, coaches were firft introduced into England, in the year 1589 ; and backney-coacbes in the year 1693. The firf fratefman that ever fet up this equipage, was Fobn de Laval de Bois Daupbin; who could not travel on borfeback on account of his enorm us bulk. Queen Elizabetb, as we find by hiftory, ufed to go even to the parliament houfe on horfeback.

Since the paradoxes take up fo mucb room, and to fo little purpofe; feveral ingenious correfpondents have advifed, and defired me, not to infert any fchemes of that kind this year: therefore fhall proceed to, New Ænigmas to be anfwered in the next Year's Diary.

## 1. Enigma 3i8. By Mr. George Brentane, of Nermanton upon Soar.

Each Diarian bard muft own my cafe hard!
I'm black, both witbout and within: My mafier's a clown, drags me up and down And has cut a great hole in my fkis; Before this was my lot, I fill'd many a pot, And rejoiced the young and the old, Buth my Mafier and Mi/s, my lips they would kifs, Whilft a good merry ftory was told. I was much with the poor, and out $0^{\prime}$ door,
'When the weather was pleafant and warm, I was dragg'd by the nofe, and ne'er did oppofe, And they knew I fhould do them no harm;

## The Gent. Diary; or, Math. Repofitory. 27

Was not faucy nor nice-nor e'er play'd at dice,
And yet, fuch hard fate was my lot;
I came off a cows but I cannot tell how :
You may think by a bull I was got.
 Sbeffeld, anfwering all the ENICMAs in the laft year's Diary.

Fierce Boreas bent on wild defiruction, raves,
Lathes his fides, drives the tremendous waves;
From deep abyfs! th' impetuous furges roam,
And in the face of Heaven fpit their foam!
Whilft Latium's bard-he makes his bero rove,
Thro' unknown ftrands, the fugitive oi Jove.
To bim I lent my aid; -and as he pleas'd,
I rous'd the billows, or the forms appeas'd!
I fkill'd in fong, in tuneful order ftand;
Wonders to fhow of heaven, air, feas, and land:
Let Magic-Lanthorn ber perfeetions thow,
When Darkness reigns, ard brings her charms to view :
Let her roufe up heroes of STRENGTH from far,
Acbilles, Ajax, or the God of war!
With nobler fcenes than thefe I feaft the eyes;
I lift each god-like mortal to the $\mathbb{R}$ ies !
Whilft only foe dumb effigies purfue,
I bring both life and action up in view !
I truth can tell, or fallhood can devife,
Exceed the truth, or mingle truth with lies!
I' $m$ call'd the darling of the delpbic maid,

Honour, vice, virtue, SCANDAL, are my trade!
1
Slander, when urg'd by me (ye wits avaft)
Traverfe thro' nations, fwift as winged hafte!
In Wales I've been, $t$ ' heap honors on the leek,
To Latin I'm no ftranger nor to Greek:
Princes-nay kings! to me oft grant the bays,
When I from cork'd up wine ambrofia raife.
My fhapes are many, and more arts endue,
Your friend (difguis'd) than ever Proteus knew!
Whether I in the realms of Pluto rove,
Or in the confines of Idalian Jove,
(It matters not) I've oft fuch talen:s giv'n
As can defcribe hell, empty face, or heav'n!
I charms poffefs to pleafe the grave, the gay;
Frequent the cburcbes, mafquerades, and play!
Garrick, poffefs'd of me, fteps on the ftage,
'Tis by $m y$ aid be charms the lift'ning age;
'Tis I that makes bim pleafe - whilft thro' the dome, Claps (loud as thunder) Shake the vaulted room!
How far more great than Helena I prove,
Who facrific'd vaft rumbers to her love ?

## 28 New IEnigmas, to be anfwered next Year.

For, when $I$ chiodfe Olympian duft to raile,$I$ build on mortals, manuments of praife!My merits are not known to ev'ry fool,But oft abus'd by fons of ridicule;
Down to time pretent, from the days of yoreI've been obferv'd in mathematic lore!My cealing is; wi:h virtue, and with vice,And can tell the vicifitucies of dice!PrizeWhen jokes are us'd, or waggifh puns prevails,I can delight men with their finger-nails;Simine, Gough, Colirdge, have me feen infate, 2 Reb.
Nor am $I$ ftran ${ }_{6}$ er unto ancient PEAT: ..... 1 Reb.
My deeds are ever ufelefs to th' Excise3 Reb.Declare my name, and win the laurel prize.

Ten thoufand thoufands owe their birth to me, To me ten thoufand thoufands bow the knee!
By me, unha pily fome mect with death;
To fome $-I$ ev'n deny the gift of breath:
Tho' now I live on earth, - to me you owe Your being (under GOD)-all that you know: Poets are oft my friends - and oft my foes;
I think, I need not any more difclufe.

$$
\text { 4. 生nigma } 32 \text { r. By Mifs Polly Stow. }
$$

Of arts and fcience Mistresses!-we teach
Lay clerks to fing, -and hallowed ones to preach !
Numbers we fcan,-in Euclid's circles tread;
We round the planets crbs, great Newton lead!
Does this perplex ? attend one myftry more,
The firft and laft-plac'd of our race explore
And tell the names which feraphims adore!
Let others boaft of their fuperior birth,
Delin'ate their pre-eminence and worth;
Be it my care, with cantion to conceal
My pedigree, in ænigmatic tale :
Yet (without vaunting) will relate an age,
Few have attain'd who grace Diaria's page!
E'er fandy defert, or the fady plain
Imbib d the lucid drops of pregnant rain:
E'er fruits nectarean from their bloffoms grew.
Hong on a tree; and bent the pliant bough :
E'er from a branch one virgin bud fhot forth, I took my rife -and rang'd this globe of earth!
Nor am I now lefs active than before,
But ftill retain the fame progreffive pow'r;
Vifit with foft falute umbrageous trees,
Lodge on the tops of fycamores with eale,

## The Gent. Diary; or, Math. Repofitory. 29

Sumetimes from poaibers I the game defend, To wand'ring birds, to quadiupedes a friend: A friend to man -yet is my nature fuch, Regardlefs of the bufy mortals touch, I his embrase elude - his grafp refufe, Thwart his defigi:s_Invalidace his views;
Baffle his fchemes his pleafure to fulfit,
Nor yield obedience to his felfifh will:
My empire o'er, when I'm no longer feen,
Silent memorials fhow where I have been. If yet to greater hunor you wou'd rife,
Draw back the curtain-take ofi this difguife;
To each enquirer fpecify my name,
The clarion's found fhall then your praife proclaim!

## 6. 出migma 323. By Mr, Gearge Langley, of Wrangle, Lino

 colaflite.By whims in drefs, folks play the fool, Invite contempt and sidicule! Reafon in thefe feems meer pretence AS MODE predominates o'er fenfe!

Thus (hear my tale and) you'll agree,
Fantaftic treatment's forc'd on me;
For, fee me now my wings expand,
And by the fire take my ftand;
Where drefs exub'rant I can boalt,
For, in that place I'm cloth'd the mof! !
When fickle fancy's pow'rful fway
Commands, I'm fript of clothing gay;
Made a reclufe ;-nay, what is more,
Am turned naked out of door;
Expos'd to wint'sy winds that blow;
In hoary frofts and fleecy fnow!
Ufage moft ftrange you'll fay t'eadure
Hard and fantartic, to be fure
Yet, howe'er whimfical and vain,
I'm feldom drefs'd expos'd to rain!
Again, -when fummer-funs pervade
The flocks that feek the noon-tide flade
Burden'd, I move with clothing gay,
And front the potent fouzce of day!
Both fexes garbs I wear polite
At once!-tho' no bermaphrodite,
Many there are (it is well known)
My drefs difcarded oft put on;
And, as you Gents the favour thare,
I pray from hence my name declare.

## 30 New Ærigmas, to be anfwered next Year.

7. FEngma 324. By the Pilgrim.

Diarian Gents! your attention a moment,
And then I requeft you to give me your comment.
Ii matters not trom whence 1 came,
Or how I firft receiv'd my name;
Let this fuffice-In days of yore,
'Fore England iaw a black-a-moor;
I ne'er was heard of-never feen,
By fubject, nor by King nor Quén !
But now, contrarieties take place,
And quite reverfe you'll find the cafe:
You'll fcarce an habitation find,
(Except for beafts) but there's affign'd;
A throne for me; where prim I ftand,
Like one who tways with fole command!
When I was borne I was defign'd,
A gen'ral friend to all mankind;
And yet (tho' few) fome men will rail,
And think my fervices grown fale:
Unkindeft treatment to the fair,
From whom I ev'ry bleffing fhare!
True as the light that glads the day,
My welcom'd fervices I pay;
My bafis when I ftand upright,
Is broader than is requifite;
Yet,-fad cataftrophe to tell!
'Tis known I from my throne have fell,
Down to the flreaming flood below,
And caus'd an inundations flow;
For which offence no pardon's given,
No patronage receiv'd from Heaven;
And if not death,-revenge they cry!
Straightway I then am hurl'd on high,
And by the neck in ruthelefs chains,
I'm bound fo long as life remains.
Now fons of the Muses your talents difplay,
And tell who I am that's fo tortur'd I pray.
8. Enigma 325 . By Mr. Thomas Truswell, of Nun-Eatono

Ye prying wits, who can with half an eye,
The meaning of the darkeft hint defcry;
Attend to me an harmlefs franger fure,
Who feemis at prefent in a drefs obfcure;
My form (ye Gents) is oft ambiguous found,
I'm fquare, I'm oval, and fometimes I'm round:
In various culours I am always feen,
In blue, or purple, os the verdant green;

## The Gent. Diary; or, Math. Repofitory. 34

With due attention, look but in my face,
The rofe and li'y there, perhaps you'll trace;
Woodbines anid vi'lets curioufly entwin'd,
Or, juft what pleales beft my mafter's mind :
I'm always handied with peculiar care,
Both morn and $e^{5}$ ning wait upon the fair;
With elemental fweets I'm often grac'd,
Such fweets as pleafe the faireft lady's tafte:
Shou'd Doll by accident but make a irip,
Or loofe her hold, or fuffer me to flip;
Down falls a tribe! a moft deftructive band,
The bane of thoufands in the Britifb land.
By what is faid, I make no longer doubt, But ye Diarian bards will find me out.
9. Ænigma 326. being the Prize Ænigmathis Yeary By Mr. Benjamin West, of Weedon-beck.

> Ardua prima via eft; Ultima prono via eft._Ovid.

Two travellers in mafquerade prefume
To make a vifit-rideers! Give us room.
True brotbers we, with each a gaping mouth, And known from Eaft to Weft-from North to South; Strange one-ey'd monfters (let the truth be told)
Like Brontes and Pyracmon, fam'd of old!
Tho? fmall in fature, each exterior part,
Defies the fpear, and mocks the pointed dart.
Above the earth we oft difplay our forms,
When angry Jove beftrides the threat'ning forms is
Cas'd in bright armour, like old $P_{\text {selus' }}$ ion,
We feel no fears, no dangers ftrive to thun;
When thund'ring peals from heav'ns high arch refound,
And fheets of livid vengeance glare around:
When thro' the world bellona fpreads alarms,
And bids the Britifb Lion roufe to arms;
Each chief participates the martial flame,
And each impatient bofom pants for fame!
Anon the trump, fhrill founding from afar, Infpires a pleafing dread ! ——The kindled war
Begins to rage - fee "might oppos'd to might,"
And fnorting fteeds anticipate the fight.
Now we appear amidft the marfhal'd train,
And bear the hero o'er th' embattled plain;
With dauntlefs fpeed we rufh upon the foe,
While thro' our mouths the crimfon torrents flow.
Yet, not to fcenes of war alone confin'd,
In fports and bufinefs we've our parts affign'd:
When

## 32 New Ænigmas, to be anfwered next Year.

When pleafure calls, we join the jovial chace, And never fail to mingle in the race; Attend eleciiontering cavalcades; And, like the dryads haunt the fylvan fiaces. Purfu'd by parpers, oft we urge our fight O'er dreary paths, involv'd in thades of nighta Princes and courtiers on our aid depend, Priefts, lazoyers and pbyficians we befriend; But may perchance, deceive them in the end. So irail (alafs!) is ev'ry earthly truft, So foon my pride be humbled in the duft! This truth perpend - and foorn the thin difguife By us, may monarcbs fall-and vaffals rife.

IRebus by Mr. Wifliam Swift.
From the reverfe to beat take a hundred, you'll fee, If you live to twice fifty, what then you will be.
2. Rebus by Mr. Anthony Temple。

If to a diverfion connected there be, One half of the place where I can be mof free; Thefe, when rightly united a name will complete, Of an extenfive genius of an ancient date.

3 Refus by Mr. Benjamin Cefypole. One ibird of a thing which boys oft whip about, One fifib of what mifers will not do without ; One $j_{3 x}$ t $b$ of a man that's reputed a thief, (Altho' he affords moft people relief) One balf of a grain that's old England's fupport, Will name a DiARIAN (you may take my word for't.)

## i Query by G. H. Nottingham.

Pray Gentiemen will you this query explain, If a man with long feet, an advantage does gain;
Of one who has ficrter? -Determine I pray; Tho' their legs of a length (in a long fummer's day.)

$$
2 \text { Query by Mr. Patrick Hall. }
$$

IT appears from cbrorelogy, that the firf appearances of the aurora borcalis, or northern lights, was in the year 1718 ; and feveral mathematicians fince, have faid; that they proceed from the vapours afcending by exhalation: if fo; what is the reafon they did not appear before the faid year 5718 .

$$
3 \text { Query by Mr. John Jackson. }
$$

Why do buddocks, as well as fome other frefh fifh, when hung up in dark places, appear to reflect a frong lighto

Answers

N? 39. Gent. Diary; or, Math. Repolitory. 1779.
Answras to the Questions in the laft Year's Diary.

1. Ques.6.629. anfwered by Mr. ALEXANDER Rowe.

First; $3 x+z$ ought to have been printed inftead of $x v y+z$. Then, put $14158=a ; 43415089=6$; and $52 \% 6=c$. Then, from the firt and third equations by reduction we have $z=\underline{a+x-x y}$ $=c-3 x: y y=\frac{a+x}{c-2 x}$. Hence, $z$ being $=c-3 x ; z^{2}=\frac{y}{c-3 x)^{2}}$; and $\left.y^{2}=\frac{a+x}{c-2 x}\right]$; which put for $\approx, z^{2}$, and $y^{2}$, in the fecond equation; we thence $y=9$, and $z=14$, confequently this amiable Fair was 23 years of age the 14 th day of September, 1777 .
2. Quest. 430. anfwered by Mr. Wileitam Winn. $\mathrm{PUT} n=5 ; m=6 ; a=$ area of the triangle, $s=\mathrm{S}_{4} 5^{\circ}, x$ and $y=\mathrm{S}$, and cof. $\angle \mathrm{CAD} . z=A D$;
then $s x+y x=s$. $<\mathrm{BED}_{\text {; }}$ and $n: m:: x:$ $\frac{m z}{n}=\mathrm{BE}$, and $I$ (Radius) $\frac{m z}{n}:: s x+s y: \frac{m z}{n}$ $X s x+s y=B C$; then $x y(A C): \frac{m z}{n} \times s x+s y:: 1:$ $\frac{m}{n y} \times s x+s y=$ tang. <BAC. and $\frac{m}{n y} \times s x+s y$ $=\frac{2 x y}{y^{2}-x^{2} .}$. Then put $e=\frac{2 n}{m s}-1 ;$ and $y^{3}-x^{3}-A$

$x^{2} y=e y^{2} x$; then by writing $\sqrt{1-x^{2}}$ for $y$ its equal ; $x$ is eafily found $\Rightarrow, 434553$ let the area be what it it will. Then put $a=$ the given area $; s$, and $c$, 三 the nat. fine and cofine of the $<B A C=51^{\circ} 38 \prime$; then $B C=\frac{\sqrt{2 s a}}{c}$ and $A C=\sqrt{\frac{2 c a}{s}}$.
3. Quest. 43 I . anfwered by Mr. Isaac Rowbottom. $\mathrm{L}_{\mathrm{ET}} \mathrm{CF}$, and CB; be the diameters of the given circles; $K$ and L their centers ; abcd $=$ one half of the required parallelogram; draw DE and joinaL, C $6 K$. Then $\overline{E L}^{2}=E F$. $\mathrm{EC}=\mathrm{BE} . \mathrm{EG} \because \mathrm{BE}$ : EC: : EF:EG. and by comp. \&c. $B E+E C: E F+E G$ : : BE:EF, Whence

## Queftions in $\mathbf{1 7 7 8}$, anfwered $\mathbf{1 7 7 9}$.

by divifion as $\mathrm{BC}-\mathrm{FG}(40): \mathrm{GF}(9):: \mathrm{BE}-\mathrm{EF}(23): \mathrm{EF}=5 \frac{7}{40}$
whence the area of the fpace GDFR is very eafily had $=129,46844$. Alfo (by 47 . Eu. 1.) $\sqrt{13^{2}-x^{2}}=K d$, and $\sqrt{16^{2}-x^{2}}=L e$, where $x=$ bd-at $\because \sqrt{13^{2}-x^{2}}+\sqrt{16^{2}-x^{2}}-d \times x=$ the area cabd, a max.
 The fame anfwered by Mr. Wirijam Sherwin.
LET $x=\mathrm{GE}$ (fee laft fig.) then $\mathrm{ED}^{2}=\mathrm{EF} \times \mathrm{CE}=\mathrm{BE} \times \mathrm{GE}=$ $\overline{9-x} \times \overline{17+x}=\overline{3^{2-x}} \times x$; whence $x=3 \frac{33}{40}$; and the area GDFR is eafily had $=129,5$. Now put $z=b d=a \epsilon$; then will $\overline{13^{2}-z^{2}} \frac{1}{2}=$ KD, and $\overline{1^{2}-z^{2} \frac{1}{2}}=L e \because z \times \overline{13^{2}-z^{2}} \frac{1}{2}+z \times \overline{16^{2}-z^{2}} \frac{1}{2}-11 z$ $=$ the area of the parallelogram eabd $=a$ max. in fluxions, $\mathcal{E}^{2} c . z=$ 6,265 , and the area $=76,6$ nearly.

The fame anfwered alfo by Mr. William Winn.
17 Describe the two quadrants LRO, HRP. Then put $\mathrm{AR}=7,825=a ; \mathrm{DR}=$ : $2,175=e$; radius $C R=r$, and $M R=n$; and IG=KF=x. Then $\sqrt{r^{2}-x^{2}}=\mathrm{GB}$. and $\sqrt{n^{2}-x^{2}}=$ FE. And $\sqrt{r^{2}-x^{2}}-a=$ IN. And $\sqrt{n^{2}-x^{2}}-2=K N$. Then, $x$ $\sqrt{r^{2}-x^{2}}-a x+x \sqrt{n^{2}-x^{2}}-e x=a$ max.
 and $\frac{r^{2}-2 x^{2}}{\sqrt{r^{2}-x^{2}}}+\frac{i n^{2}-2 x^{2}}{\sqrt{n^{2}-x^{2}}}=a+c=20$. And reduced, $x$ is eafily found $=6,26534$; and the area of the greateft infcribed parallelogram is 76,5985 .
4. Quest. 432. anfwered by Mr. Thomas Walker.
$\mathrm{Le}_{\mathrm{ET}} \mathrm{R}=\mathrm{r}, 0 \mathrm{O}, \mathrm{P}=8400$; and put $x=$ the time in which the debts will be equal. Then we fhall have $13 \mathrm{R} x+23 \mathrm{R} x-1+33 \mathrm{R} x-2+43 \mathrm{R} x-3$ $\bigotimes^{6} c$. to $x$ terms $=\mathrm{C}$ 's debt in the time $x=\mathrm{R} x \times: 1+23 a+3^{3 a^{2}}+4^{3} a^{3}$ E ${ }^{\circ}$. (by writing $a$ for $\frac{1}{\mathrm{R}}$ ) the, fum of which feries infinitely continued will be $\mathrm{R} x \times \frac{1+4 a+a^{2}}{1-a]^{+}}$(by P. 223 Simpon's Algebra) but as $x$ term3 is only wanted, the fum of the remaining terms muft be found, and deeucted from the whole infinite feries. Now it is evident (by the law of the feries) the $x$ term will be $\mathrm{R} x \times \times 3 a^{x-1}$; and the following terms will be $\mathrm{R} x \times: \overline{x+1}] 3 \times a^{x}+\overline{x+2} 3^{3} \times a^{x+1}+x+3 / 3 \times a^{x+2}+8 c$. $=\mathrm{R} x \times: \overline{x^{3}+3^{x^{2}}+3^{x+1}} \times a x+\overline{x^{3}+6 x^{2}+12 x+8} \times a^{x+1}+$ $\frac{x^{3}+9 x^{2}+27 x+27}{x a x+2}+\underbrace{}_{6}$

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Now thefe terms properly coilefted will form the four following infinite feries.
$\mathbf{R} x \times\left\{\begin{array}{l}x^{3} \times: a^{x}+a^{x+1}+a^{x}+2+a^{x}+3+\varepsilon^{\circ} c \cdot \\ 3 x^{2} \times: a^{x}+2 a^{x+1}+3^{x+2}+4 a^{x}+3+\varepsilon^{\circ} c . \\ 3 x \times: a^{x}+4 a^{x+1}+9 a^{x+2}+16 a^{x}+3+\delta^{2} c . \\ a^{x}+8 a^{x+1}+27 a^{x+2}+64 a^{x}+3+\sigma^{\circ} c .\end{array}\right.$ Whofe Sums
if infinitely continued will be $x 3 \mathrm{R} x_{a} x \times \frac{1}{\mathrm{I}-a} ; 3^{x^{2} \mathrm{R} x_{a} x} \times \frac{\mathrm{T}}{I-a_{1}^{2}}$; $3 \times \mathrm{R} x_{a} x \times \frac{1+a}{1-a^{3}} ;$ and $\mathrm{R} x_{a} x \times \frac{\mathrm{I}+4 a-a^{2}}{1-\left.a\right|^{4}} ;$ but $\mathrm{R} x_{a} x=\begin{aligned} & \mathrm{R} x \\ & \mathrm{R} x\end{aligned}=\mathbf{1}$. Therefore $\frac{x^{3}}{a} ; \frac{3 x^{2}}{1-\left.a\right|^{2}} ; \frac{3^{x-3}-3 x a}{1-a^{3}} ;$ and $\frac{1-4 a+a^{2}}{1-\left.a\right|^{4}}$ will be the fum of each feries refpectively. Therefore the fum of $x$ terms or $C$ 's debt in the time $x$, will be $\mathrm{R}^{x} \times \frac{1+4 a+a^{2}}{1-a)^{4}}-\frac{x^{3}}{1-a}-\frac{2 x^{2}}{1-a a^{2}}-$ $\frac{3^{x+3}+a}{1-a 3}-\frac{1+4 a+a^{2}}{1-a)^{+}}$. And A's debt in the time $x$ will be PR $x$ $300 \times: \mathrm{R} x+2 \mathrm{R} x-1+3^{2} \mathrm{R} x-2+4 \mathrm{R} x-3=\mathrm{PR} x-100 \mathrm{R} x \times: \mathrm{r}$ $\mp 2 a+3 a^{2}+4 a^{3}+8^{3} c$. to $x$ terms, which will be had by proceeding as above, $=\mathrm{PR} x-100 \times \frac{\mathrm{R} x}{1-4]^{2}}-\frac{x}{1-a}-\frac{1}{1-a^{2}}$. Then (per 2uef.) $\mathrm{R}_{x} \times \frac{1+4 a+a^{2}}{1-\left.a\right|^{4}}-\frac{x^{3}}{1-a}-\frac{3 x^{2}}{1-a}-\frac{3 x+3 x a}{1-\left.a\right|^{3}}-$
$1+\frac{4 a+a^{2}}{1-a_{1}^{4}}=\mathrm{PR}_{x}-100 \times \frac{\mathrm{R} x}{1-\left.4\right|^{2}}-\frac{x}{1-a}-\frac{1}{x-\left.a\right|^{2}} \cdot$ Which put into numbers and reduced, we have $54641 \mathrm{R} x-x^{3}-63 x^{2}$ $2683 x=55041$. folved, $x=11,3985$ years nearly the time when the debts are equal; which anfwers the firf part of the queftion. Then, by making $\mathrm{R} x \times \frac{1+4 a+a^{2}}{1-\left.a\right|^{4}}-\frac{x^{3}}{1-a}-\frac{3 x^{2}}{1-\left.a\right|^{2}}-\frac{3 x+3 x a}{1-\left.a\right|^{3}}-$ $\frac{3+4 a+a^{2}}{1-a 1^{4}}=8400 ;$ we have $x=12,524$ the time when $C^{\prime}$ 's debt will be 84001 . Now it appears, from a little confideration; that $A$ 's debt will be greateft, when the intereft thereof for any interval of time, becomes equal to his payment to B at the fame time; confequently, $\mathrm{PR} x$ $-100 \times \frac{k x}{1-\left.a\right|^{2}}-\frac{x}{1-a}-\frac{1}{1-a}=\frac{\frac{1}{100 \times 1+x}}{, 05}$. From whence, we get $x=3,575$ years, when A's debt will be the greateft. Again, by by making $P R x=100 \times \frac{R x}{1-\left.a\right|^{2}}-\frac{x}{1-a}-\frac{1}{I-\left.a\right|^{2}}=0$. We get
$=15,865$ years, the time when A's debt will be paid; at which time C's debt will be $21 \% .1 \mathrm{gs}$.8 d .
5. Quest. 433. anfwered alfo (only) by the fame.

Let $P$ reprefent the pole, HO the horizon, \&c. and S the place of the fun when his altitude was $32^{\circ} 17^{\prime} 3^{\prime \prime \prime}$; and $s$ his place one hour after. Then, in the ifofceles triangle SPs, there are the two fides and the included angle given hence the perpendicular $\approx \mathrm{P}=71^{\circ} 42^{\prime} \quad 13^{\prime \prime}$ and half the bafe Sv 三屰 $7^{\circ} 7^{\prime} 30^{\prime \prime \prime}$; which taken from the complement of the given altitude;
 leaves $\mathrm{Z}_{v}=50^{\circ} 34^{\prime} 54^{\prime \prime}$. Then, in the right angled triangle $\mathrm{Z}_{u} \mathrm{P}$ we have $\mathrm{Z}_{v}$, and $v \mathrm{P}$ given; hence the latitude is $I I^{\circ} 30^{\circ}$.
6. Quest. 434. anfwered by Mr. Wilitam Winn.

Put $n=a+b^{2}$, then the given equation becomes $n y^{2}-n x^{2} y^{2}=$ $x^{2 m}$; and $y^{2}=\frac{x^{2 n}}{n-n x^{2}} ;$ then $y=\overline{\left.n-n x^{2}\right]^{-\frac{1}{2}} \times x^{m} \text {; and the }}$ fluxion of the area is $\dot{z}=\overline{n-n x^{2}} \frac{\pi}{2} \times x^{m} \dot{x}$; and the fluent by Form $x^{m+5}$ $\frac{1}{4 n+4+16}$ © ${ }^{\circ}$.

The fame anfwered by Mr. Edward Parnel.
By reducing the given equation of the curve we get $y=\sqrt{a+b^{2}}$ $\times \sqrt{1-x^{2}}$; therefore the fluxion of the area $=\dot{x} y=\frac{1}{\sqrt{a+b^{2}}} \times j$ $\frac{x^{n} \dot{x}}{\sqrt{1-x^{2}}}=\frac{1}{\sqrt{a+b^{2}}} \times x^{n} \dot{x}+\frac{x^{n}+2 \dot{x}}{2}+\frac{3 x^{n}+4 \dot{x}}{2 \cdot 4}+\frac{3 \cdot 5 x^{n}+6 \dot{x}}{2 \cdot 4 \cdot 6}$ $+\frac{3 \cdot 5 \cdot 7 x^{n+8} \dot{x}}{2 \cdot 4 \cdot 6 \cdot 8} \mathcal{F}_{c .}$ And its fluent $=\frac{1}{\sqrt{a+b^{2}}} \times \frac{x^{n+1}}{n+1}+$ $\frac{x^{n+3}}{2 \cdot \overline{n+3}}+\frac{3 \cdot x^{n}+5}{2 \cdot 4 \cdot \overline{n+5}}+\frac{3 \cdot 5 x^{n+7}}{2 \cdot 4 \cdot 6 \cdot n+7}+\frac{3 \cdot 5 \cdot 7 \cdot x^{n}+9}{2 \cdot 46 \cdot 8 n+9}$ ©c. the required area.

> The fame anfwered by Mr. Wilifam Sherwin.
$F_{\text {ROM }}$ the equation of the curve $y=\frac{x^{m}}{a^{2}+b^{2} \times \sqrt{1-x x}}$; whence $\dot{x} y=\frac{x^{m} \dot{x}}{a^{2}+b^{2}} \times \sqrt{1-x x}=$ fluxion of the area; and its fluent $\frac{x^{m+1}}{a^{2}+b^{2}} \times: \frac{1}{m+1}+\frac{x x}{2 \cdot \overline{m+3}}+\frac{1 \cdot 3 \cdot x^{4}}{2 \cdot 4 \cdot m+5}+\frac{1 \cdot 3 \cdot 5 \cdot x^{6}}{2 \cdot 4 \cdot 6 \cdot m+7}+$

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$\frac{1 \cdot 3 \cdot 5 \cdot 7 \cdot x^{8}}{2} \mathfrak{F}_{c}=$ the area required.
2.4.6.8m+9

7 Quest. 435. answered by Mf. Isaac Rowbottom.
$L_{E T} A B Q$ S represent the garden; $A C B$ and QCS the the two equal canals; FGH, and efg $b$ the two nurferies; draw the ordinates PP; Pe; and PT, which will be a tangent to the curve at P . Put DC $=15=a ; \mathrm{AD}$ $=3=b ; \mathrm{Gr}=x$; and $\mathrm{P}_{r}=\mathrm{CR}=y$; then, from $\mathbf{A}$

the given equation $p^{2} x=y 3$; we have $\dot{x}=3 y^{2} \dot{y}$ (by making $\mathrm{P}=1$ ) $\because$ 1) $\frac{x y}{\dot{y}}=3^{x}=\mathrm{RT}={ }_{3} \mathrm{CR}=3 y$ (because $\mathrm{Pr}=\mathrm{CR}$ ) and by the property of the curve ACB , we have $\mathrm{PR}=b \sqrt[3]{\frac{y}{a}}$; whence by fimilar trioangles $\mathrm{RT}: \mathrm{PR}:: \mathrm{P}_{r}: r t=\frac{b}{3} \sqrt[3]{\frac{y}{a}}=\sqrt[3]{\frac{y}{a}}$ (becaufe $b=3$ ): Again from the equation $p \dot{y}^{2}=y^{3}$, we have $\dot{x}=\frac{3 y^{2} \dot{y}}{2 x} \because \frac{\dot{x}^{y} y}{\dot{y}}=\frac{3}{2}$ $x=r t=\sqrt[3]{\frac{y}{a}} \because y=\frac{27}{8} a x 3$; alfo, by the property of the femicubic parabola HGF, we have $\overline{\mathrm{Gr} 2}: \overline{\mathrm{Pr}} 3:: \overline{\mathrm{EG}]^{2}: \overline{\mathrm{EF}}}=$
$\left.\frac{27}{8} a x^{3}\right|^{3} \times\left.\frac{2 \overline{2 b-7 x}}{2}\right|^{2} \div x^{2}$. Consequently $\frac{\left.\overline{27} a x\right|^{3} \times \frac{2 \overline{b-7 x}}{2} \div\left. x^{2}\right|^{\frac{7}{3}}}{}$ $\times \frac{\overline{2 h-7 x}}{2} \times \frac{3}{5}=$ the area of the femiparabola EFG a Max. In fluxions $7 x^{6} \dot{x} \times \overline{2 b-7 x}{ }^{5}-35 x^{7} \dot{x} \times \overline{2 b-7 x} 4$ reduced, $x={ }_{6}^{1} b=$ $\frac{\mathrm{x}}{2} \because \mathrm{GE}=1 \frac{\mathrm{~T}}{4}, \& \mathrm{EF}=1,16565$.

Again, as $\mathrm{DC}: \mathrm{DB}_{3}:: \mathrm{RC}: \mathrm{Re}_{e}=b \sqrt[3]{\frac{y}{a}} ;$ then $\mathrm{DB}-\mathrm{R}_{f}=f$ $=b-\sqrt[3]{\frac{y}{a}} \because$ ff $\times g e=b-b \sqrt[3]{\frac{y}{a}} \times 2 y$ area efg $b, 2$ max. fluxed $\mathcal{E}^{2} c . y=, 6328125$. Laftiy, from the equation $p^{2} x=y^{3}$, we have $y \dot{x}=3 y y^{3} \dot{y}$ the fluxion of the area of the curve (or canal) ACB, whole fluent is $\frac{3}{4} x y$; but when $x=a, y=b \because \frac{3}{4} a b=6,75$ fquare chains, the area of the canal ACB. Also, $1,748475=$ the; area of the nor-

$$
\mathrm{C}_{3}
$$

fury

38 Questions in $177^{8}$, anfiwered 1779.
fry HGF; and, 94921875 square chains $=$ that of the nursery efgb, from whence all that is required may be eafily known.

Otherwise. Let $A D Q Y=\frac{\pi}{2}$ of the garden; $A C D$ and $Q C Y=$ $\frac{\pi}{2}$ of the canals; HGF, and IPKP the nurferies. Produce KP to R , and fut $\mathrm{AD}-b=3 ; \mathrm{DC}=1 \frac{1}{=}=a ; \mathrm{PR}=y$. Then $\mathrm{Pr}=\mathrm{CR}$ $=a y^{3} b .-3 \times \overline{b-y}=$ the area of EXP, a max. fluxed Etc. $y=$ $\frac{a}{4} b$. Now it is well known that the fubtangent to the femicubic parabola is $\frac{2}{3}$ of its corresponding abfc. $\because$ (by Simpler's Geom, p. 201.) as $\frac{3}{2} \mathrm{Gr}: \mathrm{PP}:: \frac{3}{2} \mathrm{Gr}+\mathrm{Er}: 2 \mathrm{PP}$. Hence $\mathrm{G} r=\frac{1}{2}$. Then, as $\overline{\frac{1}{2}}^{2}$ : $\overline{\mathrm{PF}}{ }^{3}:: \mathrm{GE}: \overline{\mathrm{HF}}{ }^{2}$; and $\mathrm{HF}=2,3313$, the fame as above.

The fame anfwered by Mr. Thomas Walker.
Let $A B C D$ reprefent half the garden, AVB one half of the canals, and half the parabolic nurfery; and HIK half the rectangular one; and let PT be a tangent to each curve at the point $P$; and through $P$, draw He parallel co CD , and put $x=u r, S$ and $y=\mathrm{Pr}=\mathrm{RV} ; a=\mathrm{SV}=3$, and $b$ $=\mathrm{SA}=1 \frac{\mathrm{I}}{2}$. Then (Ex. 3 P. 203 Emerson's fluxions) the fubtangent $r t=\frac{3}{2} r v=\frac{3 x}{2}$;
 and the fubtangent $\mathrm{RT}={ }_{3} \mathrm{RV}=3 y$, and by the property of the curve, $a: b 3:: y: \overline{\mathrm{RP}}{ }^{3} \because \mathrm{RP}=b \sqrt[3]{\frac{y}{a}}$; And (by fimilar triangles) RT $; \mathrm{RP}:: \mathrm{Pr}: r t=\frac{b}{3} \sqrt[3]{\frac{y}{a}}=\sqrt[3]{\frac{y}{8 a}}$ (because $b=1 \frac{1}{2}$ ) therefore $\sqrt[3]{\frac{y}{8 a}}=\frac{3^{x}}{2} \because y=27 a \times 3$, and $\mathrm{D} v=b-b \sqrt[3]{\frac{y}{a}}+x$ $=\frac{3-7 x}{2}$; then by the property of the curve, $\left.\left.\overline{r_{2}}\right|^{2}:\left.\overline{\mathrm{P}}\right|^{3}:: \overline{\mathrm{D}_{v}}\right]^{2}$ $\left.\left.\left.: \mathrm{D}_{a}\right]^{3} \because \mathrm{D}_{a}=\left.\overline{27 a x_{3}}\right|^{3} \times \overline{\frac{3-7 \lambda}{2}}\right]^{2} \div x^{2}\right]^{\frac{x}{3}}$ (and by Ex. 2. page $25^{2}$ of the above quoted fluxions) $\overline{27 a \times 3}]^{3} \times \frac{\overline{3-7 x^{2}}}{2} \div\left. x^{2}\right|^{\frac{1}{3}} \times \frac{3-7 x}{2}$ $\times \frac{3}{5}=$ the area of the femiparabola $a w \mathrm{D}$. In fluxions, $\widehat{\delta}^{\circ} c, x=\frac{1}{4} \because$ $y=\frac{81}{64} ; v \mathrm{D}=\frac{5}{8} ; \mathrm{D} a=2,3309$; and the area of the femiparabola $=8742375$; and, $8742375 \times 2=148475=$ the area of the whole nurfery.

Again, $a: b 3:: y: R I=b \sqrt{\frac{y}{a}} ;$ and $b-b \sqrt{\frac{y}{a}}=H$, and by $-b y \sqrt{\frac{y}{a}}=$ the area of the parallelogram IHCK $=$ a maximum

N•• 39. Gent. Diary ; or, Math. Repofitory, 1779. 39 in fluxions and reduced $y=\frac{81}{64}=\mathrm{HC} \because: 1 \mathrm{IH}=\frac{3}{8}$; and the area of the whole nurfery $\frac{81}{64} \times \frac{3}{8} \times 2=94921875$; and the area of each of the canals $=\frac{3 \mathrm{BA} \times \mathrm{VS}}{2}=6,75$, and the remaining part of the garden $x, 80230625$ fquare chains.

The fame anfwered by Mr, William Percivalo
Put $b=150=\mathrm{AB}$, and $a=300=\mathrm{DB} ; x=\mathrm{EF}$. Then $p^{2} \mathrm{y}$ $=3 y^{2} \dot{y}$, and $\dot{x}=\frac{3 y^{2} \dot{y}}{p^{2}} \because \frac{3 y^{2} \dot{y}}{p^{2}}$ $=$ the fluxion of EFG; whofe fluent $\frac{3 y^{4}}{4 p^{2}}=\frac{2 p^{2} x y}{4 p^{2}}=\frac{\rho^{x y}}{4}=$ the area of the fpace EFG $\because \cdot$ $\frac{3^{a b}}{4} \times 4=3 a b=135000 \square$ links

$=I A, I R, I 6$ perches $=$ area of the canals. Then, by the nature of the canals, $a: b 3:: x: \frac{x b 3}{a}=\overline{\mathrm{FG}}^{3} ;$ and $\mathrm{FG}=b 3 \sqrt[3]{\frac{x}{a}}$ $\because \mathrm{GC}=b-b \sqrt[3]{\frac{x^{4}}{a}} ;$ and $b x-b \sqrt[3]{\frac{x^{4}}{a}} ;$ or $x-\sqrt[3]{\frac{x^{4}}{a}}=$ a maxim. which put into fluxions and reduced gives $2 x=\frac{27 a}{3^{2}}$ 253,125 links the length of the required rectangle; and putting $\frac{27 a}{64}$ for $x$ in the value GC above, we get GC $=\frac{x}{4} b=37 \frac{\pi}{2}$ links $=$ the breadth: hence the area $=15$ perches. Now, from the curve HNK, whofe equation is $p x^{2}=y^{3} \because^{\circ} y=p \frac{x}{3} x^{\frac{2}{3}}$; which $p \frac{1}{3} x \frac{2}{3} \dot{x}$ is the fluxion of the required curve, whofe fluent is $\frac{3 p \frac{1}{3} x \frac{2}{3}}{5}=\frac{3 y x}{5}$; there fore this curve being $\frac{3}{5}$ of its circumfcribing rectangle, when the rectangle is the greateft, the curve will be fo too; whofe bafe and diameter are $=$ the length and breadth of the rectangle $=\frac{253,125 \times 37,5 \times 3}{5}$ $=5695,3125$ links $=9$ perches the area of the required curve, the remainder or the garden $=1 \mathrm{R} .08 \mathrm{P}$.

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8. QuEST.

## 8 Quest 436 anfwered by Mr. Edward Parnez.

Let $x \approx$ be wrote for $y$ in the given equation, and it becomes $x^{3}+$ $x^{3} z+x^{3} z^{3}=a x^{4} z^{3} ;$ whence $1+z+z^{3}=a x z^{3}$; and therefore $x=$ $\frac{1+z+z^{3}}{a z^{3}} ; y=x z=\frac{1+z+z^{3}}{a z^{2}} ;$ and $\dot{x}=\frac{3 \dot{z}+2 z \dot{z}}{-a z^{4}} ;$ and confequently $p y^{2} \dot{x}=p \times \frac{\overline{1+z+z)^{2}}}{a z^{2}} \times \frac{3 \dot{z}+2 z \dot{z}}{-a^{4}}=$ the fluxion of the Solidity; the correct fluent of which is $\frac{p}{a 3}$
$\times \frac{3}{7 z^{1}}+\frac{4}{3 z^{0}}+\frac{7}{5 z^{3}}+\frac{2}{z^{4}}+\frac{10}{3 z^{3}}+\frac{2}{z^{2}}+\frac{3}{z}+2 \times$ hyp. log. $\frac{z}{b}-\frac{p}{a^{3}} \times \frac{3}{7^{67}}+\frac{4}{3^{b^{6}}}+\frac{7}{5^{b}}+\frac{2}{b^{4}}+\frac{10}{3^{b 3}}+\frac{2}{b^{2}}+\frac{3}{b}$ (where $p=$
 $=0$ ) or by writing $\frac{y}{x}$ for its equal $z$, we have $\frac{p}{a_{3}}$ $\times \frac{3 x^{7}}{7 y^{7}}+\frac{4 x^{6}}{3 y^{6}}+\frac{7 x^{5}}{5 y^{5}}+\frac{2 x^{4}}{y^{4}}+\frac{10 x^{3}}{3 y^{3}}+\frac{2 x^{2}}{y^{2}}+\frac{3 x}{y}+2 \times$ hyp. log. $\frac{y}{b x}$ $-\frac{p}{a^{3}} \times \frac{3}{7 b^{9}}+\frac{4}{3 b^{6}} \div \frac{7}{5 b^{5}}+\frac{2}{b^{4}}+\frac{10}{3 b^{3}}+\frac{2}{b^{2}}+\frac{3}{b}=$ the folidity required.

The fame anfwered by Mr. Isaac Rownot tomp
PuT $\frac{x}{v}=y ; 3,1416=p ;$ then $x=\frac{v^{3}+v^{2}+1}{a}$ whence $\dot{x}=$ $\frac{3 v^{2} g+2 v v}{a}$ and the fluxion of the folidity is $p y^{2} \dot{y}=p \times \frac{{\overline{v 3}+v^{2}+1}_{a v}^{a}}{}=$ $\frac{3 v^{2} \dot{v}+2 v \dot{v}}{a}$ whofe fluent is $\frac{p}{a_{3}} \times$
$\frac{3}{2} v^{7}+\frac{4}{3} v^{5}+\frac{7}{5} v^{5}+2 v^{4}+\frac{10}{3} v^{3}+2 v^{2}+3 v+2$ hyp. log. $v$; in which, placing $\frac{x}{y}$ for $v$, gives (when $x$ or $y$ is a given quantity) the folidity required.

9 Quest. 437. anfwered by Mr. Thomas Walker.
$\boldsymbol{P}_{\mathrm{v}} \mathrm{s} ;=$ the fum of the two fides $; a=$ the bafe; $m=16 \frac{1}{12} ;$ and $x=$ the greater fide $;$ then $\$-x=$ the leffer fide, and (prop. 24. B. 2. Emerfon's Geom.) a:s::2x-s: $\frac{25 x-x^{2}}{a^{2}}=$ the difference of the fegments of the bafe $\because \frac{a^{2}+2 s x-s^{2}}{2 a}=$ the greater fegment; and
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$\frac{4 a^{2} x^{2}-a^{2}+2 s x-5^{2} \mid}{2 a}=$ the perpendicular. And by the laws of falling bodies $\frac{1}{m \frac{1}{2}} \times \frac{\left.4 a^{2} x^{2}-a^{2}+2 s x-s^{2}\right]^{\frac{1}{4}}}{4 a^{2}}=$ the time down the perpendicular; and $x \sqrt{\frac{2 a}{m}} \times \overline{4 a^{2} x^{2}-\overline{a^{2}+2 s x-s^{2}}}{ }^{1}-\frac{T}{4}$ and $\overline{s-x}$ $\times \sqrt{\frac{2 a}{m}} \times \overline{\left.4 a^{2} x^{2}-\overline{a^{2}+25 x-s^{2}}\right]^{2}}-\frac{1}{4}=$ the time of falling down the fides. Therefore, $s \sqrt{2 a}_{m}^{m} \times\left.\overline{4 a^{2} x^{2}-\left.\overline{a^{2}+2 s x-s 2}\right|^{2}}\right|^{-\frac{T}{4}}=a$ minimum. In fluxions, $\mathcal{F}^{\circ} c, x \doteq \frac{\left[s^{3}-s a^{2}\right.}{2 s^{2}-2 a}=\frac{s}{2}$; therefore the $\Delta$ is ifofceles.

The fame aniwered by Mr. Edward Parnex. By the principles of mecbanics; the time of defcent down any inclined plane, is as the leagth of the plane directly ; and as the fquare root of its height reciprocally: therefore the times of defcent down the fides C.A and CB (of the triangle $A B C$ will be as $\frac{A C}{\sqrt{D C}}$ and $\frac{B C}{\sqrt{D C}}$ re. Spectively; and their fum as $A C \times B C$ $\checkmark D C ; A$
 which (per quef.) is a minimum. But when $\frac{A C+B C}{\sqrt{D C}}$ is a minimum, the $\sqrt{\overline{D C}}$, and confequently the area of the triangle $A B C$, muft be a maximum, (becaufe $A B$ and $A C+B C$ are given quantities) and $\because$ (per Theor. 5. P. 198. Simplon's Geom. 2d Ed.) $A C=B C, \& A D=$ BD ; and the triangle ABC , an ifofeeles one.

## The fame anfwered by Mr. Adam $\mathrm{O}_{\mathrm{l} \text { iver. }}$

BY mecbazics, the time in falling down the perpendicular $C D$ is as
 $\div \sqrt{\bar{D}}$ which will be a minimum as well as the real time. Now, as $C A+C B$ is a given quantity, it is evident that $\sqrt{C D}$ will be a maximum. The points A and B being looked upon as the foci of an ellipfis; CD will be greateft when it is the femiconjugate of that ellipfis; for by the property of the ellipfis, the femiconjugate is greater than any ordimate parallel to it. Therefore $\mathrm{CA}=\mathrm{CB} ; \mathrm{AD}=\mathrm{DB}$.
10 Quert. 438. admits of neither maximum nor minimum. It not being properly attended to before publication, Eqg. which overfigbt the editor hopes h:s kind contributors will generounly eacure, on account of his then bad ftate of health, boc. And defires Mr. Fojepls Fames (in future) to be more careful in whatever he may propofe to public conideration, soc.

## II. Quest. anfwered by Abdolonimus.

Let E and W, be the caf and went points of the horizon; then, it is evident, becaufe the oirection of the wind was due eaft, that the kite was due eaft from the toy. Therefore, let K the piace of the kite, B that of the boy, KIB the ftsing ; draw the ord. BK, which will reprefent the diftance of the kite from the boy; alfo let C be the place where the fhadow of the kite fell upon the ground; and let DC, BC, KC,
 and $B T$ be drawn; then as BT touches the fring at $B$, it will therefore be a tang. to it at that point. Draw the fubtangent PT, and from K, let fall the IKD. Put $\mathrm{BI}=100=s ;$ tangent $\mathrm{BT}=t=$ $137,3265: 46$ yards; abs. $\mathrm{PI}=x$, its corsefponding femiord. $\mathrm{BP}=y$ fubtangent PT $=v$; and let $a=$ the tenfion of the ftring at I. Then (fuppofing the ftring to form the catenarian curve) we fhall have $s^{2}=$ $2 a x+x^{3}$, and $\frac{s y}{a}=v \cdot \cdot \frac{s^{2}-x^{2}}{2 x}=a=\frac{s y}{v}$ hence, $y=\frac{s^{2}-x^{2}}{2 s x} \times v_{0}$ But (by 47.Eu. I.) $y^{2}=t^{2}-v^{2} \cdot v=\frac{2 s t x}{s^{2}+x^{2}}$; which written for $v$, in the value of $y$ found above, we get $y=\frac{s^{2}-x^{2}}{s^{2}+x^{2}} \times t=\mathrm{BP}$ (by the prep. of the catenary $\frac{s^{2}-x^{2}}{2 x} \times$ hyp. $\log \cdot \frac{s+x}{s-x}$; from whence $x$ is found $=50$, \& then $B K=164,7918176$ yards, the diftance of the kite from the boy.

Again, the fun's decl. at the given time was $1^{\circ} 25^{\prime} 18^{\prime \prime}$ found by proportioning the given hours from noon; confequently, there are given the lat. decl. and hour, to find the fun's alt. $=30^{\circ} \quad 3^{\prime} 8^{\prime \prime}$ to which adding $17^{\prime} 32^{\prime \prime}$ his femidiam and refract. $-8^{\prime \prime}$ his parallax (had from aftronomical tables) gives $30^{\circ} 20^{\prime} 24^{\prime \prime}$ the apparent alt. of the fun'suprer limb; and his azimuth from the eaft rowards the fouth $=\angle \odot \mathrm{DE}=\angle \mathrm{BDC}$, whofe cof, call $b ; \mathrm{BK}=d$, cotang, fun's alt. $=c$; and let $x=$ fine DBK. Then $d x=\mathrm{DK}, c d x=\mathrm{DC}$ ? $d x \sqrt{1-c^{2}}=K C$; and $d^{\prime} \sqrt{1-x^{2}}=$ BD. Alfo by trig. $d$ $\sqrt{1-x^{2}+c^{2} x^{2}-2 b c x \sqrt{1-x^{2}}}=\mathrm{BC}$, whence

$=\angle K C B$; from whence, by a quadratic equation, $x$ is found $=$ , $91{ }^{8} 3546$; and the kites height; ${ }^{1} 51,3373^{2} 373$ yards. W. W. R.

# Nn. 39. Gent. Diart ; or, Math. Repofitory, 1779: 43 


#### Abstract

- * As Mr. Beck (the propofer of the Prize Quefion) fent no folution along with it: and having this year received no fatisfactory folutions to the fame; although feveral ingenious correfpondents have attempted to give folutions thereto: yet, fome, through mifaking the daia; and others, apprehending fome ambiguity in the terms under which it is pronofed, \& $c$. Thall therefore for the prefent) omit inferting any of then; but leave the further confideration thereof to then, to another year, ơ's. fha! therefore in the next place, give fome emendations and corredions to fome folutions that have been publifhed in fome preceding Diaries.


To begin then with Quest. 7. propofed 1775 , and anfwered in 1776 . Mr . W. T. defires the following folution a place this year.

Let ABC be the garden; AI, HB , and KC, the three pillars; draw GF perpendicular to AC . and thro' $G$, draw ED, parallel to $A B$; and put $A B=B C=a$ $=295,161, A C=b,=417,4206 ;$ and put $16 \frac{1}{1} \frac{1}{2}=c$. Then, by the laws of falling bodies, ${ }_{4}^{9^{c}}=I A$; $c=\mathrm{HB}$, and $4 c=\mathrm{K} \stackrel{4}{\mathrm{C}}$; then put $x=$ the time of defcent down each plane (and p. Ig,
Emerfon's mechanics $1 \frac{1}{2}^{\prime \prime}: \frac{9 c}{4}:::_{x}^{\prime \prime}$ :
 $\frac{3 c x}{2}=I G$, and in like manner $c x=H G ;$ and $2 c x=K G$; and (per 47. $E u$. 1.) $\left.\left.\frac{3 c}{2} \times x^{2}-\frac{9}{4}\right]^{\frac{1}{2}}=A G ; c \times \overline{x^{2}-1}\right]^{\frac{1}{2}}=\mathrm{BG}$; and $2 c \times$ $\left.\overline{x^{2}-4}\right)^{\frac{1}{2}}=$ CG. Then (cor. p. 23. B. 2. Emerfon's geom.) $\mathrm{CD}=$ $\frac{a}{2}-\frac{15 c^{2}}{2 a}+\frac{3 c^{2}}{2 a} \times x^{2}:$ and $\mathrm{CF}=\frac{b}{2}-\frac{175 c^{2}}{32 b}+\frac{7 c^{2}}{8 b} \times x^{2} ;$ for which, fubftitute $u+w x^{2}$, and $m+n x^{2}$. Now (by Sim. $\triangle$ s) CB:CA : : $\mathrm{CD}: \frac{b u+b v x^{2}}{a}=\mathrm{CE}$, and $\mathrm{CE}-\mathrm{CF}=\mathrm{EF}=\mathrm{FG}=\frac{b u}{a}-m+$ $\overline{\frac{b v}{u}-n} \times x^{2}=p+s x$ by fubrtitution. Then (p. 47. Eul. I.) CF ${ }^{2}+$ $\mathrm{FG}^{2}=\mathrm{CG}^{2}$; that is, $\left.\overline{m+n x^{2}}\right|^{2}+\overline{p+\left.5 x^{2}\right|^{2}}=4 c^{2} x^{2}-16 c^{2} . \mathrm{Re}-$ duced, $x^{4}+\frac{2 m n+2 p s-4 c^{2}}{n^{2}+s^{2}} \times x^{2}=-\frac{m^{2}+p^{2}+16 i^{2}}{n^{2}+s^{2}}$ In numbers $x+408,385 x^{2}=-22926,664$. folved, $x=8,195$. Hence all the
ief is eafily reft is eatily had.
N. B. I took the times of defcent, $I, I \frac{T}{2}$, and 2 feconds, and not as printed : for, as the queffion is printed, it gives $x+-228,1932 x^{2}=-$ $16314: 4343$, which is impofibible.

The fecond Quest. 1776. anfwered alfo by Mr. W. T.
Lex K, be the center of the wheel, and put $a=\mathrm{BF}=\mathrm{DM}=$ the height of the fall; $x=$ the radius of the wheel $;$ and $z=$ the fine of the angle EKF $=$ GKF.
Then (fcho. p. 2.B. I. Emer-
fon's trig.) $2 \approx \sqrt{1-z^{2}}=$ the fine of the angle EKG= DFM; and by rigonometry
$\sqrt{1-z^{2}}: x:: z: \frac{z x}{\sqrt{1-z^{2}}}$
$=\mathrm{FE}$; and $2 z \sqrt{1-z^{2}}: \mathrm{H}$
$a:: 1: \frac{a}{2 z \sqrt{1-z^{2}}}=D F$;

then $D F-E F=\frac{a-2 z^{2} x}{2 z \sqrt{1-z^{2}}}=D E$; (and by fimilar triangles) $F D$ :
FB:: ED: $\mathrm{EC}=a-2 z^{2} x$. But the force of the wheel will be as the velocity of the water on the floats at $E$, multiplied into the radius of the wheel, or as $x \times\left.\overline{a-2 z^{2} x}\right|^{\frac{x}{2}}=$ a maximum. Which (fuppofing $z$ giver) gives $x=\frac{a}{3 z^{2}}$. From this expreffion, it is evident that if $\approx$. be variable, $x$ and confequently the force of the wheel will be greateft, when $z$ is indefinitely imall. Therefore the cafe in hand admits of no maximum in the underfbot wheel, but when the angle DFM is indefinitely fmall, and the radius of the wheel indefinitely great. But in the overfoll wheel the angle DFM is $=90^{\circ}$, and $z=$ the fine of $45^{\circ}$, and $x=\frac{2 a}{3}$.

Remark. It appears, the under/bot has greatly the advantage of the overfoo wheel, when they act by impulfe alone.
N. B. This folution is nearly the fame as that publifhej, Prob. 27 . of Mr. Emerfon's mifcellanies.

A correezed folution to Quest. 8. 1776. by Mr. W. Tp
Put $A B=a$, the given object to be cut; $\mathrm{DE}={ }^{n}$; the force acting at $\mathrm{E}=m$; and put $x$ = the fine of half the required angle, then $\sqrt{1-x^{2}}=$ the cofine; then by trigonometry, $x:{ }_{2}^{a}:: x: \frac{a}{2 x}=\mathrm{BD} . \mathrm{C}$ And, by the property of the lever $\frac{2 m n x}{a}=$
 the lorce at $B$, acting upon the perpendicular $B C$; but the force upon

No. 39. Gent. Diary; or, Math. Repofitory, 1779. 43 $B A$, is to the force upon $B C$, as the angle $G B D$ is to radius; that is as $\sqrt{1-x^{2}}: I:: \frac{2 m n x}{a}: \frac{2 m n x}{a \sqrt{1-x^{2}}}$ the force to cut $A B ;$ a maximum or $\frac{x}{\sqrt{1-x^{2}}}=$ a maximum. In fluxions, $\mathcal{E}^{\circ} c . x=\sqrt{\frac{1}{2}}=$ the natural fine of $45^{\circ}$. Hence the angle $\operatorname{EDA}=90^{\circ}$, at which the fciffars will cut the beft.

Nzw Mathematical Questions to be anfwered in the next year's Diary.
(i) Quest. 44I. by Abdolonimus.

Four equations I fend, in hopes that fome friend Will hafte for to give me relief;
By quadratic equations, and fair operations,
From hence * fhow the caule of my grief.

(2) Quest. 442. by Mr. Joseph James, of Stoke-Bißhope

IT is required to find a fquare number; fuch, that being multiplied by 4 , and that froduct leffened by 16 . the remainder fhall be a fquare number?
(3) Quest. 443. by Mr. Patrick Haid, of Denby, Derbyfhire.

A gentleman having a garden in the form of a quadrant of an ellipfe, whofe femi-traniverfe $=15$, and femi-conjugate axe = 10 yard 3 ; which he is defirous to have oivided into two trilineal fpaces, by a walk drawn from the right angle of the faid garden, and terminating in the curve; fo that the fpace lying next the greates femi-axe, may be to the other, in the ratio as 3 to 4 . Query, the greateft rectangular fith-pond that can be infcribed in the fpace bounded by the walk, the semi-tranfverfe, and the curvilineal part of the ellipfe.

## 46 New Questions to be anfwcred in next Year's Diary

(4.) Quest. 444. by Mr. John Wiles, mater of the FreeSchool, at Mark in Cleveland, by whom youth are taught the ENGicsh Language, and the various branches of the Mathewmetics.

To determine the length of the tangent (TM) drawn to touch an ellipsis (whole iameters are 40 and 30 refpeclively) in the point ( $M$ ) foch; that if the femi-ordinate (PM) and a right line (MC) from the point of contact to the center of the ellipfis be drawn; the difference of the areas of the two triangles (CPM) and (PMT) formed thereby, may
 be a minimum.
(5.) Quest. 445 . By Mr. ALEx. Rowe, of Reginnis, near Penzance o

ON the 2 If t of June, 1777, at a certain place, the fun being due east ; it was observed, that the fine of the fun's diftance from fix $0^{\prime}$ clock, was to that of his altitude, as 2 to 3 . required the latitude of the place.
 byfhire.

If the fub-tangent of a curve be exprefied by $\frac{\overline{b x-x}]^{3}}{\frac{b-x^{2} \times \sqrt{a^{2}+x^{2}}+a b}{}{ }^{3}}$
$\times \frac{\dot{y}^{2} y}{\dot{x}^{2}}$; Quere the femi.ordinate $y$; when $a=4, x=3$, and $b=1000$ yards refpeetively.

> (7.) Quest. 447. By Mr. John Wile es, of Mark.

An ere\&t declining dial declines from the South 30 degrees; and the plane's difference of longitude exceeds the fubfyles diftance from the meridian, jun equal to the co-latitude of the place. To determine in what latitude this dial is fixed.

## (8.) Quest. 448. By Mr. Thomas Walker.

Let there be a right angled triangle, and a femiparabola joined together at the leaf angle of the triangle, and vertex of the parabola, fo,
that the bafe and abfcifs may make one right line; the legs of the triangle being 80 and 60 ; and abfcifs and greateft femioroinate of the parabola 80 and 50 . Required the dimenfions of the greateft parabola that can be infcribed in the fpace contained by the regment of the hypothenufe, tangent, and curve; when the tangent is drawn fo as to divide the area of the triangle in the ratio of $3: 2$.

## (9.) Quest. 449. By Mr. William Winn, of Tbirf, Yorkflire.

On a certain day in 1777, at $60^{\circ}$ clock in the morning, as I was fitting in a room, the Sun fhining in at the window, I obfeved the rays to fall on the cieling of the room from a reflecting body on the floor (which was an horizontal plane,) I oblerved the fame, when the SUN was due eaft, and meafured the diftance of two rays upon the cieling, and found it $\mathbf{1 2 , 8 4 6 0 6 4}$ feet. Moreover, I found the fum of both the refiected rays from the cieling to the body, to be to their difference, as 12,846064 to 2,646224 . Required the latitude; the time of the year; and the height of the room.
(10.) Quest. 450. By Mr. Ralph Thompson, of Witherley Bridge.

What are the dimenfions of the area, of the greatef femicubical parabola that can be infcribed in an annulus, with its vertex in the inner circle ; the fum of whofe circumferences is 125,664 ; and difference of their diameters $=20$. And alfo, the length of a chord of the outer circle perpendicular to its diameter, that will cut off one half of the faid parabola,

## (ii.) Quest. 45i, By Mr, Wiletam Sherwin, of Afon, upon Trent,

A noted furveyor of land, in meafuring a nobleman's park, found a Gifh-pond; upon the brink of which grew a ftately oak, whofe neareft diftance from the park wall was 1,5 chains; and he obferved, that the angle (at any point of the brink of the-pond,) fubtended by that perpendicular height of the wall which was in a right line with that point and the oak tree was $1^{8} 1^{\prime} 43^{\prime \prime}$; and the height of the wall was 4 yards. From whence he defires fome ing wious diarian, will in the next year's Diary, tell him the exact area of the pond.
(12.) Quest. 452. By Mr. Thomas Walker.

Given the time of evacuation of a paraboloid thro' a circular hole in the vertex of $1 \frac{1}{2}$ inch diameter $19^{\prime}{ }_{2} 3^{\prime \prime} 12^{\prime \prime \prime} \frac{1}{2}$ the neareft dißance from the middle of the bafe to the curve furface 45,161175 inches ; tequired the diameter and folid content?

48 New Questions to be anfwered in next Year's Diary.
(13.) Quest. 453. beingthe Prize Quest. by Mr, Isaac RowдотTOM.

A gentleman has a garden in the form of the trapezium $A B C V$, in which are two canals a triangular one ABO, and another AVC, bounded by a fraight walk $A C$, and two equal curved ones AV, VC, uching each other in their vertices V , whofe equation is $p x=y 3$.

Now, on a certain day in the fpring, ${ }^{1777}$, I being employed in furveying his eftate, obferved that at $55 \frac{7}{15}$ min. paft $6 a^{\text {c clock }}$ in the morning the fhadow of a faff 6 feet long erected at $\mathbf{C}$, fell upon the walk KC, and its length was 15,87872 feet; but $1 \frac{17}{225}$ hours after, it fel! upon the walk CO , and its length
 was then but 7,52444 feet: alro at $\frac{137}{450}$ hours paft noon on the fame day, the fhadow of a tree fanding perpendicular to the horizon at $A$, fell upon $A B$ : moreover, I found that if a right line was drawn from $\mathbf{C}$, and another from $A$, to the fummit of a fir flanding perpendicular to the horizon at $O$, the angles formed by thefe lines and the horizon would be $5^{\circ} 14^{\prime} 47^{\prime \prime}$ and $17^{\circ} 32^{\prime} 10^{\prime \prime}$. Thefe are all the dimenfions that can poffibly be procured, only (from an old plan of this garden,) we found, that when the walks AV,VC were made, they took the leaft quantity of materials poffible; and the gentleman him felf, remembering that the angle $A B C$ was right; and that the canal AVC, exceeded ABC, by 2 a. I $r \cdot 36,3 \mathrm{I} p$. It is requefted, that fome of your ingenious correfpondents, will give the dimenfions of each feparate past of this garden, fo that the true area thereof may be known.


[^0]:    Mr. Edward Parmel, Mr. Alexanter Rowe, and Mr. Ralpb T'bompfor, (the piopoferst are exactly the fame; which want of room will not admit of infertion; but take notice of the following remark. It appears that the two firft folutiong bef answer the conditions of the queftion: for the area of the nurfery in eacis are the fame (although the canals are taken the contraty way of the parallelogram) So

